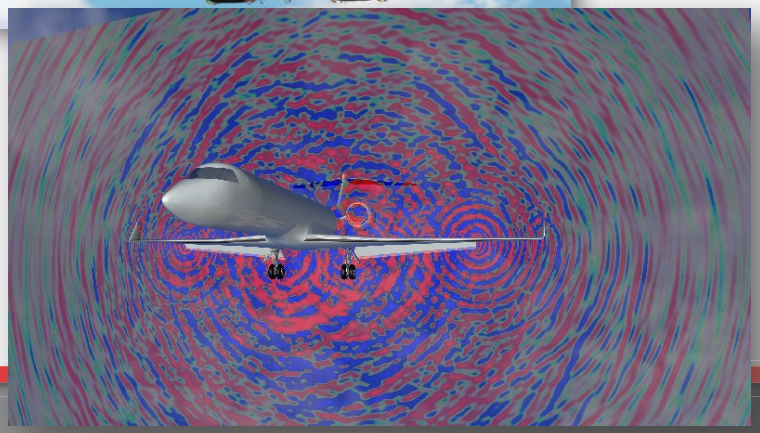




# Recent Advances of the Lattice-Boltzmann Method for the Simulation of Transonic Flows

**Swen Noelting**

With contributions from : Hudong Chen, Raoyang Zhang, Pradeep Gopalakrishnan, Yanbing Li et al

Ehab Fares, Damiano Casalino, Benedikt König, Benjamin Duda, André Ribeiro et al

**Applied Modeling & Simulation (AMS) Seminar Series**

May 10, 2016

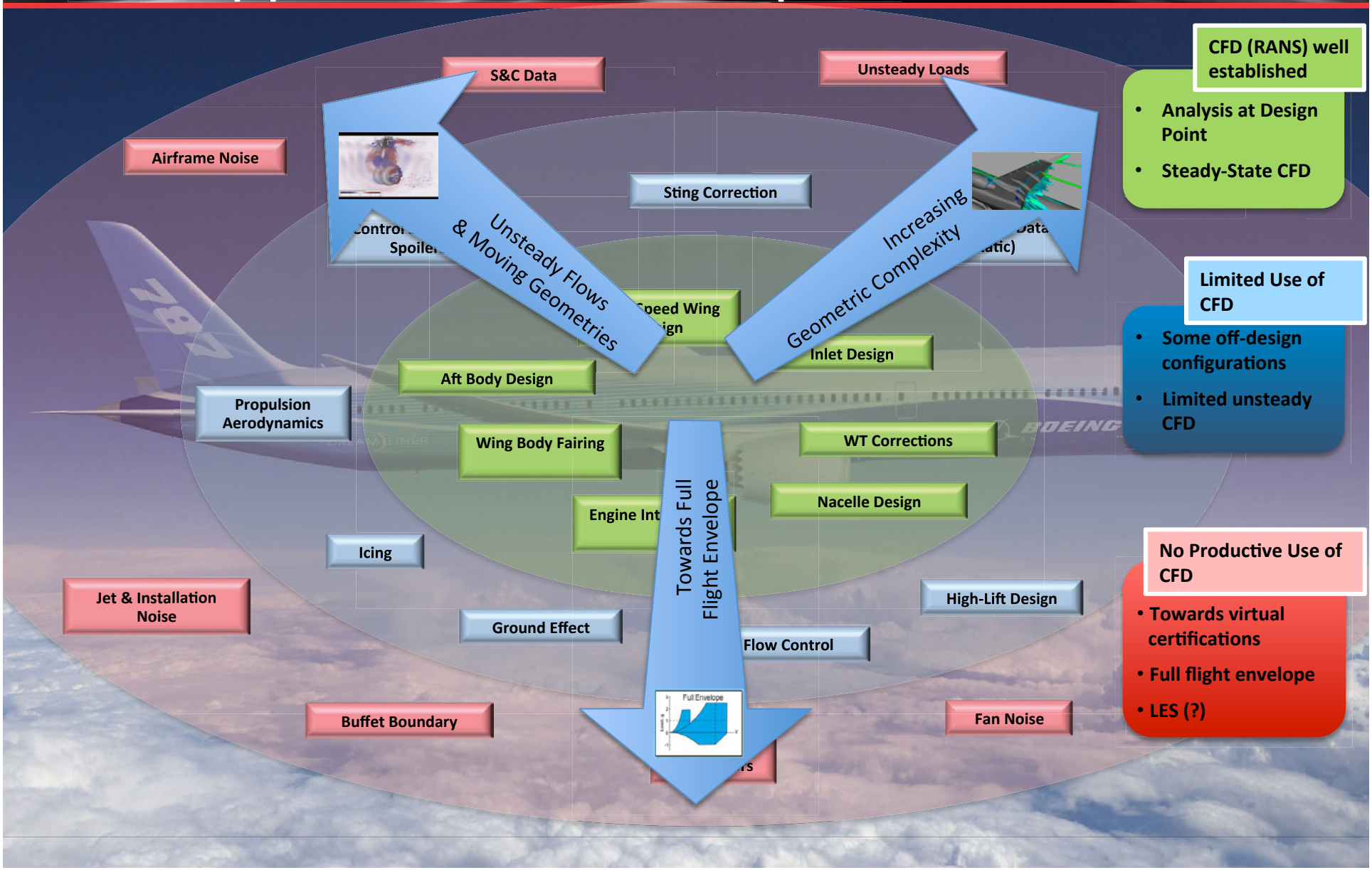
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# Outline

- Motivation: CFD Applications in Aerospace
- Overview of PowerFLOW Projects at NASA
- Theory & Background
  - *LBM*
  - *Turbulence model*
  - *Wall treatment*
  - *Extension to transonic flows*
- Transonic Code Validation and Application Examples
  - *Fundamental Validations*
  - *Industrial Application Examples*


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# CFD Applications in Aerospace



# Motivation – Vision 2030

- CFD Vision 2030
  - *2014 Report to NASA by Key Industry Players (Boeing, Lockheed, Pratt&Whitney,...)*
- Main challenges for CFD to move beyond current status:
  - *Efficient handling of unsteady turbulent flows with significant regions of separation*
  - *Mesh generation*
  - *Robustness and automation of CFD simulations*
  - *Efficient use of HPC infrastructure*
  - *Managing very large amounts of data*
  - *Multi-disciplinary analysis & optimization*
- Hybrid RANS-LES and wall-modeled LES seen as best prospects
- Can LBM provide a contribution to address these challenges?

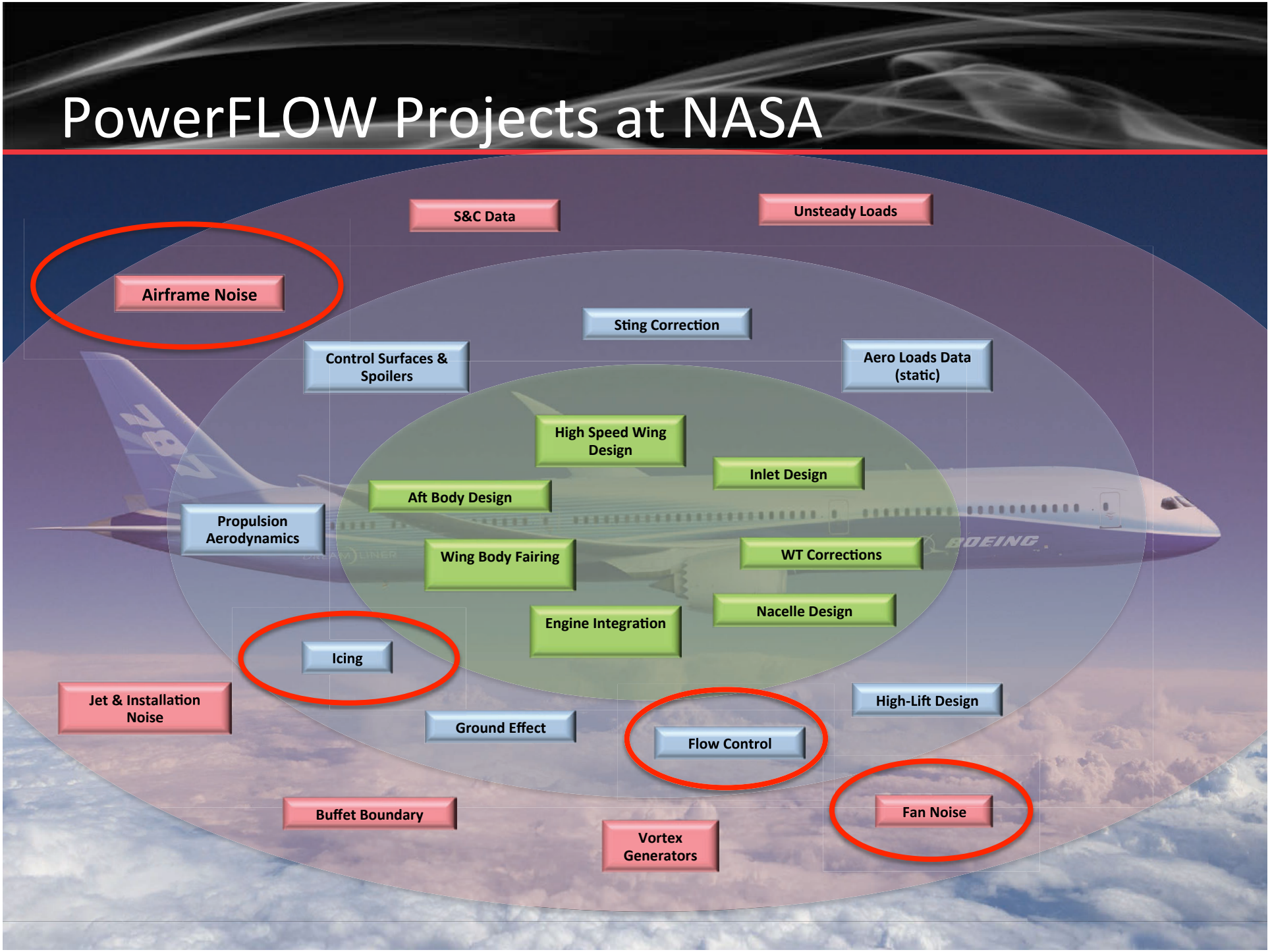

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# PowerFLOW Projects at NASA



# Aeroacoustic Predictions

## NASA ERA Project

- **Simulation-based airframe noise predictions**
  - Simulated geometry: As–built 18% scale Gulfstream model
  - Baseline configurations
    - 39º flap deflection, main gear removed
    - 39º flap deflection, main gear deployed
  - Most flap and gear concepts simulated prior to wind tunnel testing
    - ROLD, FENoRFins, FLEXSEL, etc.
    - Solid and porous versions of knee, wheel, brake fairings
  - Sample quiet configuration
    - FENoRFins plus fully treated main gear

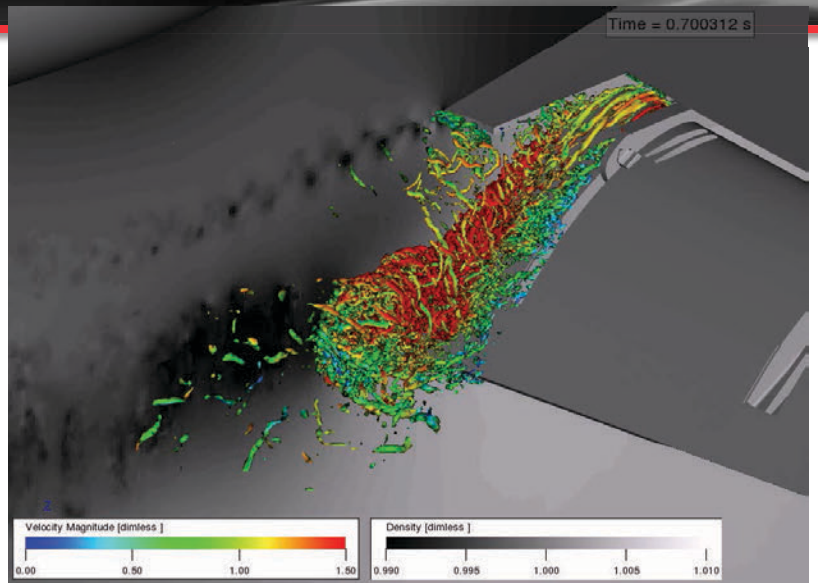


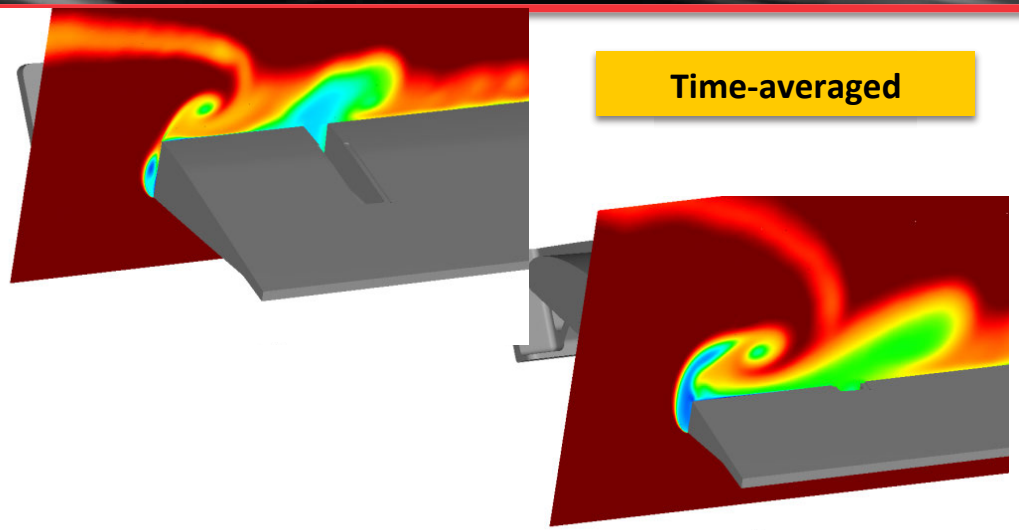

- **Accomplishments**
  - Predicted farfield noise for baseline and quiet configurations in good agreement with14x22 measurements
    - Established computational simulations as an accurate predictive tool
    - Paved the way for application to full-scale


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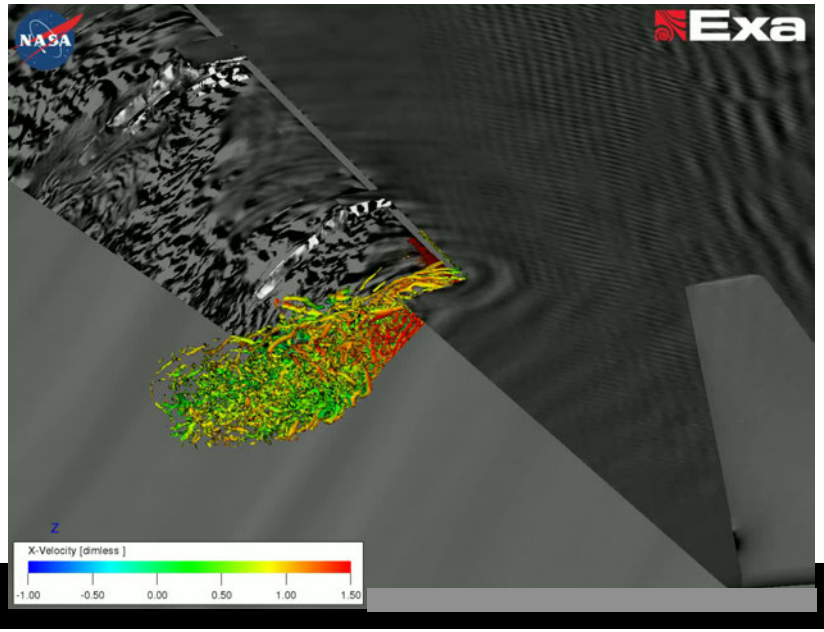
# Airframe Noise – Flap Edge Noise

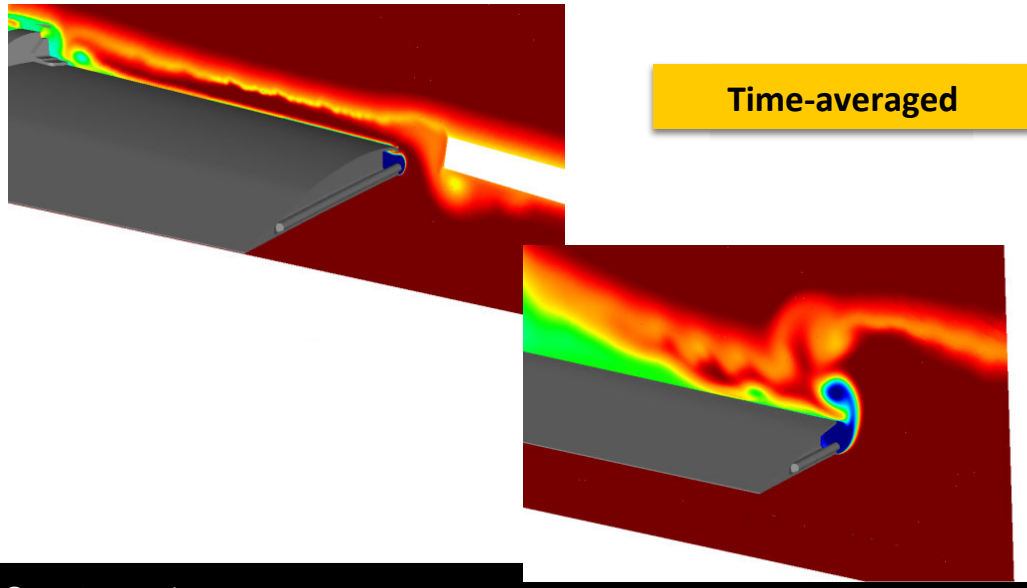
**NASA ERA Project – G550**



**Time-averaged**

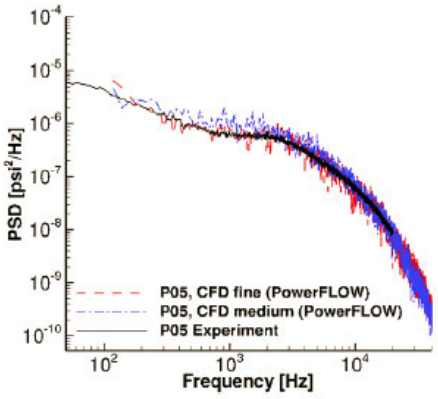


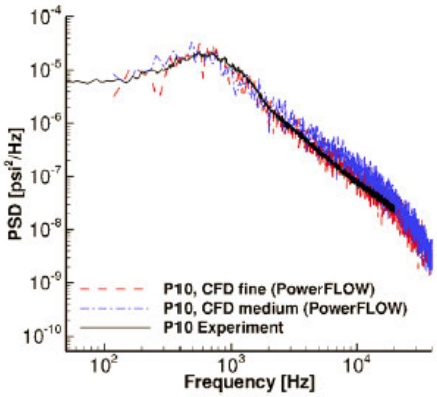
**Time-averaged**

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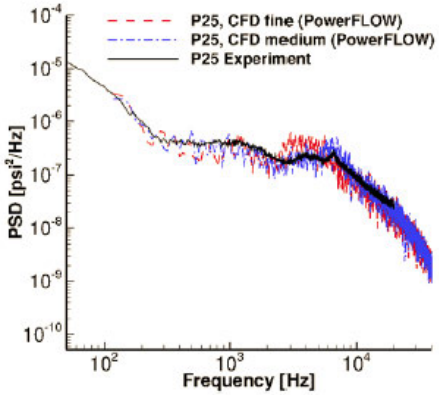
# Airframe Noise – Flap Edge Noise



d) Probe 5 location



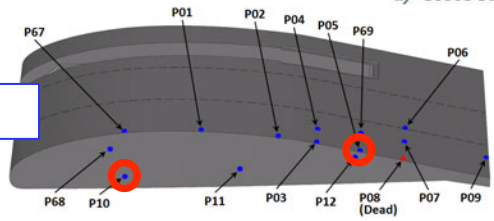
a) Probe 10 location

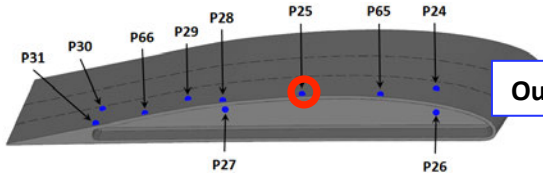


b) Probe 25 location

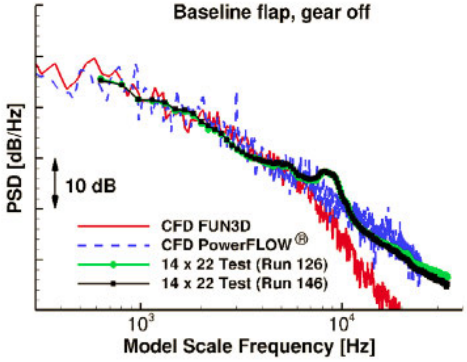
**Surface Probes**

**Inboard Flap**




**Outboard Flap**

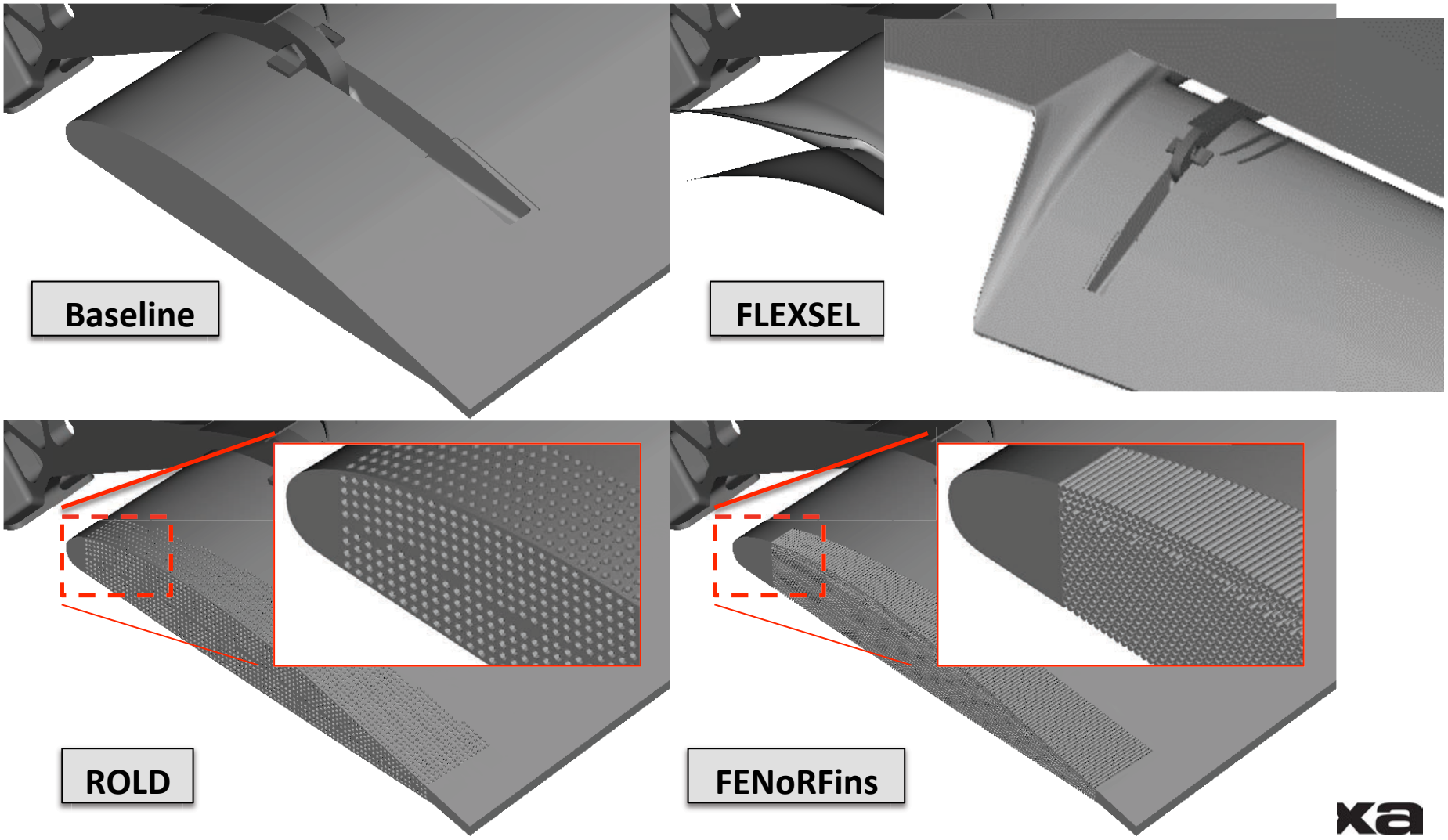



**Far-Field Probes**

All simulations were carried out prior to wind tunnel tests


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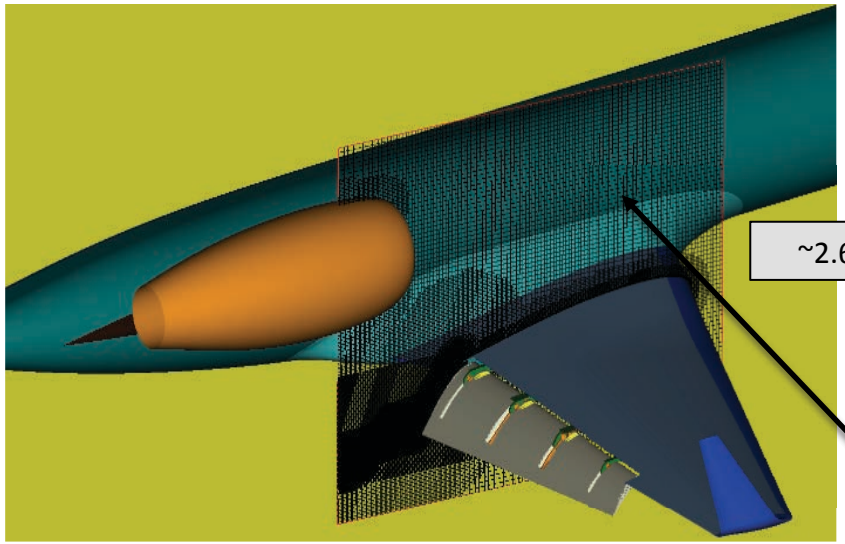
# Airframe Noise – Noise Reduction Concepts



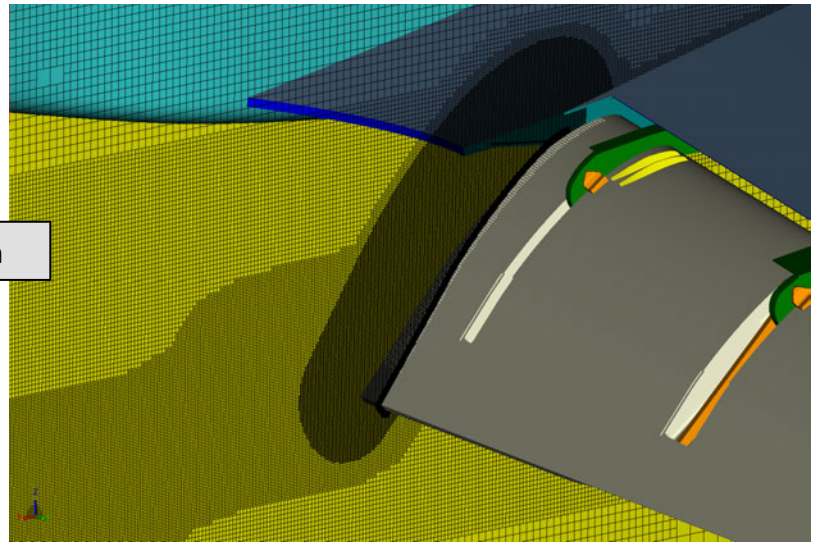


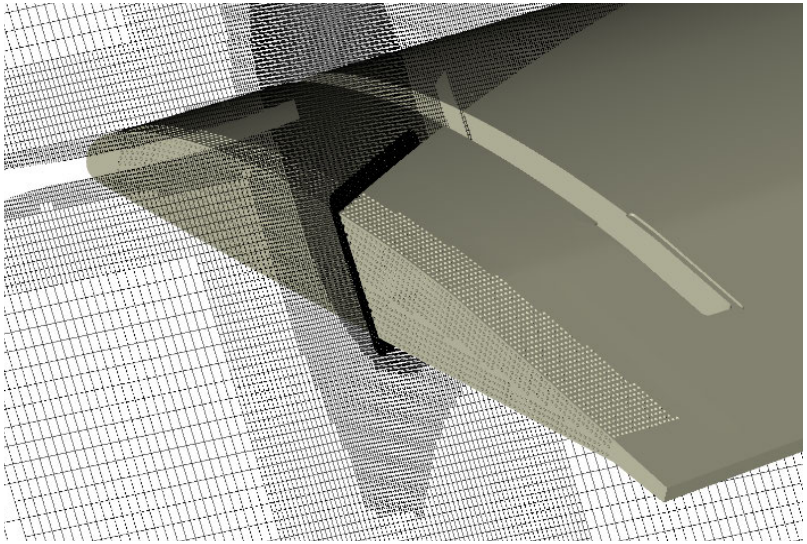
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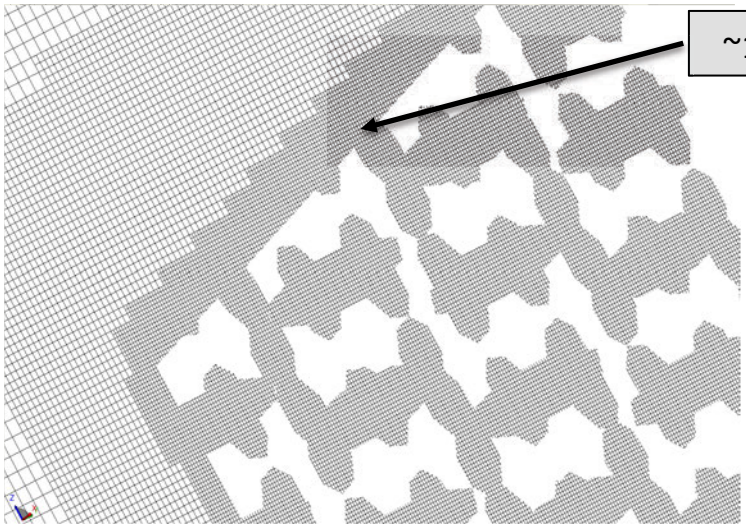
# Computational Mesh



~2.6m half-span







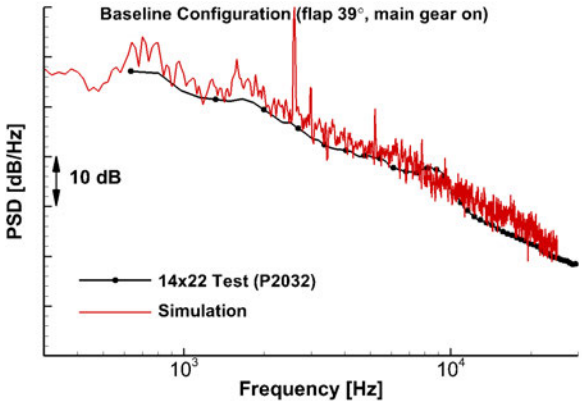
~1mm hole size

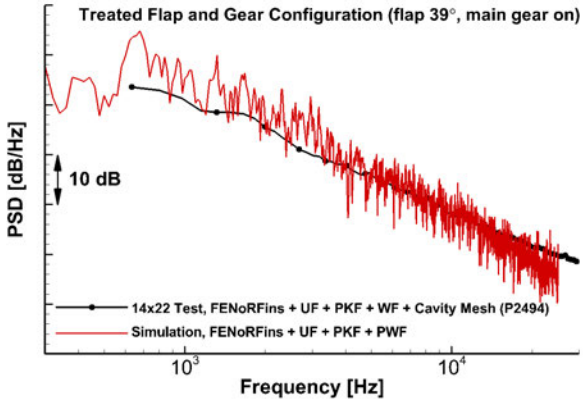


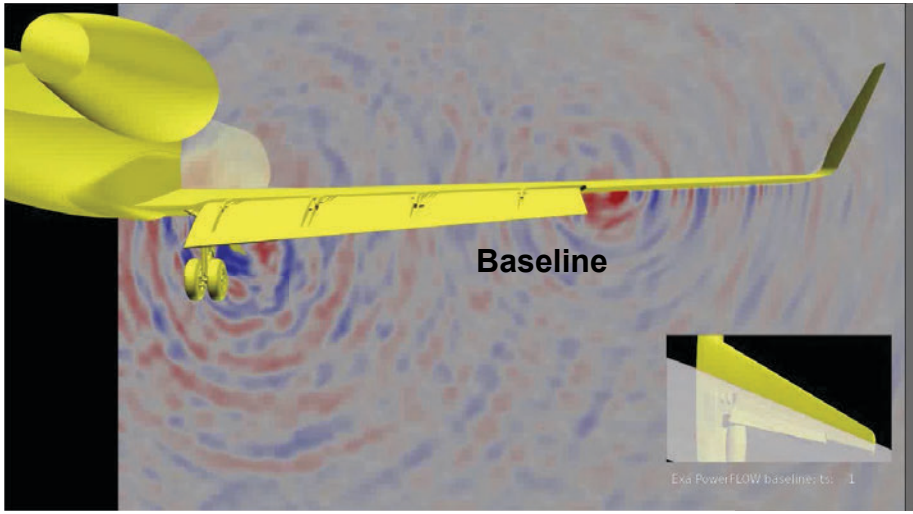
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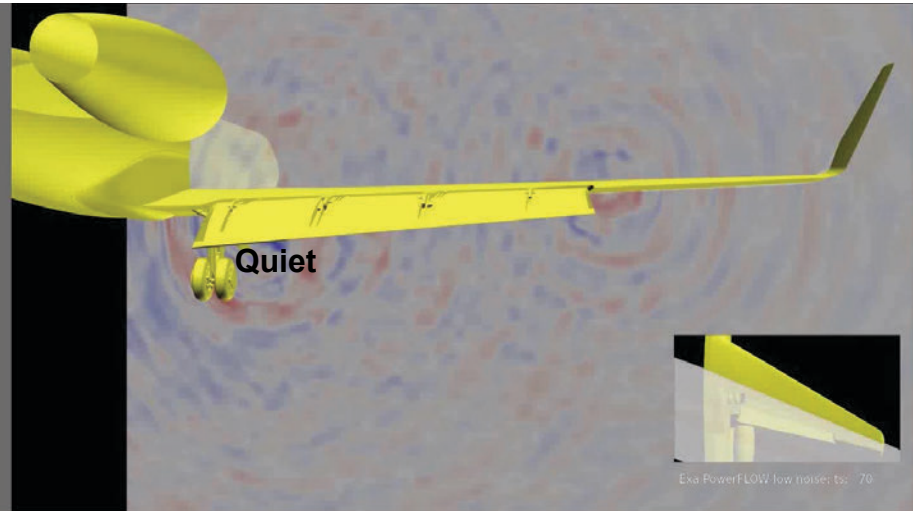
# Baseline v. quiet Configurations

**Flap 39º, main gear on configuration**



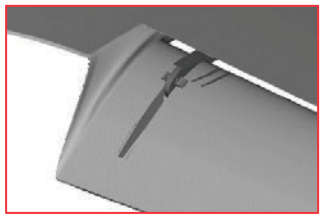



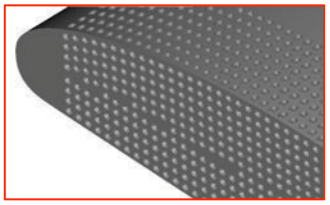


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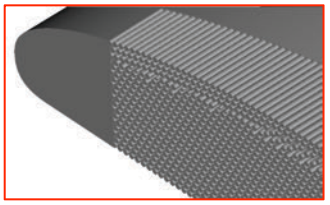
# Flap Noise Reduction Concepts



FLEXSEL



ROLD



FENoRFINS

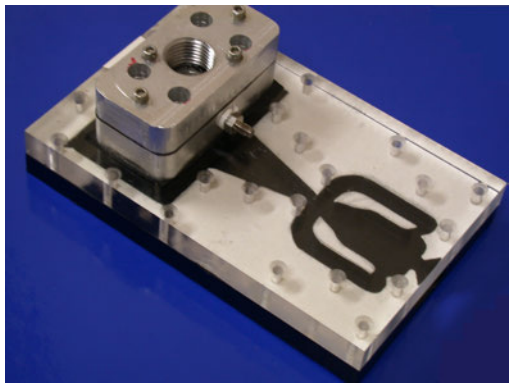
| | Experiment 14x22 WT | | | PowerFLOW Simulations | | |
|---|---|---|---|---|---|---|
| | FLEXSEL | ROLD* | FINS* | FLEXSEL | ROLD* | FINS* |
| 👎 (baseline – concept) OASPL [dB] (1kHz – 30kHz) | 3.6 | 3.9 | 3.5 | 4.3 | 4.7 | 3.9 |

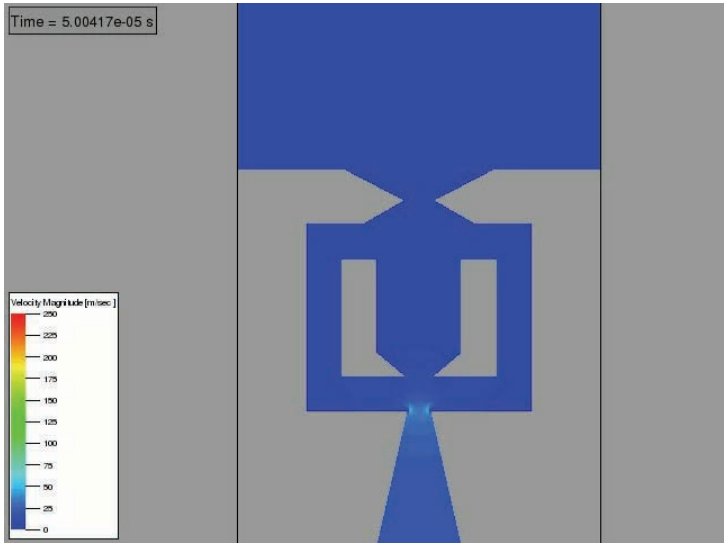
All simulations were carried out prior to wind tunnel tests

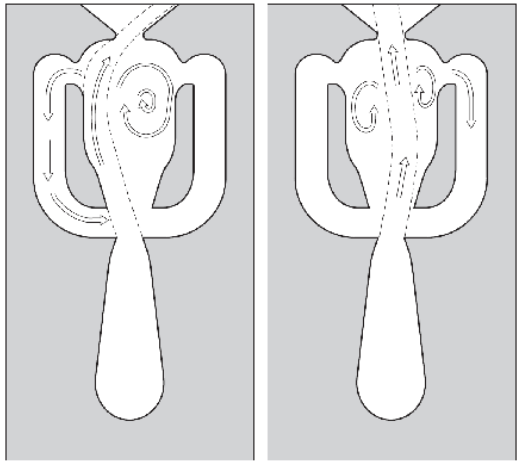
***The aerodynamic values shown here correspond to the smallest holes and fin diameter tested**


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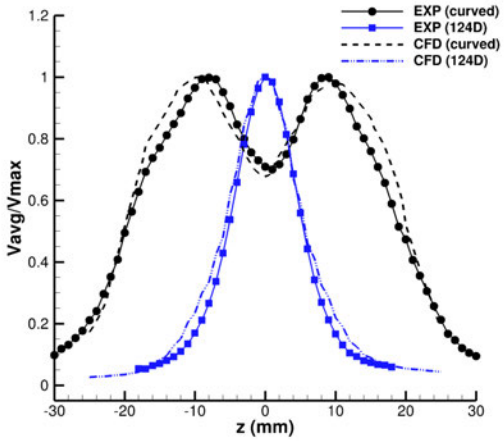
# Flow Control

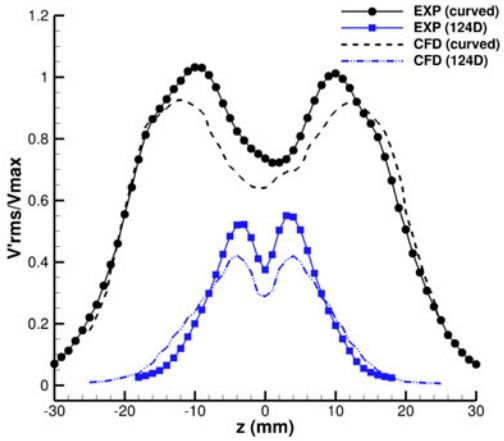





**Source**
AIAA 2012-3239

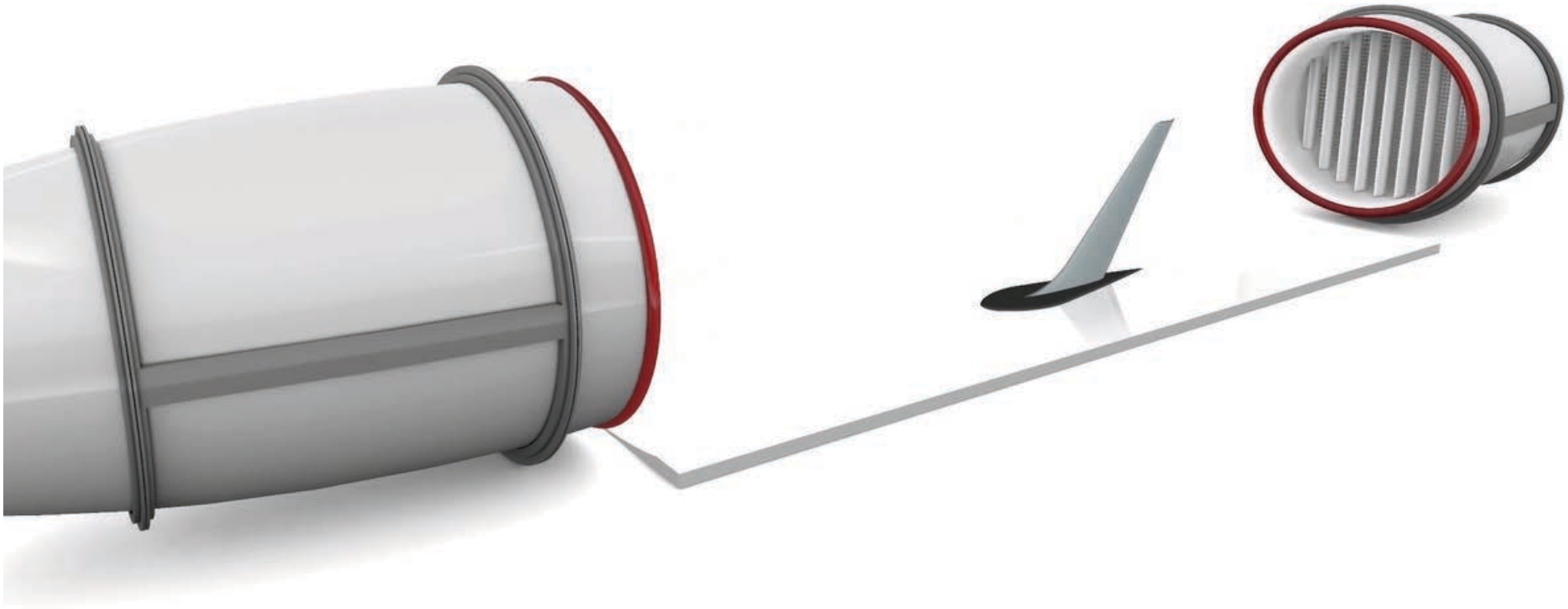




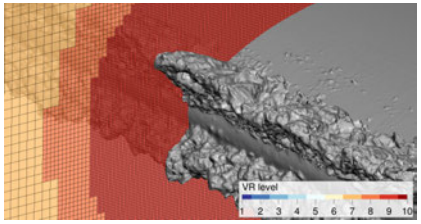
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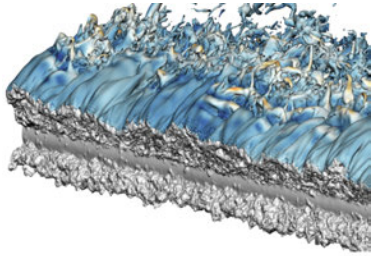
# Tail Rudder with Active Flow Control



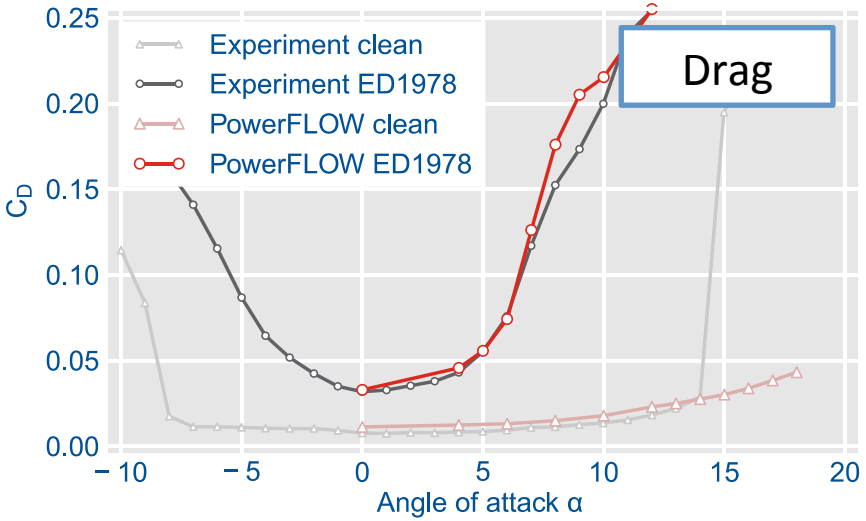

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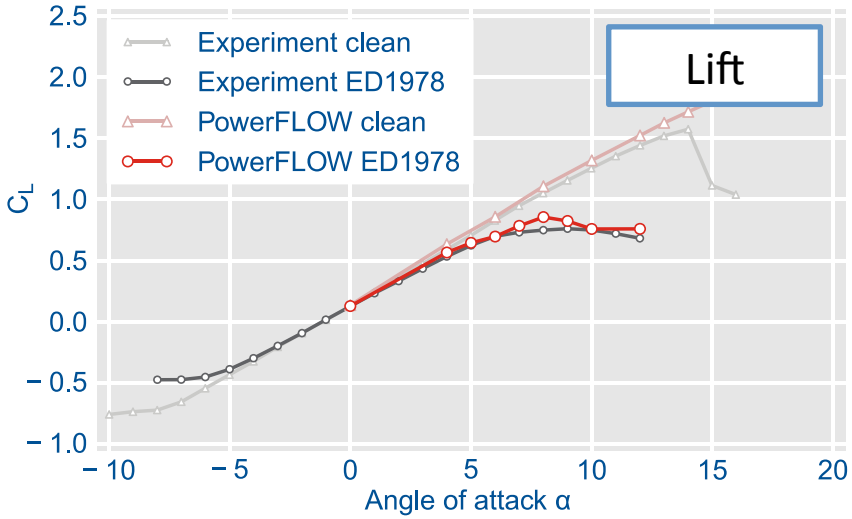
# Aerodynamic Simulation of Realistic 3D Ice Shapes

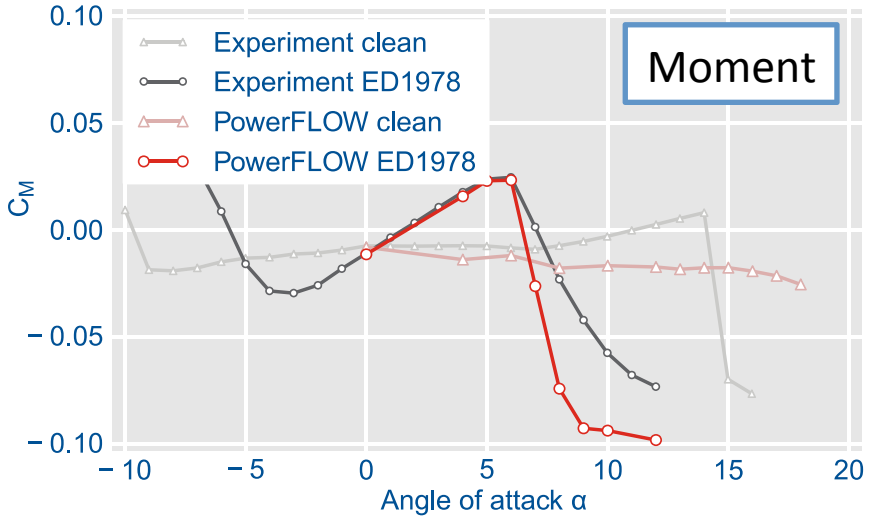


3D Ice Shapes provided by NASA/Glenn



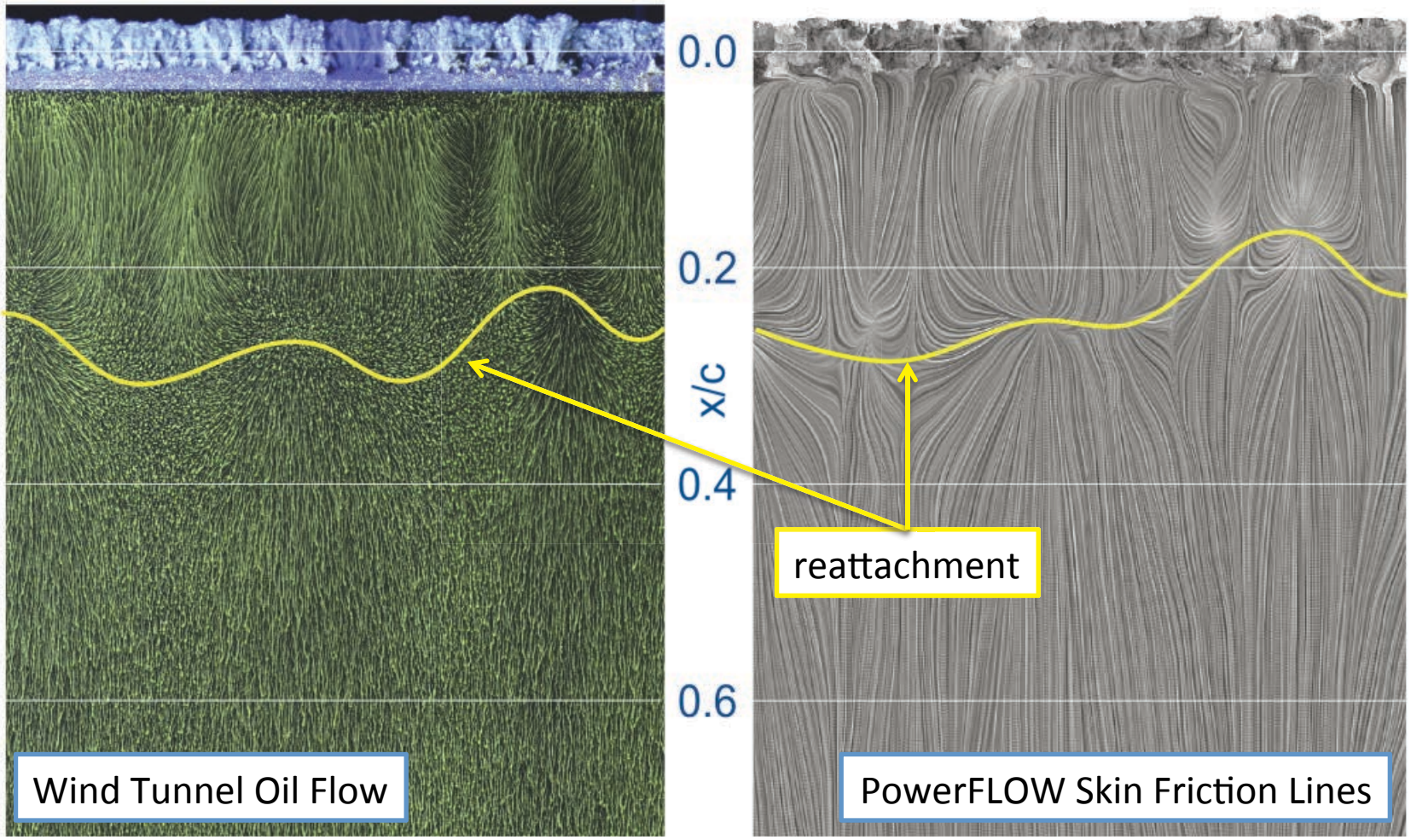





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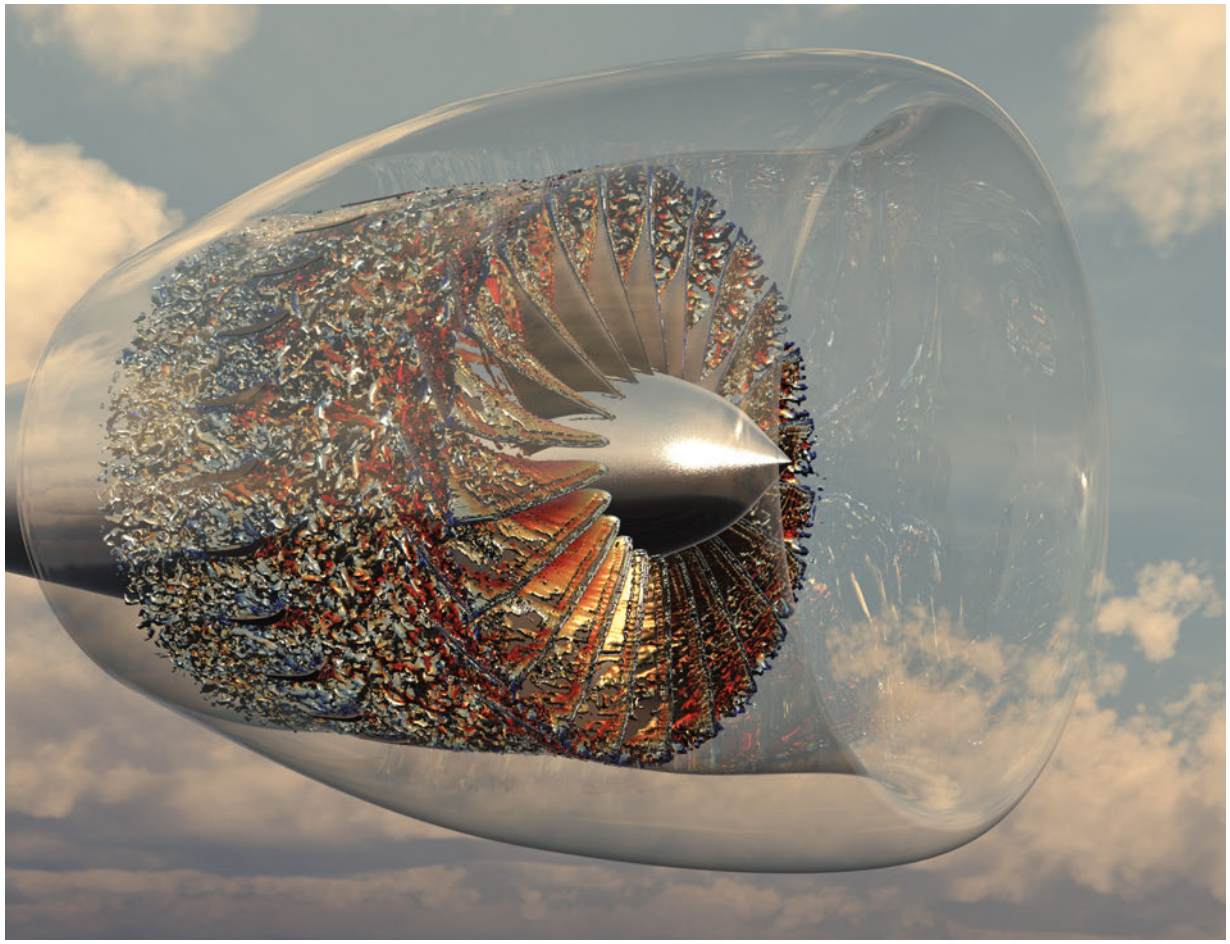
# 3D Ice Shape – Surface Flow Visualization





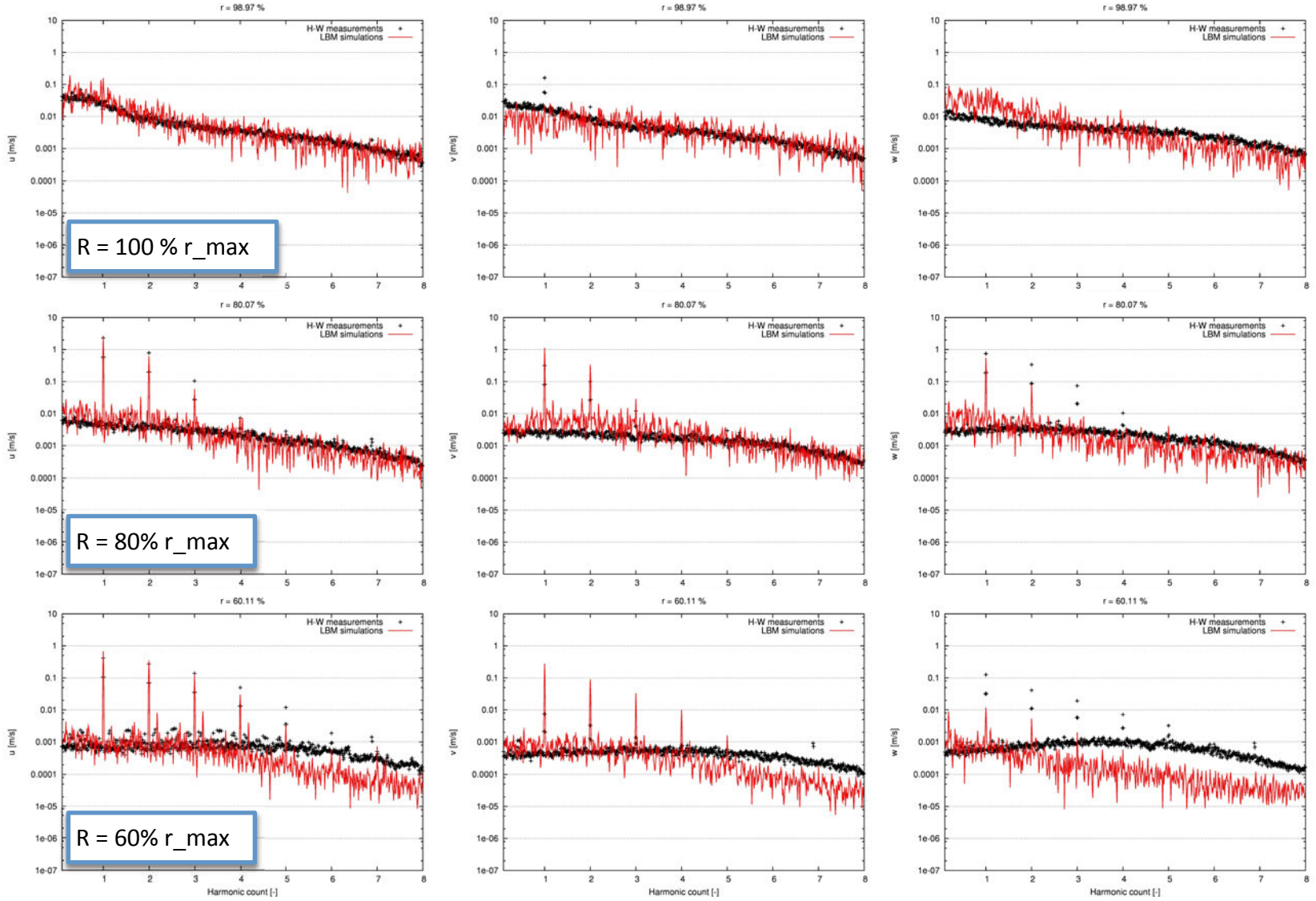
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# Fan Noise: RC2 Fan/OGV Configuration




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# Flow results between rotor & stator – comparison with NASA measurements

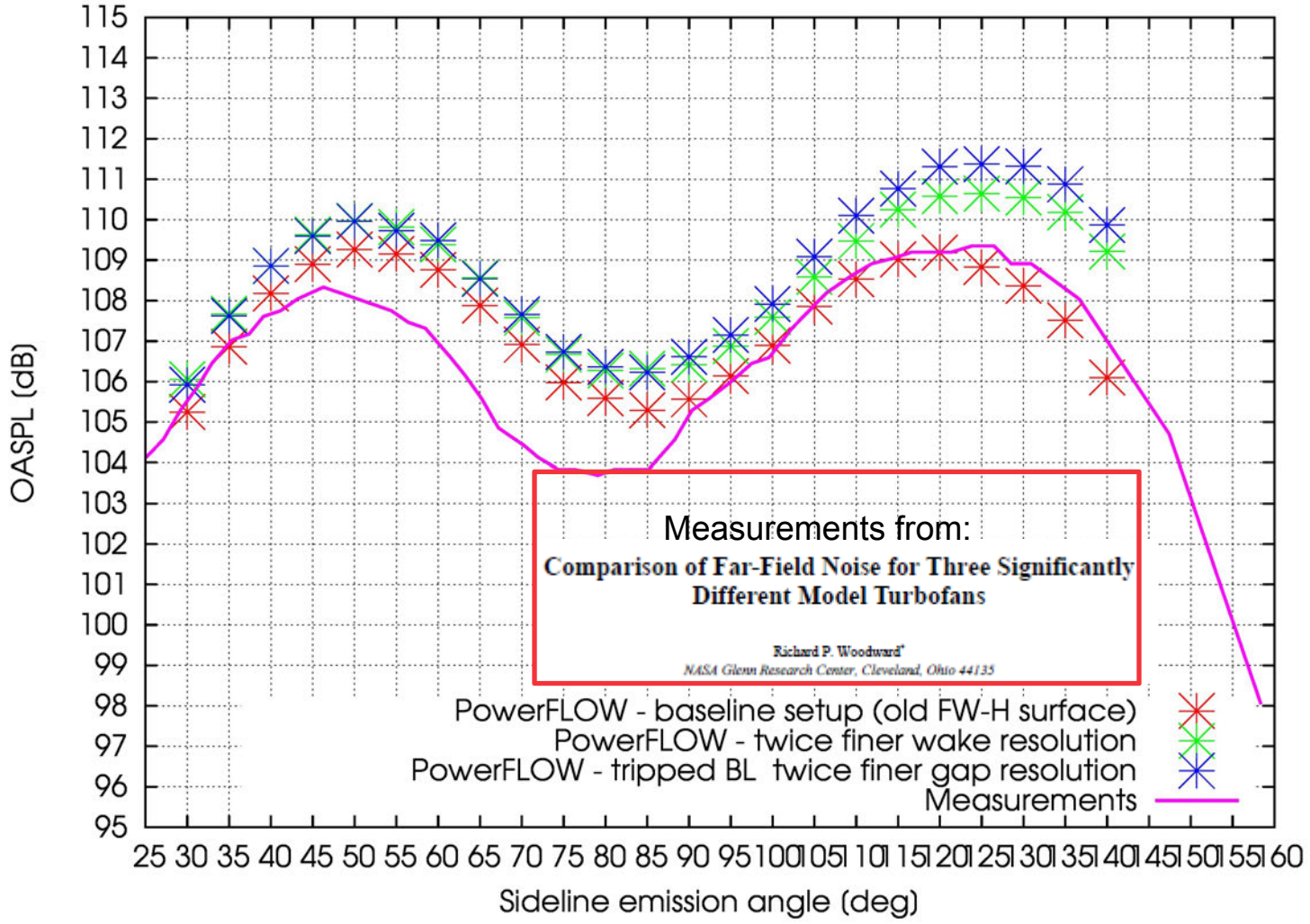



Velocity spectra Tripped



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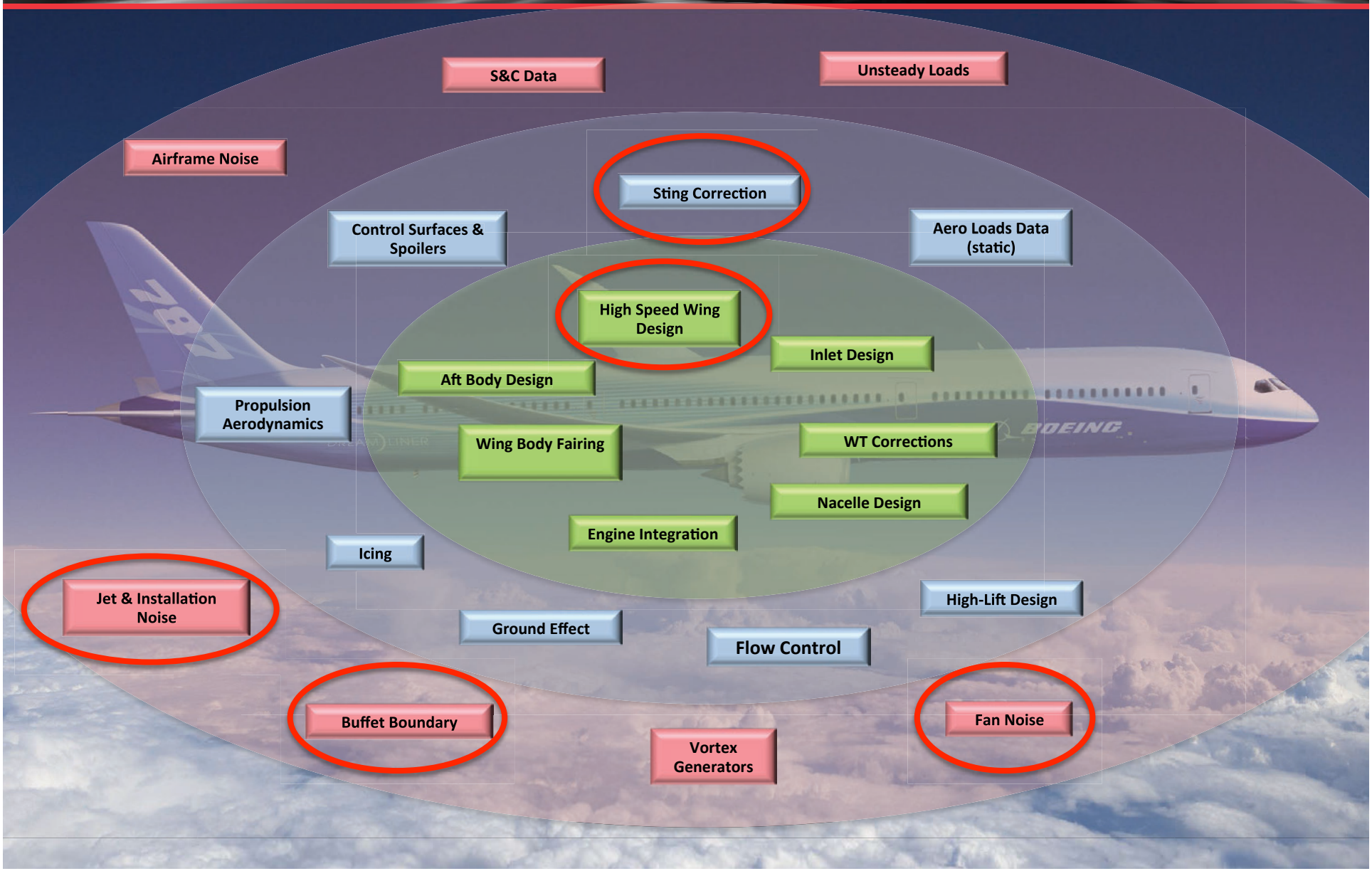
# Far-field noise results





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# High Speed Applications



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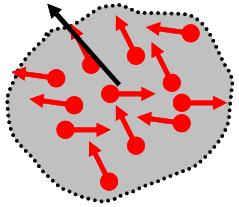

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# Kinetic theory: Basics

Boltzmann kinetic theory describes fluid behaviour based on particle density distribution function

$$f\left(\vec{x},\vec{c},t\right)$$

particle number density at time t and position x with velocity ***c***



**Boltzmann Equation:**

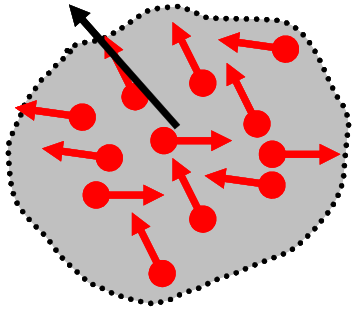
$$\frac{\partial}{\partial t} f\left(\vec{x},\vec{c},t\right)+\vec{c}\cdot\nabla f\left(\vec{x},\vec{c},t\right)=\Omega$$

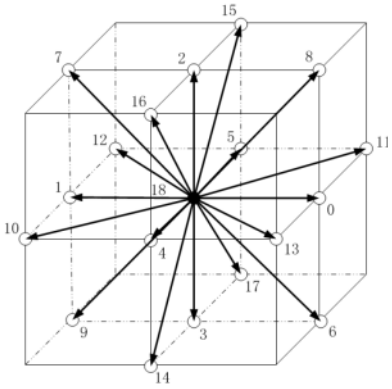
- LHS represents advections of particle distribution in space at fixed velocity for each ***c***
- RHS defined the collision process that involves inter-particle interactions
- Collision process can be modeled as simple relaxation to its equilibrium state (e.g. the BGK form*)


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# Lattice Boltzmann Methods

Discretization in space and time, using a finite set of discrete particle velocity values to represents the hydrodynamic properties*:






D3Q19 lattice

**Lattice Boltzmann Equation :**

$$f_i\left(\vec{x}+\vec{c}_i,t+1\right)-f_i\left(\vec{x},t\right)=\Omega_i\left(\vec{x},t\right)$$

**BGK form of collision:**

$$\Omega_i\left(\vec{x},t\right)=-\frac{1}{\tau}\left[f_i\left(\vec{x},t\right)-f_i^{eq}\left(\vec{x},t\right)\right]$$

Lower order LBE model recovers the Navier-Stokes equation at the nearly incompressible limit**

*Chen & Doolen 1998 **Qian et al. 1992., Chen et al 92


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# Lattice Boltzmann Methods

- Macroscopic quantities are direct results of the moments of particle density distributions
  - *Density* $\rho(\vec{x},t) = \sum_i f_i(\vec{x},t)$
  - *Velocity* $\rho(\vec{x},t)\vec{u}(\vec{x},t) = \sum_i \vec{c}_i f_i(\vec{x},t)$
  - *…*

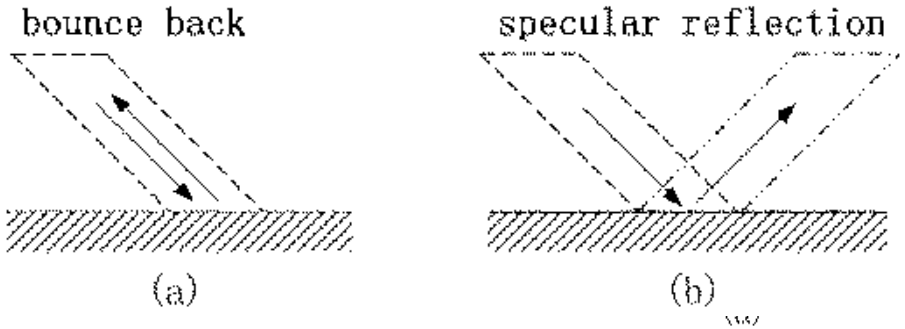
- Pressure obeys the thermally perfect gas law

$$P = \rho\theta \qquad \theta = RT$$


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# LBM Surface Dynamics

- No-slip/freeslip BCs are achieved via bounce-back/specular-reflection process*




- Momentum flux across the fluid-solid interface corresponds to surface pressure and wall shear stress*

$$\mathbf{F} = p\hat{n} + \tau_w \hat{t} \quad \sim \quad \sum_{m \in Pgrams,out} \left[ \left( \vec{c}_m f_m \right)^{out} - \sum_{n \in Pgrams,in} \left( \vec{c}_n f_n \right)^{in} \right]$$

- Generalized slip algorithm has been formulated to realize turbulence wall boundary conditions (slip velocity with imposed wall frictions)


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# Remarks

- Properly constructed LBE models can recover N-S physics, … and beyond!
- LBM is a very accurate solver with extremely low numerical dissipation
  - *Convection is exact due to the limited discrete velocities*
- Very efficient for performing time dependent flow simulations
- A very robust solver due to realizability, and stability condition is *a priori* guaranteed

- Plus …. Special Features of LBM Implementation in PowerFLOW
  - *Near wall physics (surfel concept)*
  - *LBM-VLES turbulence model*
  - *Variable resolution*
  - *Efficient parallel implementation*
  - *Extension to supersonic speeds*


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# LBM-VLES Turbulence Model

- LBM-VLES turbulence model concept
  - *Single turbulence model for all flow conditions*
  - *Resolved turbulent structures are simulated directly, unresolved scales are modeled*
  - *Subgrid contributions are accounted for by an effective relaxation time scale*

$$f_i(\vec{x}+\vec{c}_i\Delta t, t+\Delta t) - f_i(\vec{x},t) = -\frac{1}{\tau}\left(f_i - f_i^{eq}\right) \quad \Rightarrow \quad F_i(\vec{x}+\vec{c}_i\Delta t, t+\Delta t) - F_i(\vec{x},t) = -\frac{1}{\tau_{effective}}\left(F_i - F_i^{eq}\right)$$

- Modification of turbulent flow relaxation time
  - *Derived from a systematic renormalization group (RNG) procedure*

$$\tau_{effective} = \tau_0 + \tau_{turb}, \qquad \tau_{turb} = C_\mu \frac{k^2}{\varepsilon}\frac{1}{T\sqrt{1+\tilde{\eta}^2}}, \qquad \tilde{\eta} = \psi\left(\eta_s, \eta_\Omega, \eta_h \ldots.\right)$$

  - *where $\tilde{\eta}$ is the time scale of mean flow (strain, swirl, buoyancy, ….)*
  - *Effectively reduces eddy-viscosity in regions of high vortical fluctuations (e.g. separated regions)*
  - *Conceptually similar to DDES & SAS*

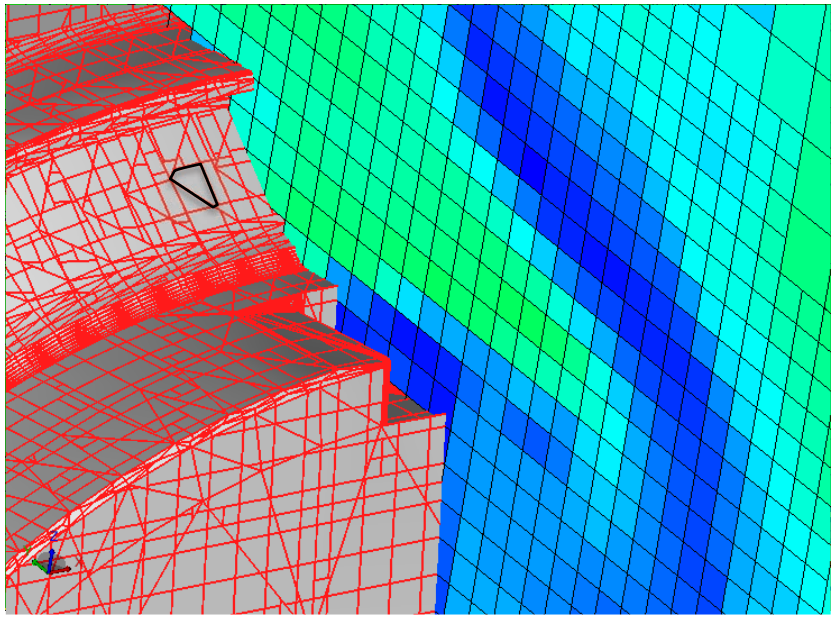
- LBM-VLES contains HOT to account for non-linearity of the Reynolds stress

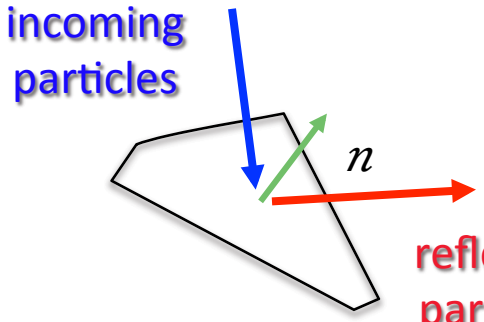
Chen, H., et al. "Expanded analogy between Boltzmann kinetic theory of fluids and turbulence.“, JFM, 2004.


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# Near Wall Physics in PowerFLOW

- Surfel Concept
  - *Arbitrary orientation & shape of elements*
  - *Near wall Sampling*
    - All needed weights pre-computed based on near wall volume elements
    - Ensure Conservation
  - *Momentum exchange*
    - Correspond to changes in pressure and friction
  - *Second Order Accuracy*
  - *Extended wall model for high Re#*
    - Including pressure gradient effects

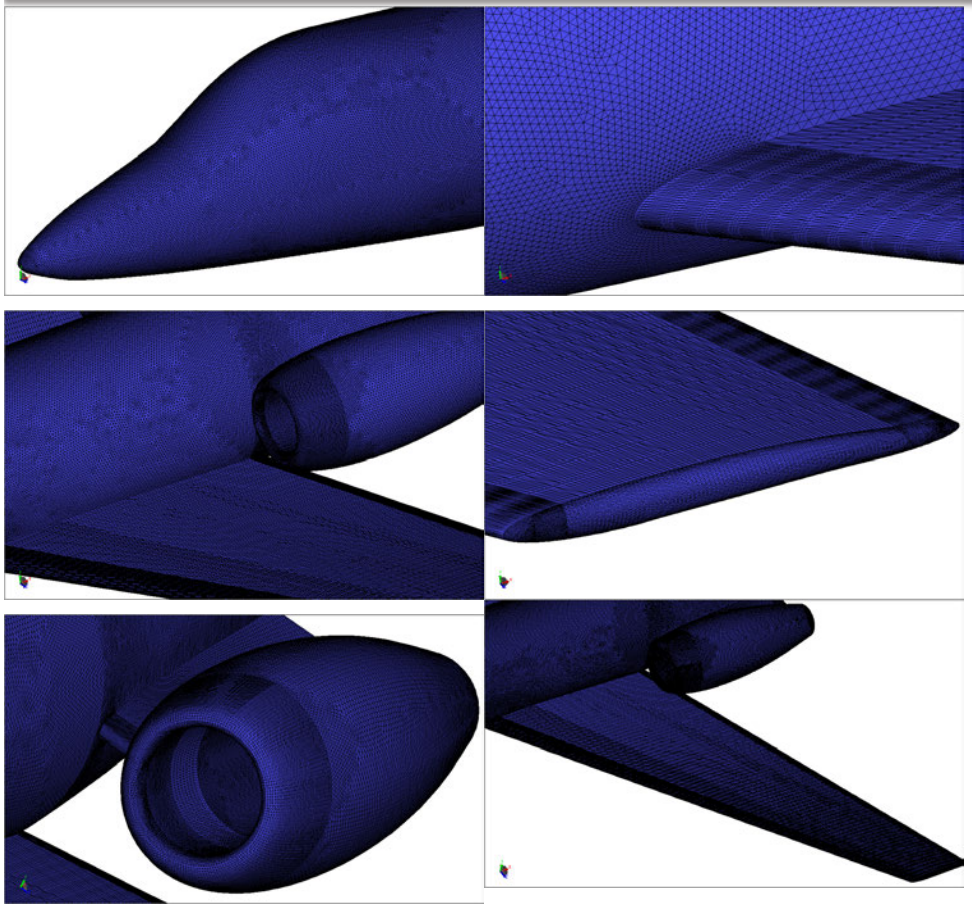


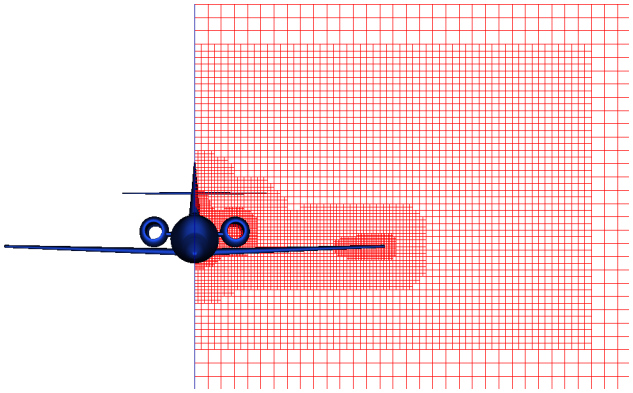


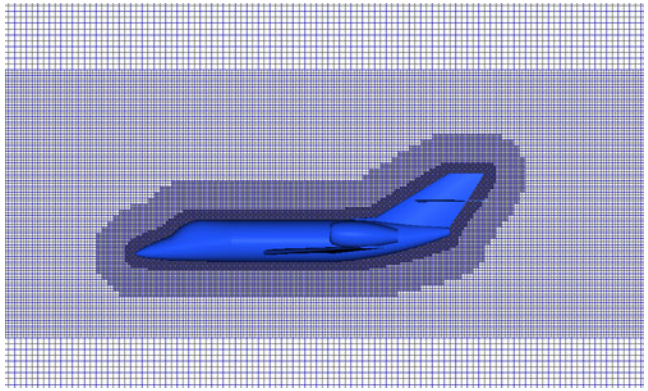


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# Typical Cartesian Grids Generation



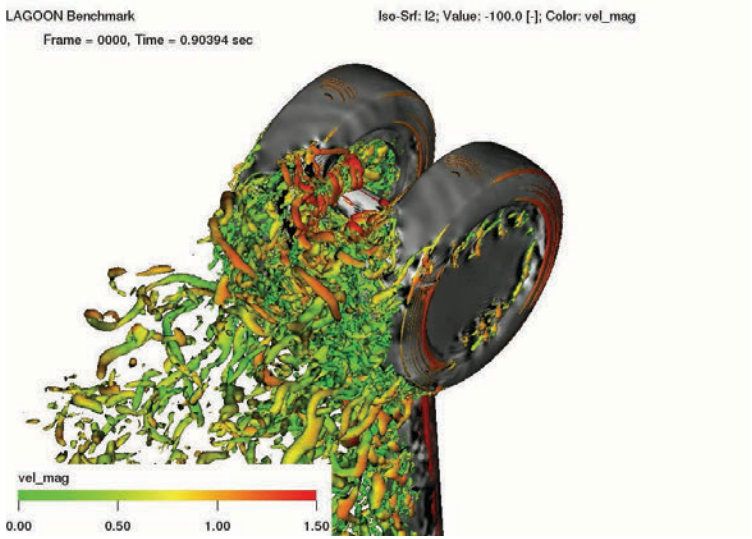




Once surface grids and regions of refinement are defined, volume grid generation is fully automatic


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# Efficient Parallel Implementation

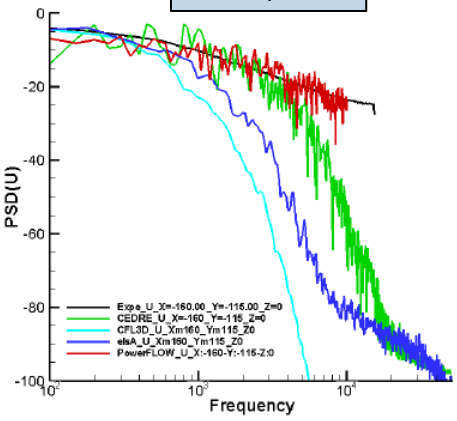



| | Power-FLOW | CFL3D | CEDRE |
|---|---|---|---|
| Turb. Model | VLES | MDDES | ZDES |
| Number of Elements | 123M | 43M | 61M |
| Number of Procs. | 276 | 240 | 480 |
| CPU-hrs for 1s simulated time* | 21,000 | 854,000 | 1,960,000 |

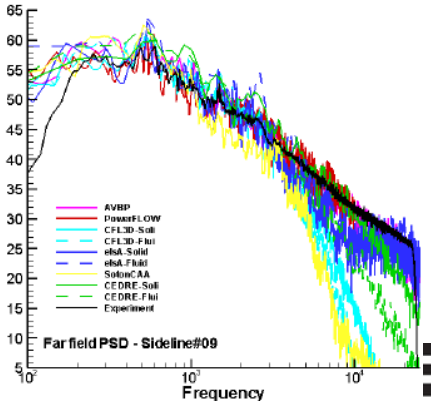
* Manoha (Onera), Caruelle (Airbus), AIAA-2015

Lagoon (BANC-III

Velocity PSD



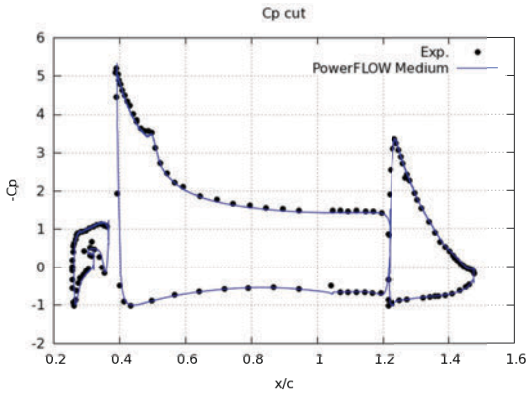

Farfield PSD

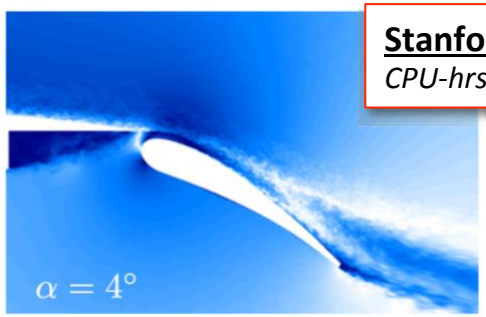




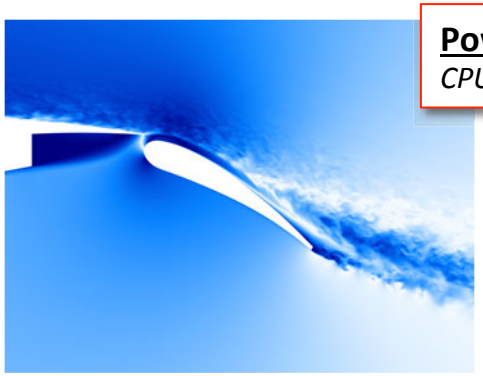
© Exa Corporation

# Efficient Parallel Implementation




**Stanford WMLES***
*CPU-hrs: 17,000,000***



**PowerFLOW*****
*CPU-hrs: 5,000***

* Bodart, Larson, Moin, "Large eddy simulation of high-lift devices", AIAA 2013-2724.

** CPUh normalized for 1 flow pass and a span of 1 chord

*** Simulations executed in collaboration with NASA


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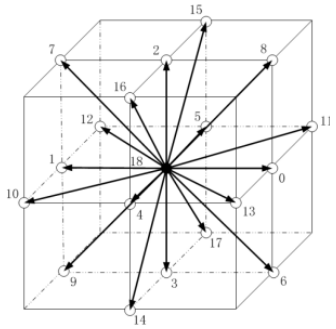
# Extension of LBM to Transonic/High speed Flows

- Rigorous Theory based on Hermite Expansions (Shan et al, 1998, 2006)
  - *Projection of LBM in Hermite Polynomials*
    - Expansion coefficients are the moments of distribution function
    - No assumption on small Ma# or constant Temperature
  - *Truncate the expansion to certain order*
  - *Represent solution in Velocity Space*

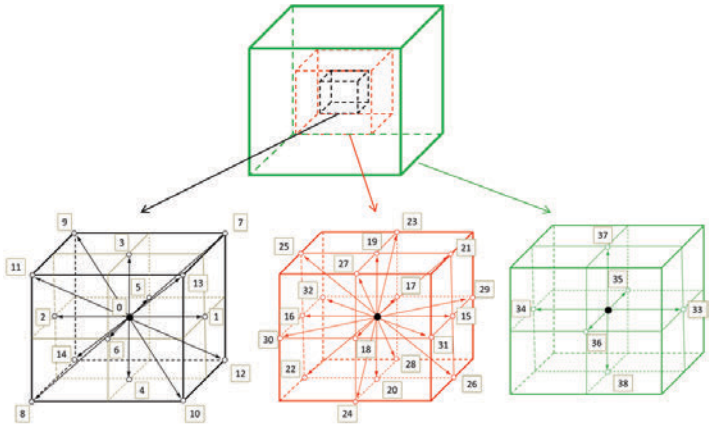

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# Extension of LBM to Transonic/High speed Flows

- High order multi-speed LBE models (D3Q27, D3Q39, D3Q125 …)



D3Q19 Model
$Ma_\infty$~0.4 ($Ma_{local}$~0.99)



Hybrid D3Q39 Model $Ma_{max}$~2.0

- Hybrid approach to couple with thermal dynamics field

$$\partial_t S + u_\alpha \partial_\alpha S = -\frac{1}{\rho\theta}\partial_\alpha q_\alpha + \frac{\Phi}{\rho\theta}. \qquad S = c_v ln\left(\frac{\theta}{\rho^{\gamma-1}}\right)$$

Nie, X.B., Shan, X., and Chen, H., "Lattice-Boltzmann/Finite-Difference Hybrid Simulation of Transonic Flow", AIAA-Paper 2009-139


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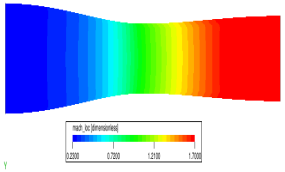
# Outline

- Motivation: CFD Applications in Aerospace
- Overview of PowerFLOW Projects at NASA
- Theory & Background
  - *LBM*
  - *Turbulence model*
  - *Wall treatment*
  - *Extension to transonic flows*
- Transonic Code Validation and Application Examples
  - *Fundamental Validations*
  - *Industrial Application Examples*

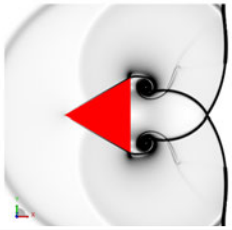

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# Transonic Code Validation & Application

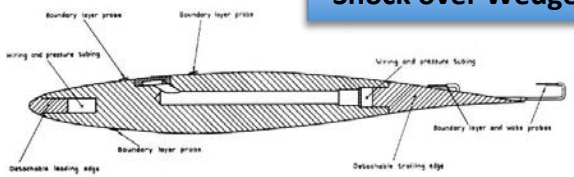
## Fundamental Validations



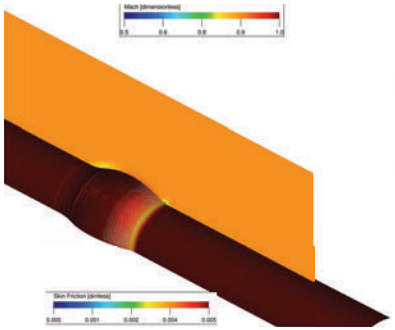
CDV nozzle

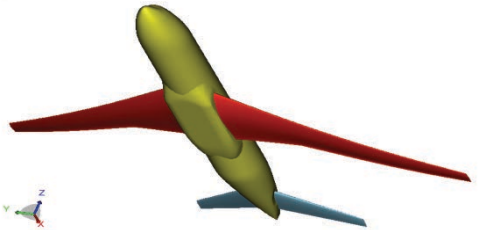


Shock over Wedge



RAE 2822 Airfoil

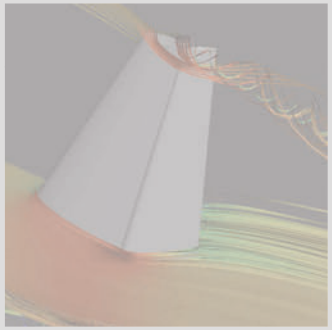




CRM

Transonic Bump

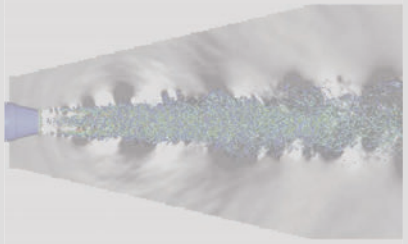
## Industrial Applications



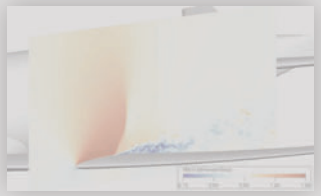
Fan Noise



Flow Control



Jet Noise



Buffet



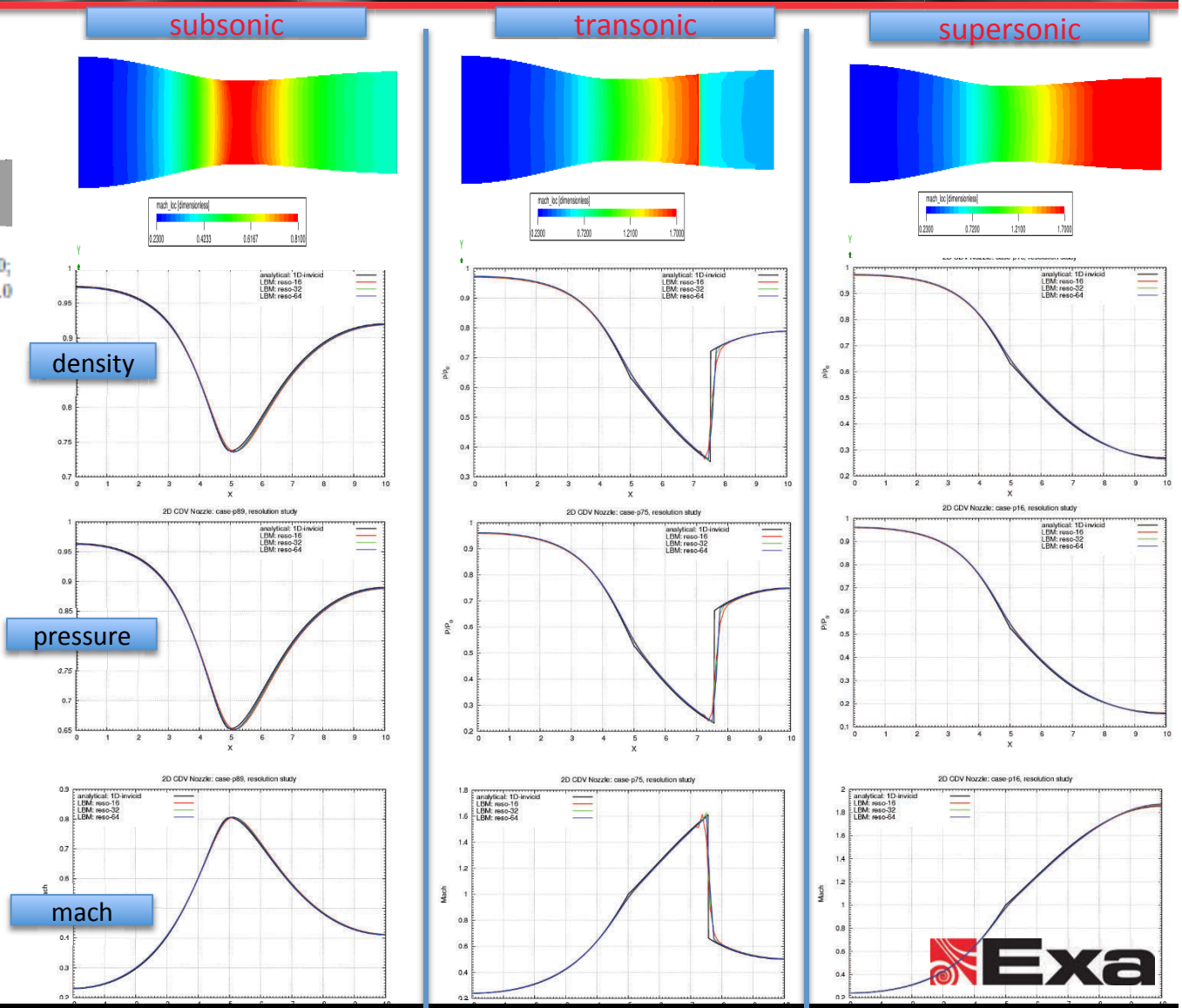
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# 2D CDV Nozzle (DNS): Sub-sonic/Transonic/Sueprsonic Flow Conditions



$$y(x) = \begin{cases} \pm[1.75 - 0.75\cos((0.2x - 1.0)\pi)], & \text{if } x \leq 0.0; \\ \pm[1.25 - 0.25\cos((0.2x - 1.0)\pi)], & \text{if } x > 0.0 \end{cases}$$

- Converge-Diverge Nozzle configuration
- Compared with analytical 1D invicid flow solution
- Simulated at low viscosity at various flow conditions



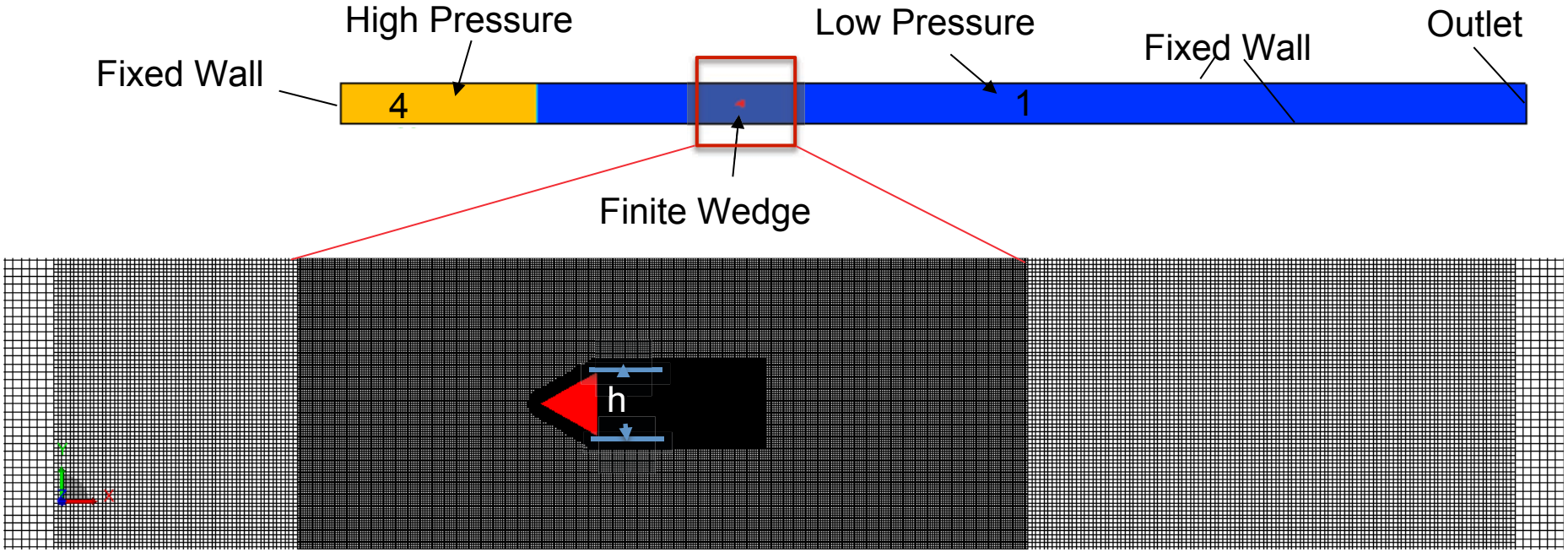


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# Collision of a Planar Shock with a Finite Wedge Setup

**Shock Tube Setup**

S-M. Chang and K-S. Chang: On the shock-vortex interaction in Schardin's problem, Shock Waves, 10:333-343, 2000




**Initial Conditions**:

P4/P1 = 4.0, T4/T1 = 1

**Boundary Conditions**:

No-slip walls
Outlet pressure P1
Re 50000

**Grid Resolutions**:

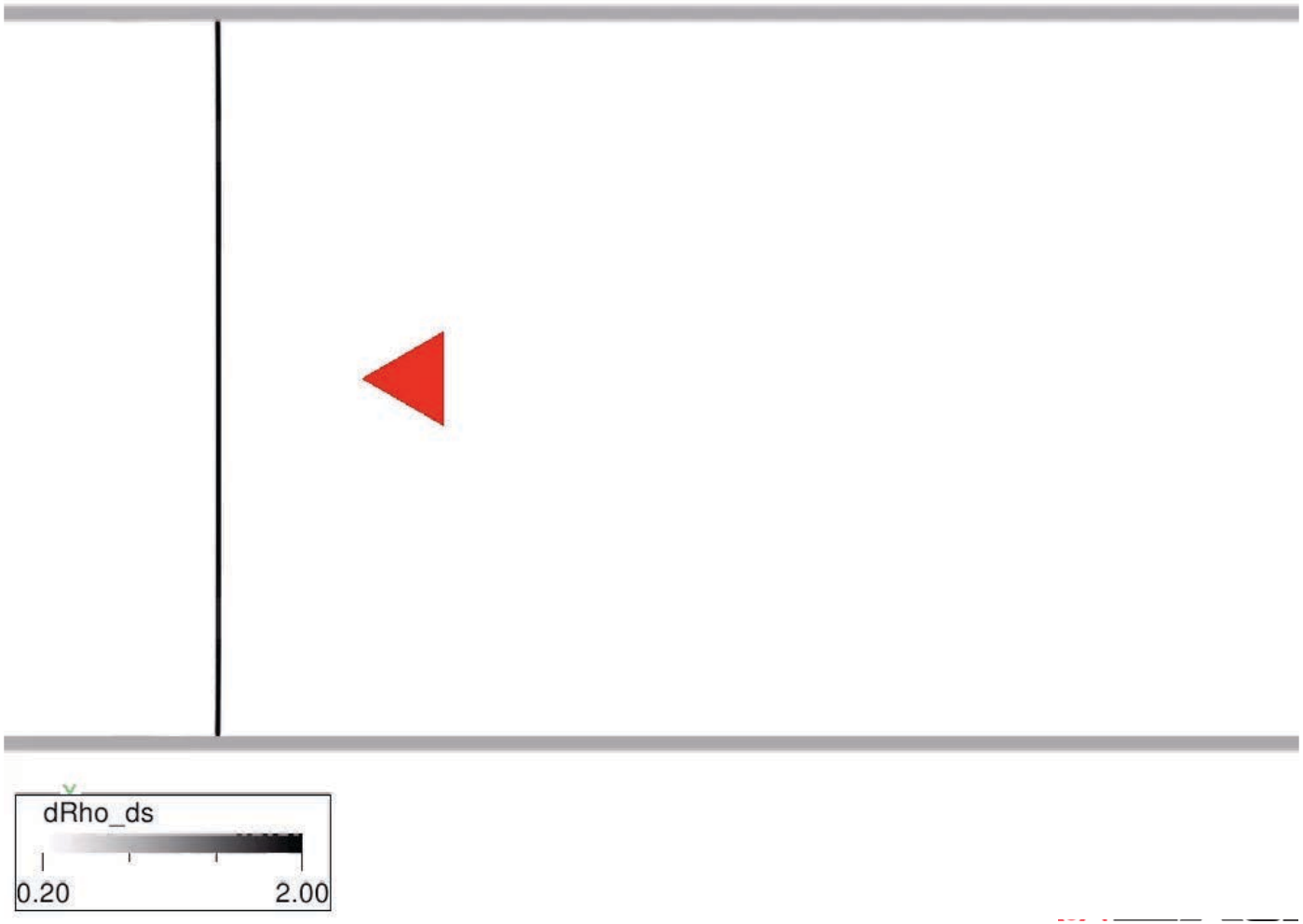
| | |
|---|---|
| Coarse | h/128 |
| Medium | h/256 |
| Fine | h/512 |


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# Collision of a Planar Shock with a Finite Wedge

Animation of the plane shock moving over the finite wedge (Animation time 0.001 s)

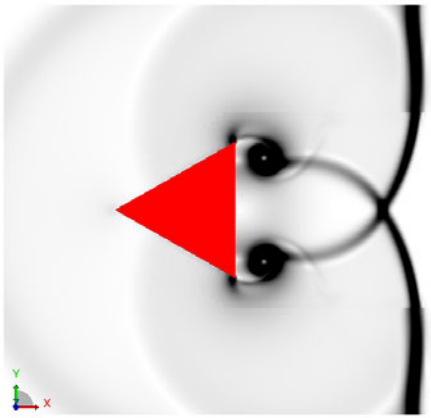
Planar shock moves at Mach 1.34



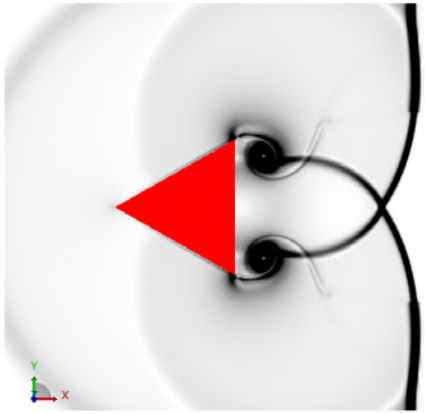


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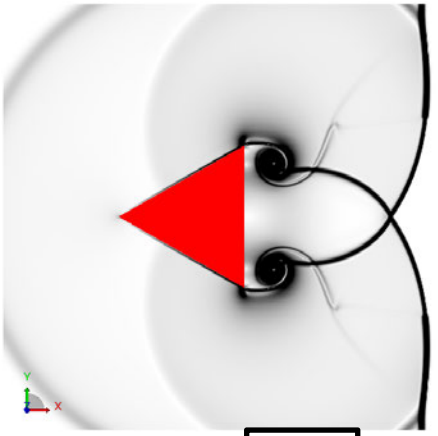
# Collision of a Planar Shock with a Finite Wedge



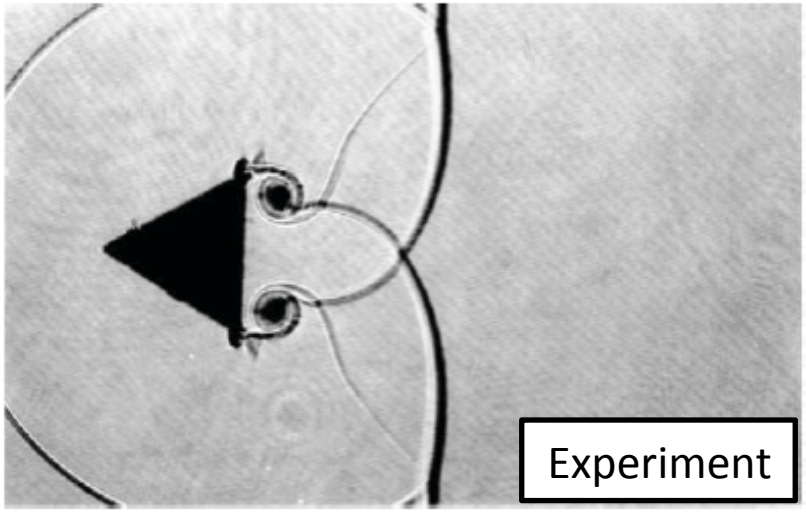
coarse



medium



fine



Experiment

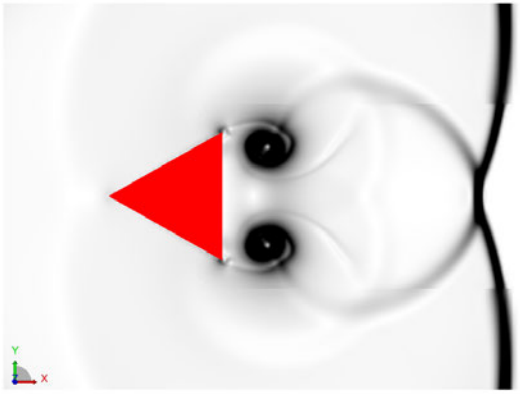
t = 91 μ sec

t = 0 corresponds to the instant, when the planar shock first collides with the finte wedge

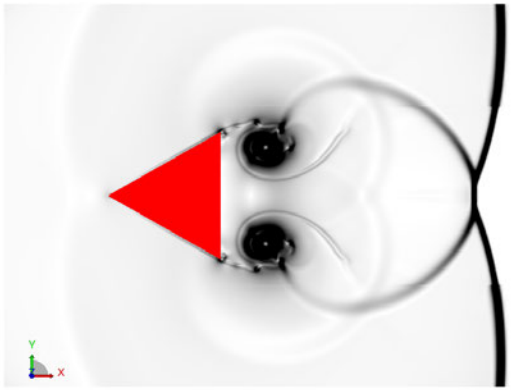


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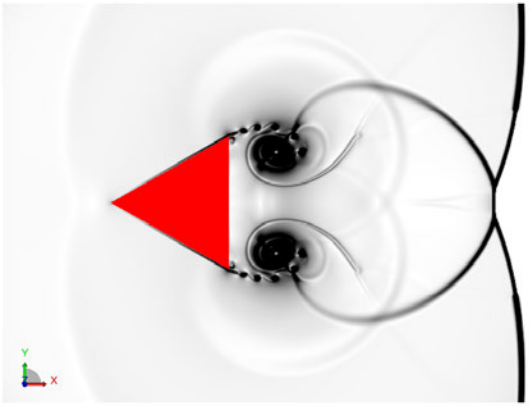
# Collision of a Planar Shock with a Finite Wedge



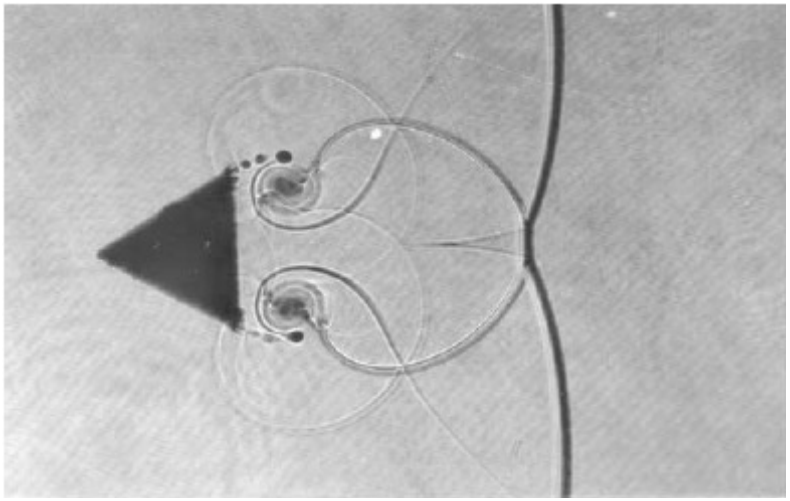
coarse



medium



fine



Experiment

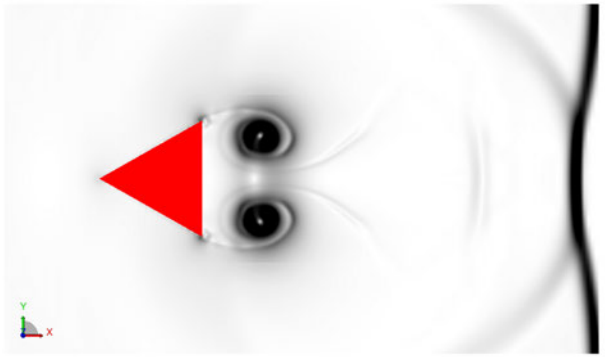
t = 128 μ sec

t = 0 corresponds to the instant, when the planar shock first collides with the finte wedge

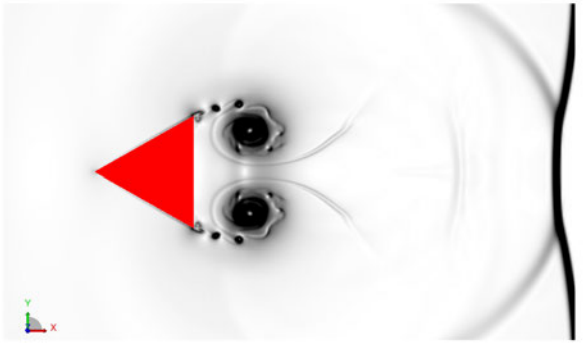


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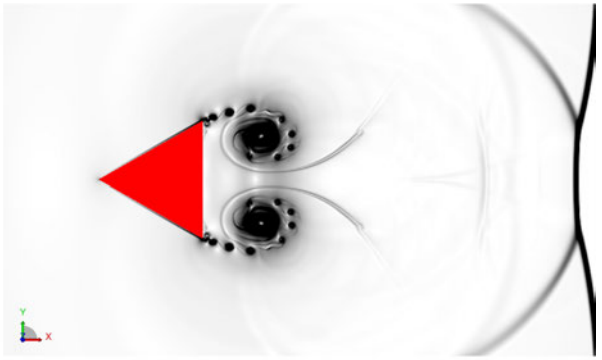
# Collision of a Planar Shock with a Finite Wedge



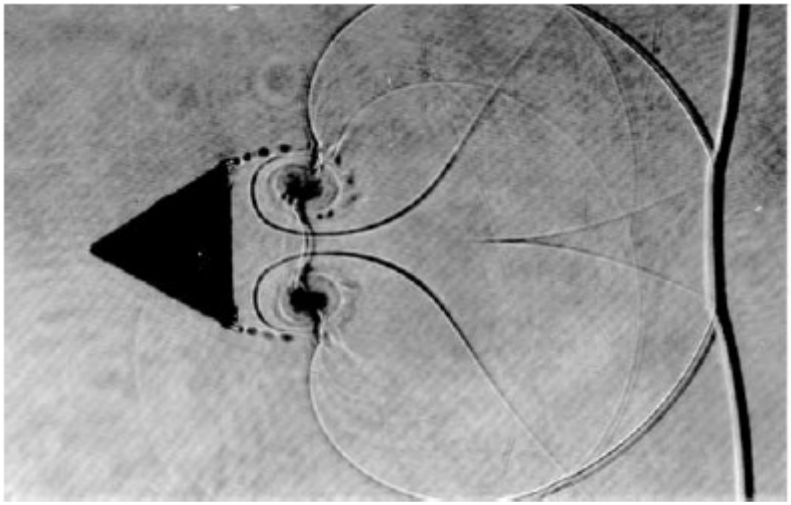
coarse



medium



fine



Experiment

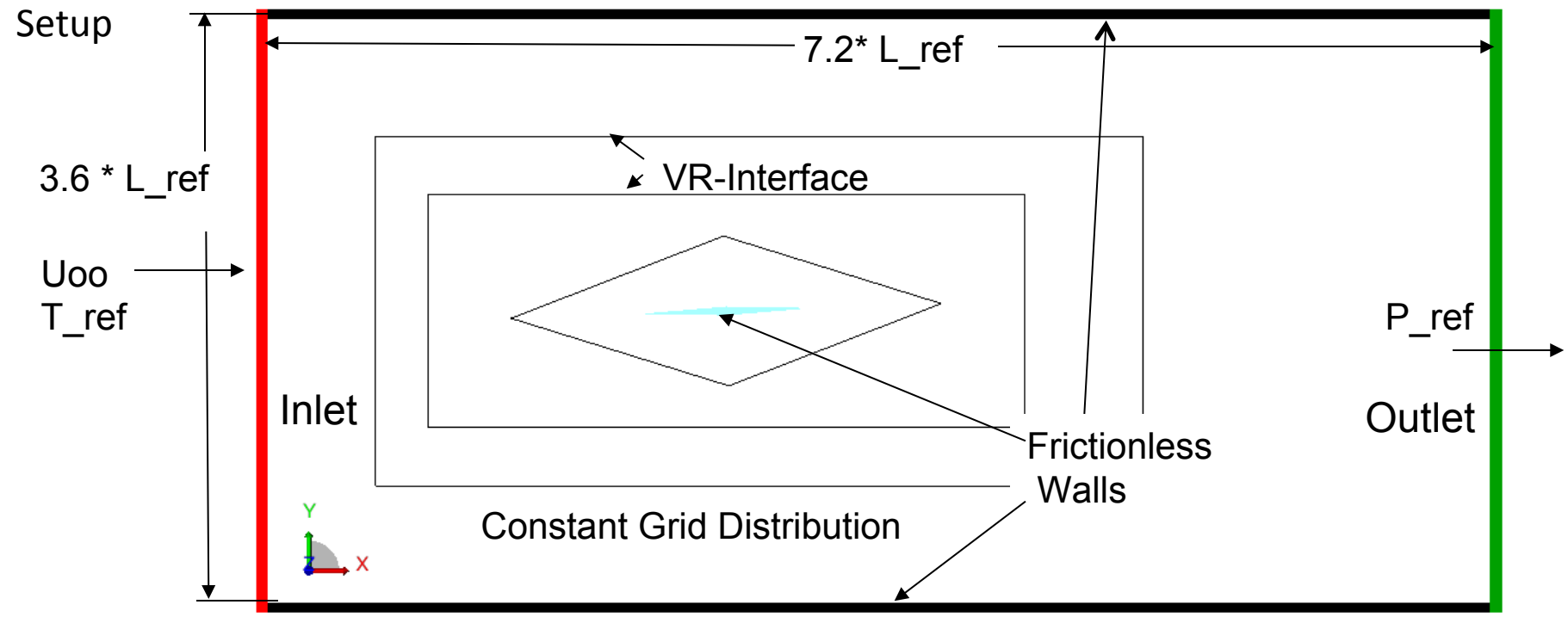
t = 151 μ sec

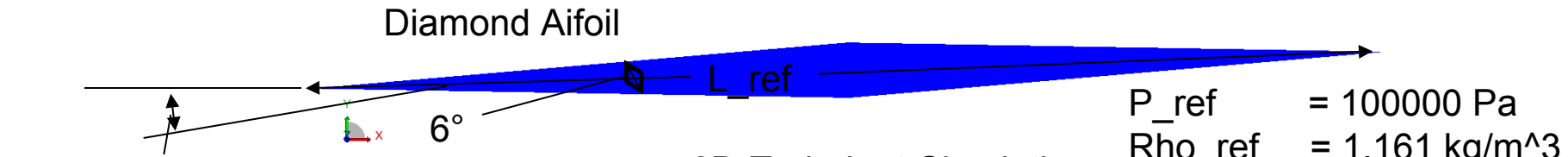
t = 0 corresponds to the instant, when the planar shock first collides with the finte wedge



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# Supersonic Diamond Airfoil



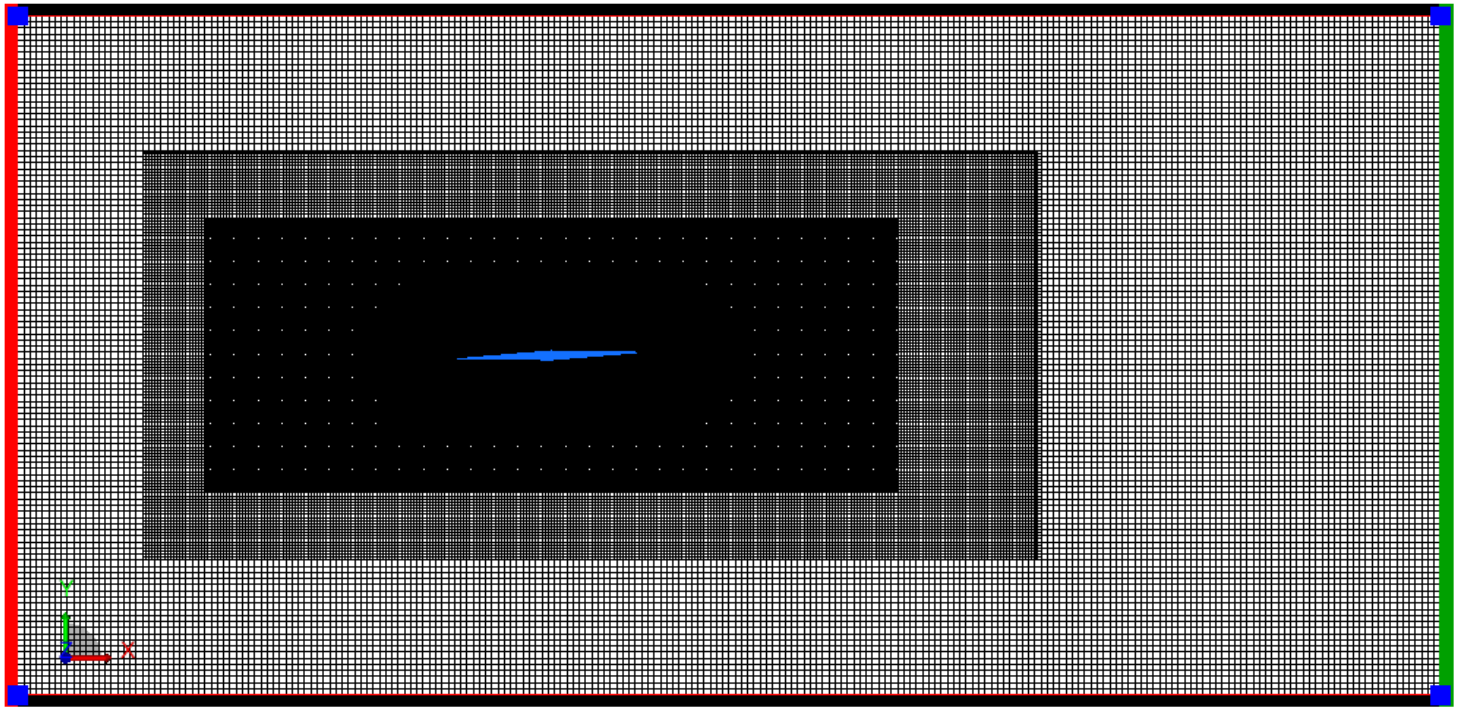

L_ref = 1 m
Area_ref = 1 m^2

2D-Turbulent-Simulation
Moo = 1.4
Re = 3.24E+07

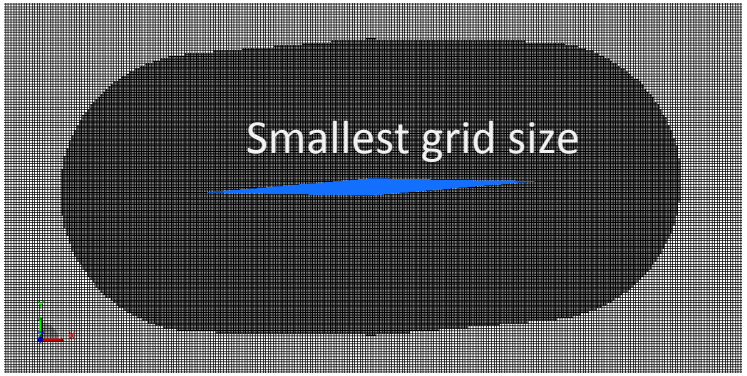
P_ref = 100000 Pa
Rho_ref = 1.161 kg/m^3
T_ref = 300° K
AOA = -2°


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# Supersonic Diamond Airfoil



Grid
Resolution 512 per chord (coarse)
Voxel-Size 1000/512 = 1.95 mm
Total Voxels 1.46 Mill.
Fine Equivalent Voxels 1.01 Mill.

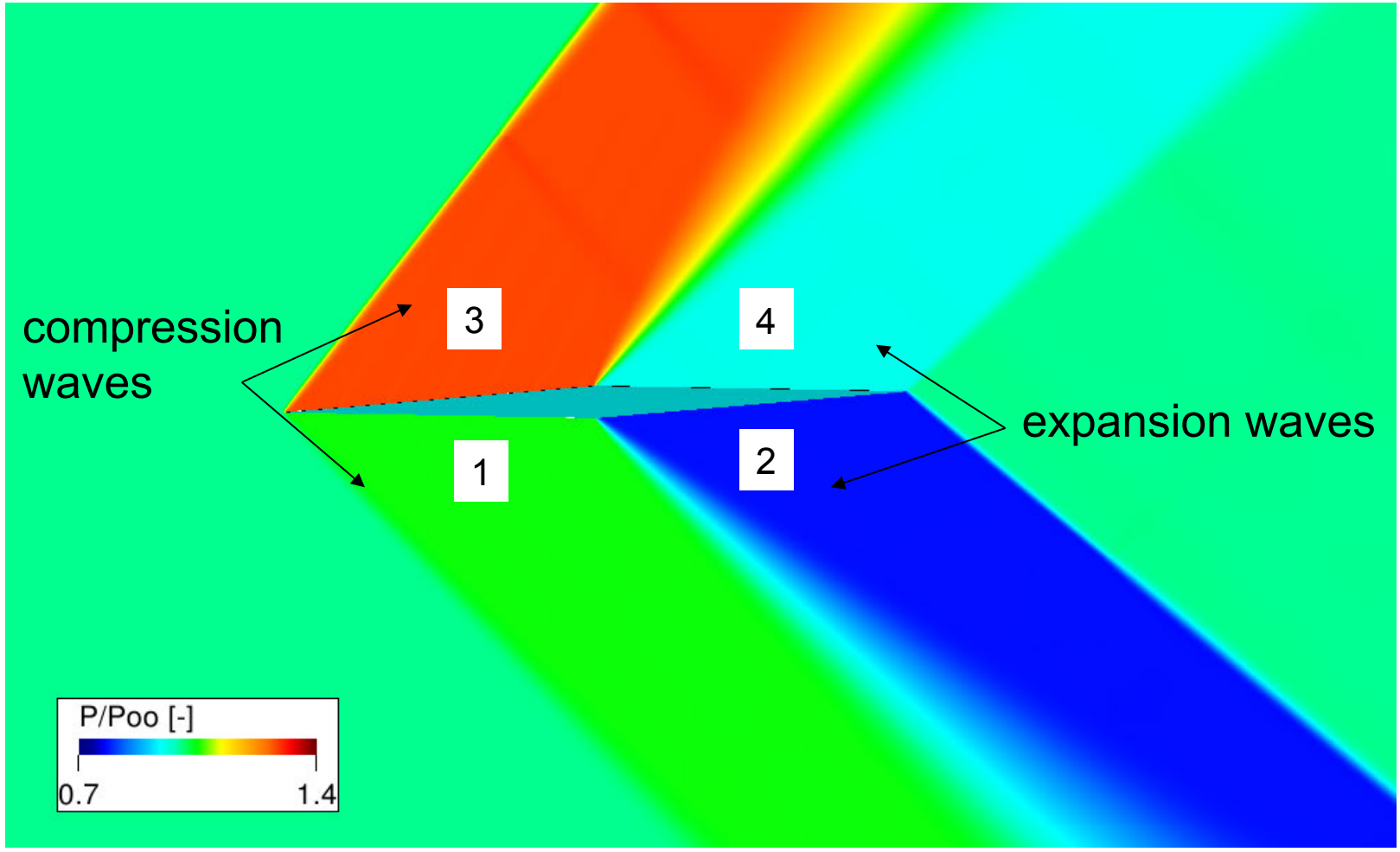




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# Supersonic Diamond Airfoil

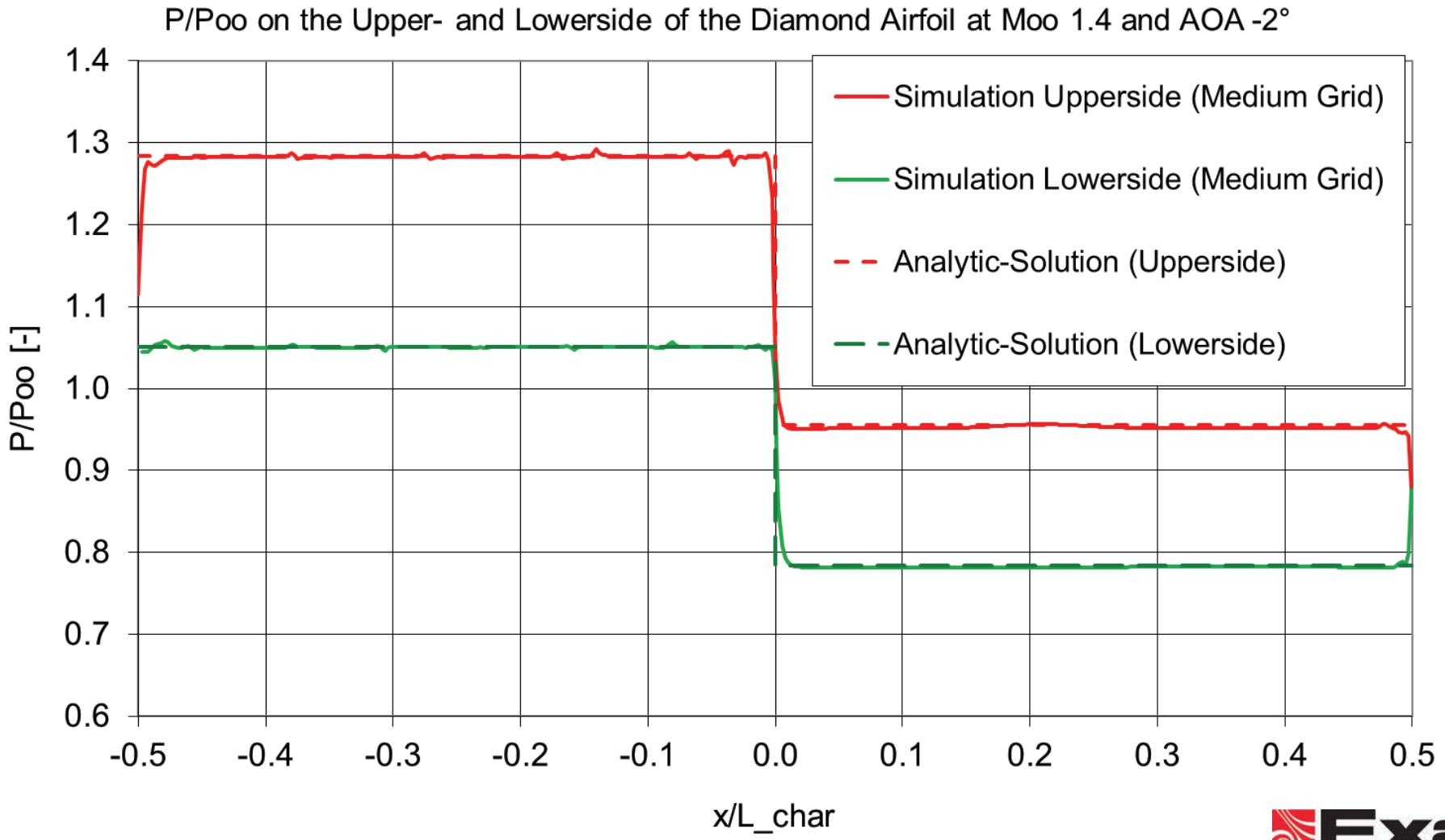
Pressure Distribution for Moo 1.4 and AOA -2





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# Supersonic Diamond Airfoil



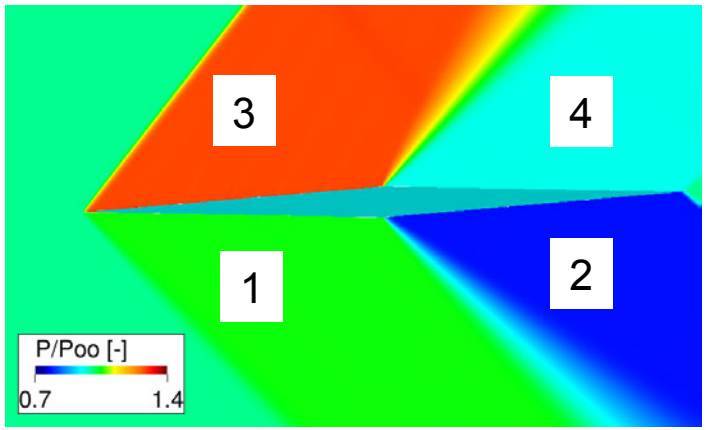


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# Supersonic Diamond Airfoil

| Angle of Attack AOA ° | -2.0 | | | |
|---|---|---|---|---|
| Inflow Mach Number Moo | 1.4 | | | |
| | Turbulent-Simulation | | | Analytic-Solution |
| Grid | Coarse | Medium | Fine | |
| Lift Cl [-] | 0.1471 | 0.1474 | 0.1463 | 0.1473 |
| Drag Cd [-] | 0.0165 | 0.0165 | 0.0165 | 0.0165 |
| Pressure Relation P1/Poo[-] | 1.0502 | 1.0501 | 1.0502 | 1.0502 |
| Pressure Relation P2/Poo[-] | 0.7821 | 0.7819 | 0.7820 | 0.7838 |
| Pressure Relation P3/Poo[-] | 1.2823 | 1.2820 | 1.2821 | 1.2841 |
| Pressure Relation P4/Poo[-] | 0.9551 | 0.9555 | 0.9530 | 0.9553 |
| Mach Number M1 [-] | 1.3617 | 1.3637 | 1.3661 | 1.3650 |
| Mach Number M2 [-] | 1.5616 | 1.5625 | 1.5652 | 1.5690 |
| Mach Number M3[-] | 1.2109 | 1.2165 | 1.2215 | 1.2152 |
| Mach Number M4 [-] | 1.4241 | 1.4260 | 1.4267 | 1.4310 |

Resolution coarse = 512 per chord
Resolution medium = 768 per chord
Resolution fine = 1024 per chord

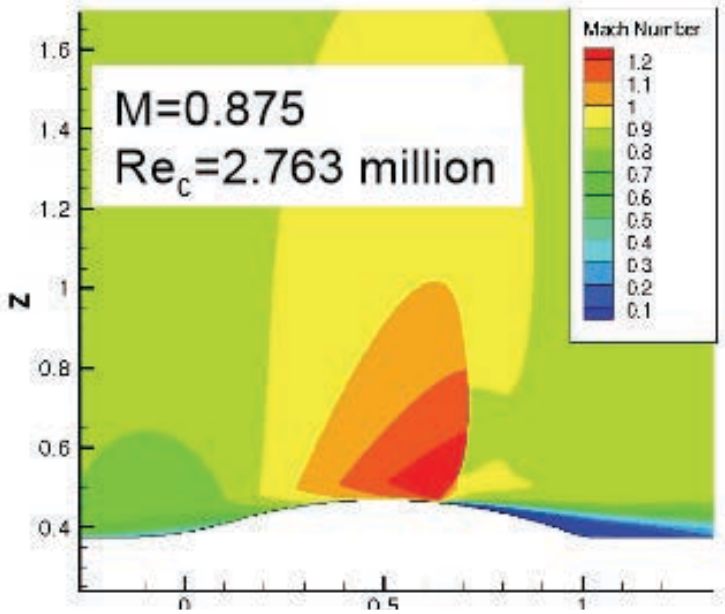


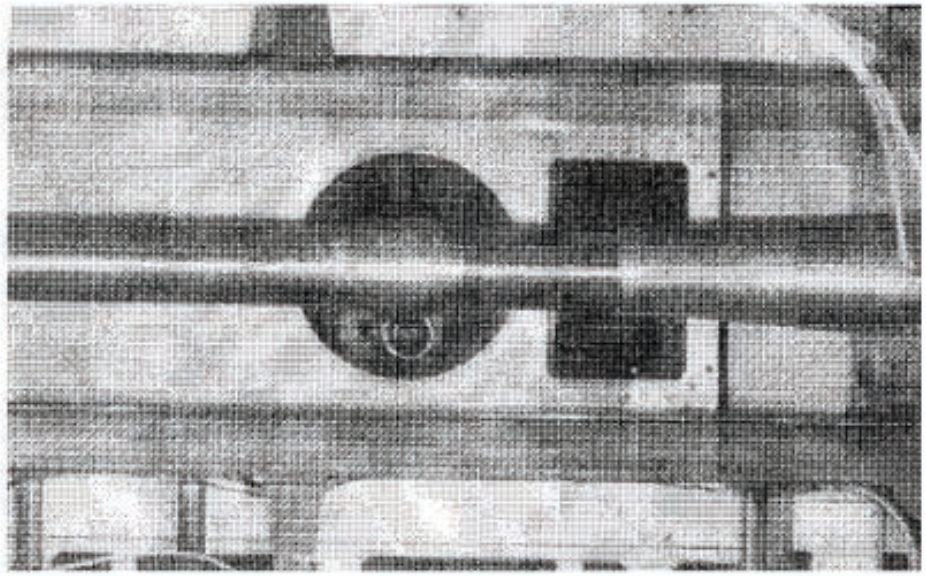


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# Axisymmetric Transonic Bump

- Part of NASA's 40% challenge
- Includes shock-induced separation, widely-used dataset for many years, axi-symmetry removes 2D questions
- RANS typically overestimates separation bubble by 20-30%



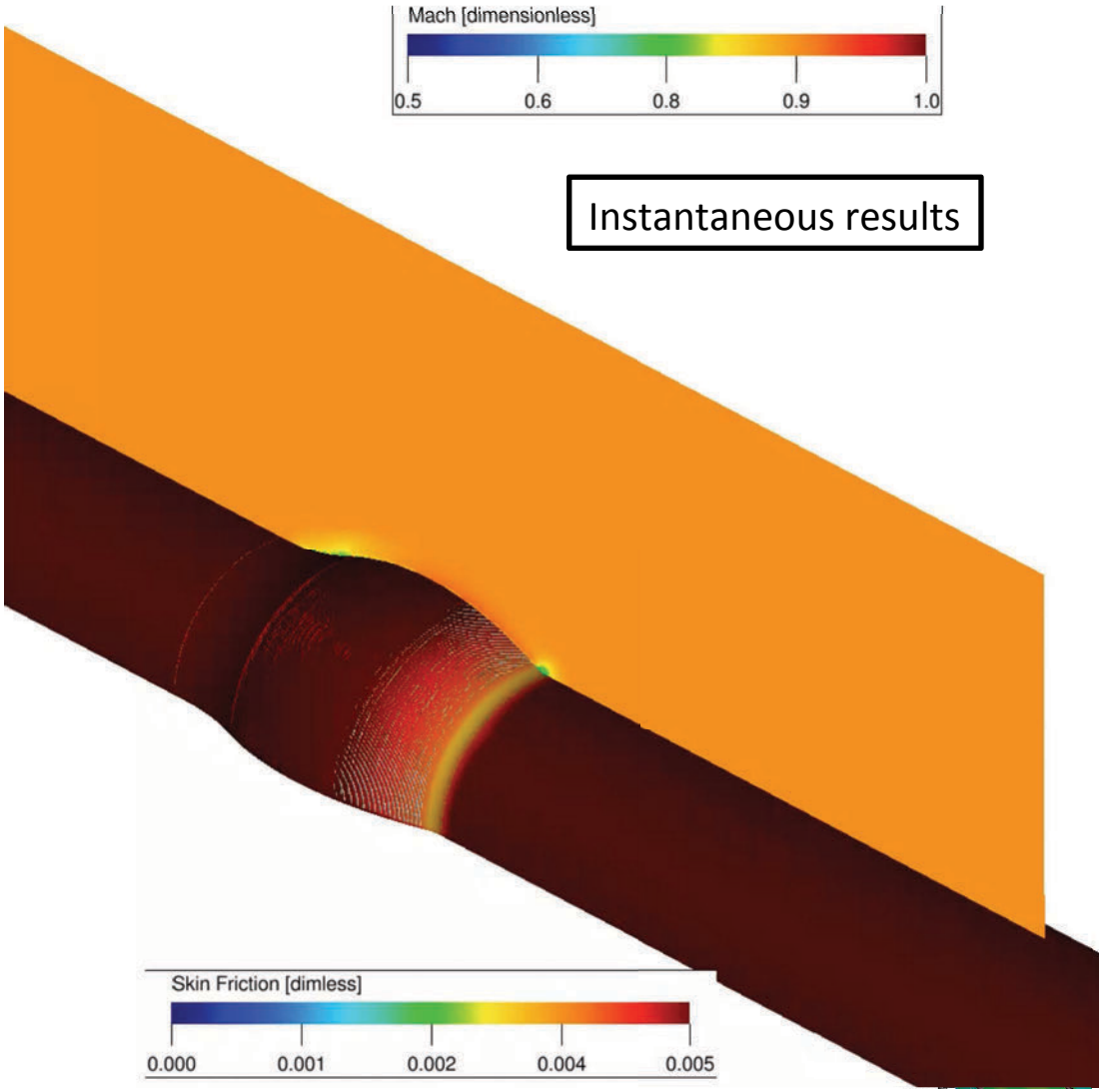



Bachalo, W. D., Johnson, D. A., "Transonic, Turbulent Boundary-Layer Separation Generated on an Axisymmetric Flow Model," AIAA Journal, vol. 24, no. 3, pp. 437-443, 1986.


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# Axisymmetric Transonic Bump

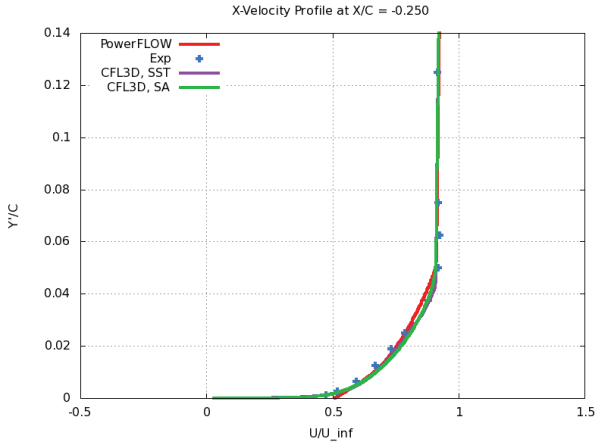
- Volume cut shows location and sharpness of shock
- Skin friction contours indicate flow separation
- Iso-surfaces of $\lambda_2$ highlight resolved turbulent fluctuations in wake

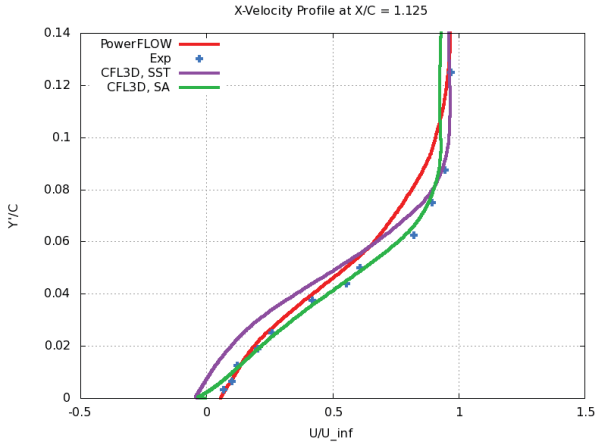


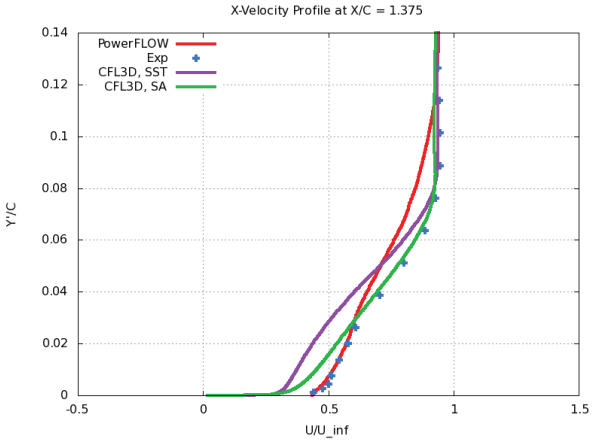


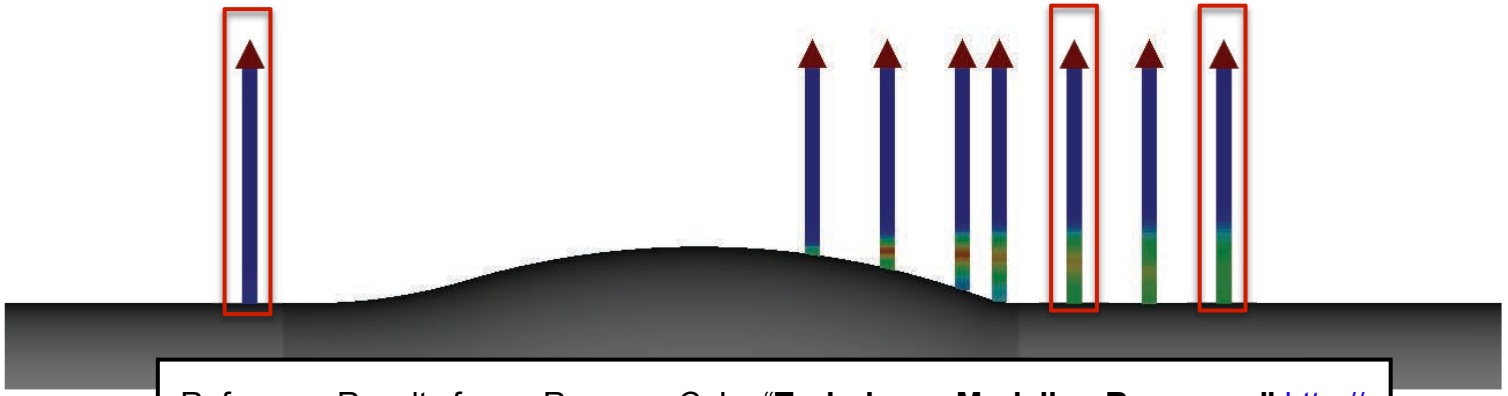
© Exa Corporation

# Axisymmetric Transonic Bump X-Velocity Profiles



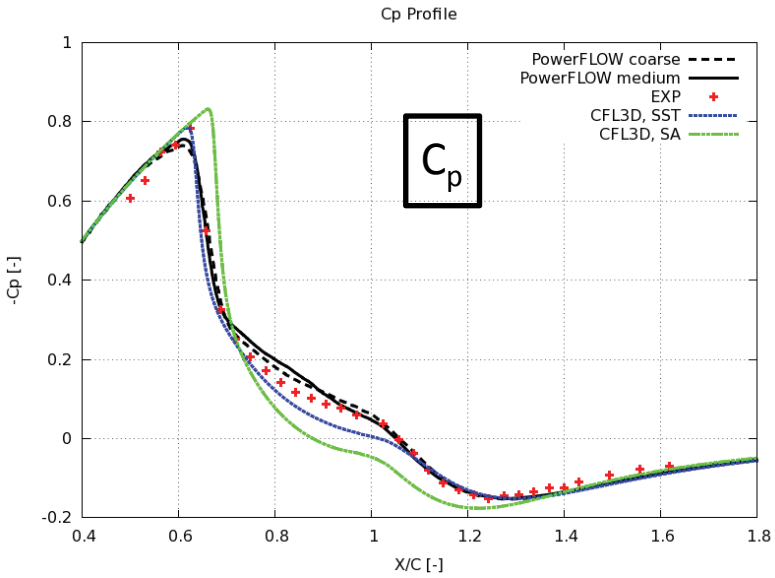



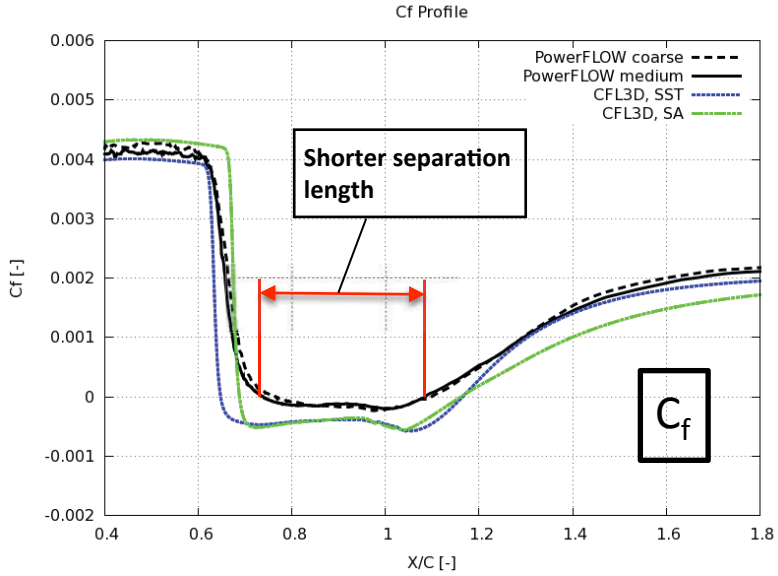



Reference Results from : Rumsey, C. L., "**Turbulence Modeling Resource,**" http://turbmodels.larc.nasa.gov


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# Axisymmetric Transonic Bump Pressure and Skin Friction Distribution

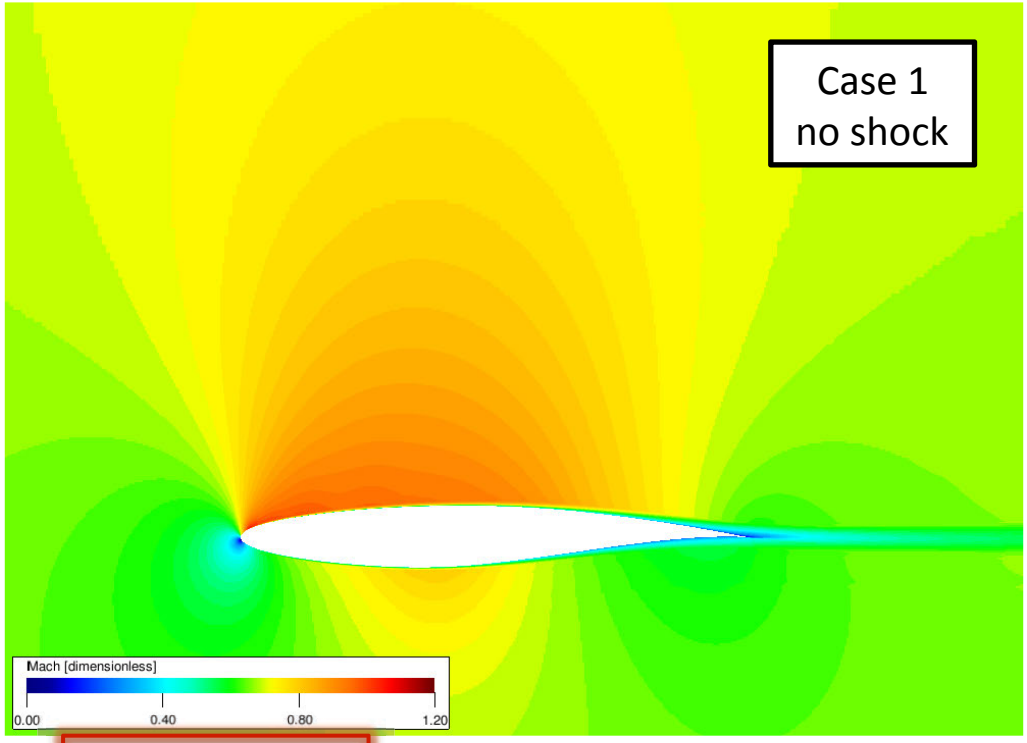



- Unsteady flow in separation after shock captured
- Improved prediction of separation length and skin friction compared to standard RANS


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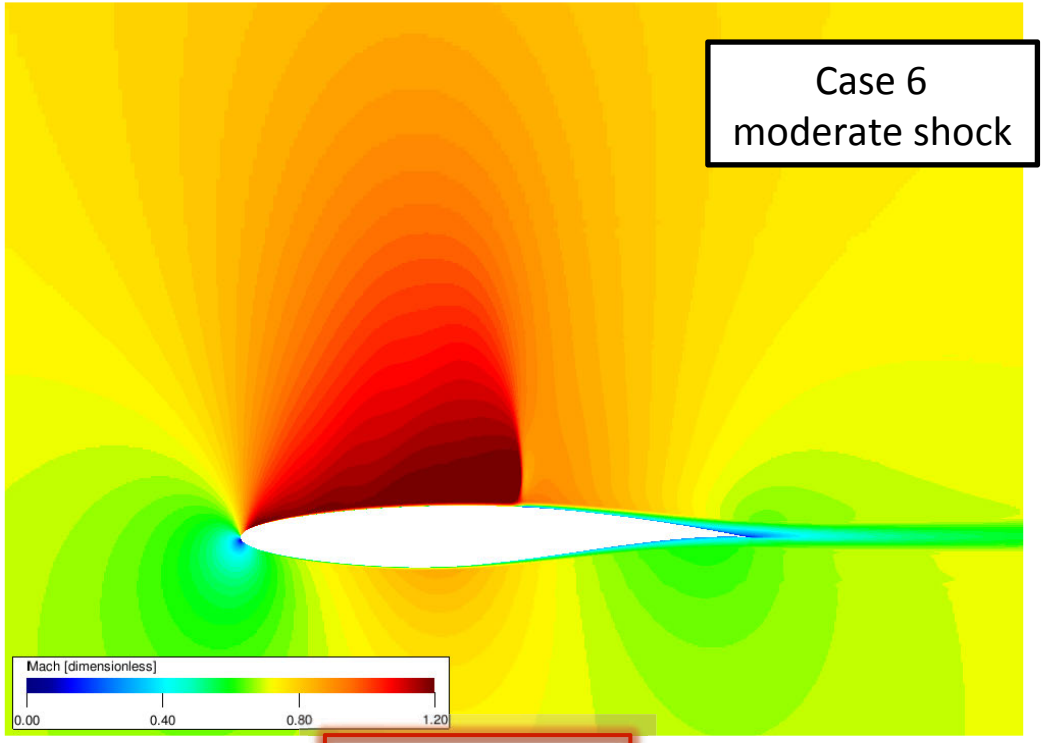
# Transonic Flow over the RAE 2822 airfoil




| | Case 1 | Case 6 | Case 9 | Case 10 |
|---|---|---|---|---|
| Ma [-] | 0.676 | 0.729 | 0.73 | 0.75 |
| AoA [°] | 1.8148 | 2.4508 | 2.6873 | 2.7147 |
| Re [$10^6$] | 5.7 | 6.5 | 6.5 | 6.2 |


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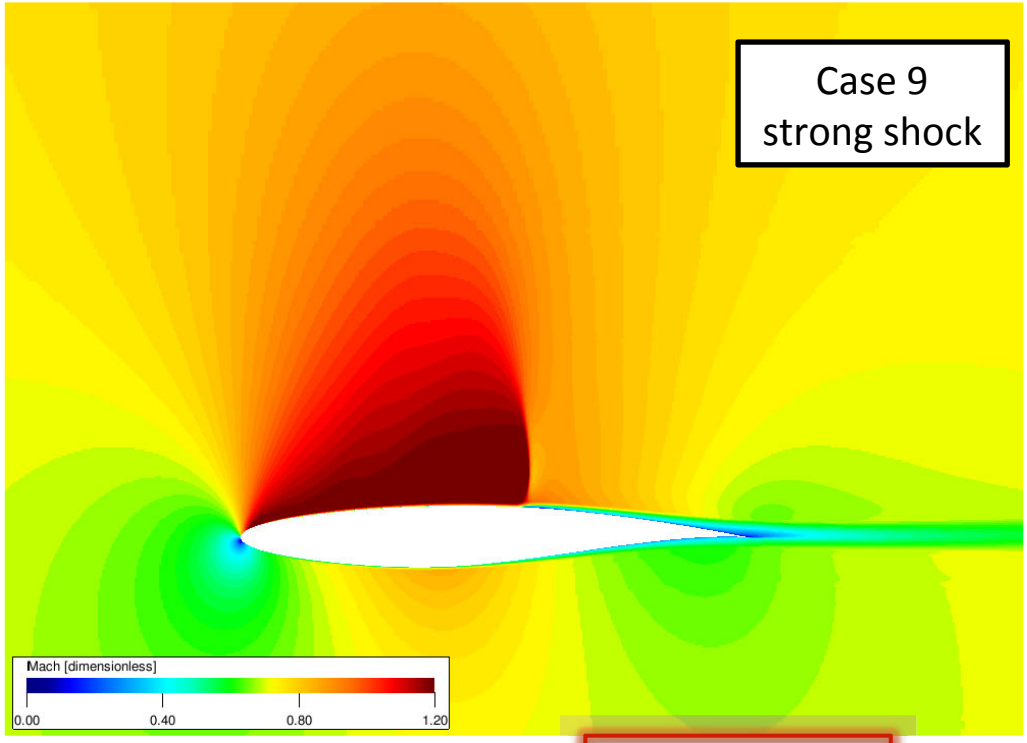
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|---|---|---|---|---|
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| Re [$10^6$] | 5.7 | 6.5 | 6.5 | 6.2 |


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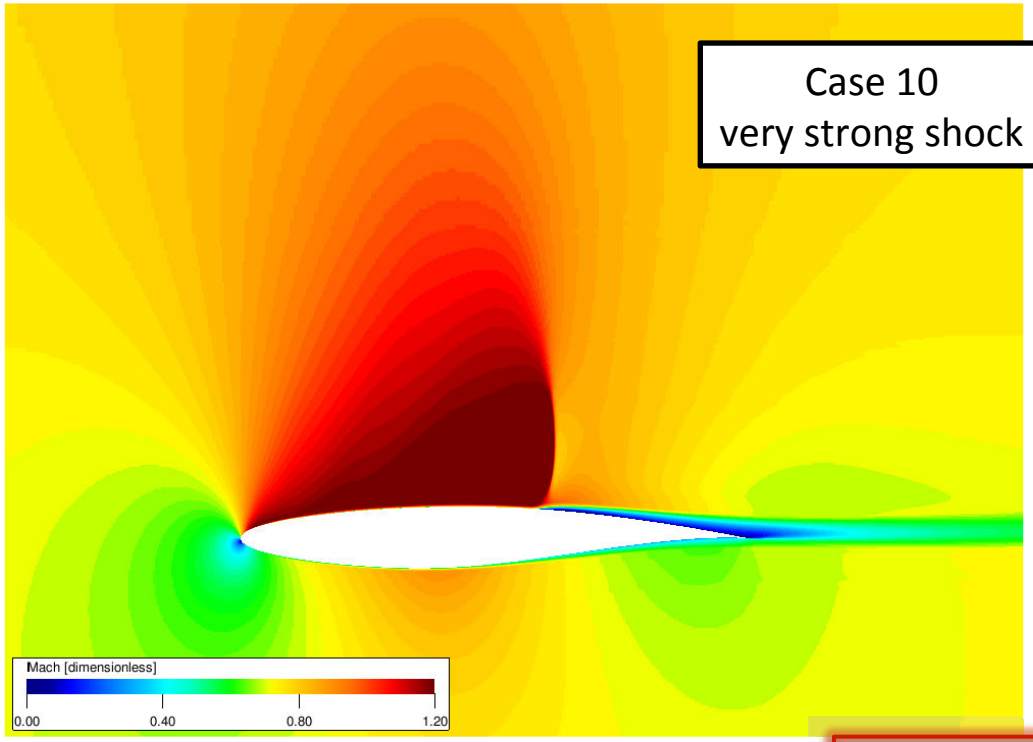
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|---|---|---|---|---|
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# Transonic Flow over the RAE 2822 airfoil

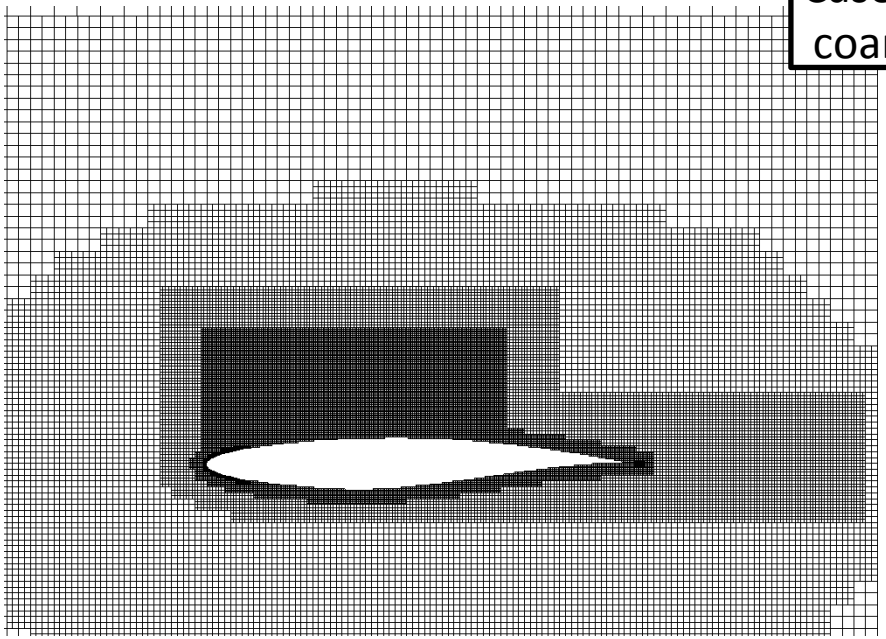


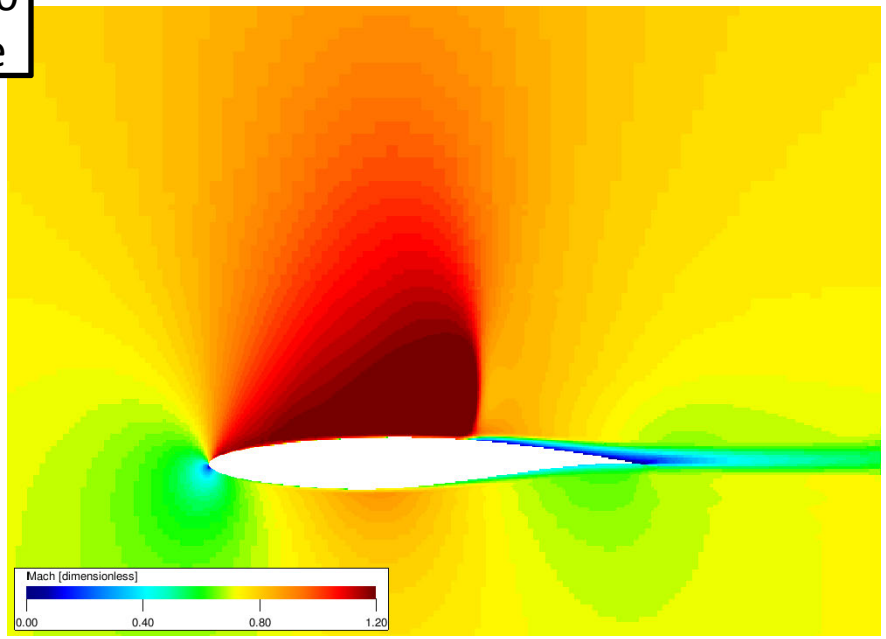

| | Case 1 | Case 6 | Case 9 | Case 10 |
|---|---|---|---|---|
| Ma [-] | 0.676 | 0.729 | 0.73 | 0.75 |
| AoA [°] | 1.8148 | 2.4508 | 2.6873 | 2.7147 |
| Re [$10^6$] | 5.7 | 6.5 | 6.5 | 6.2 |


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# Transonic Flow over the RAE 2822 airfoil

Case 10
coarse

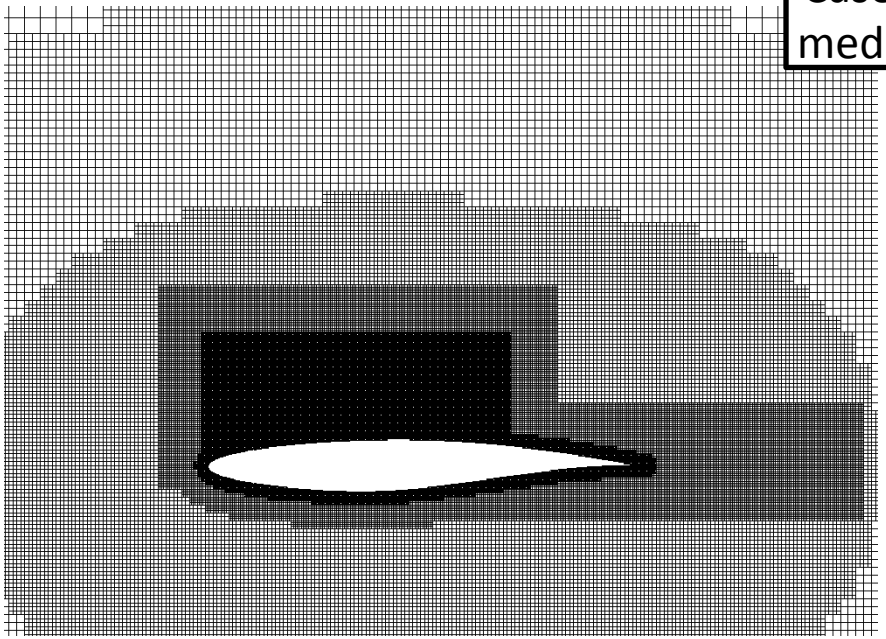


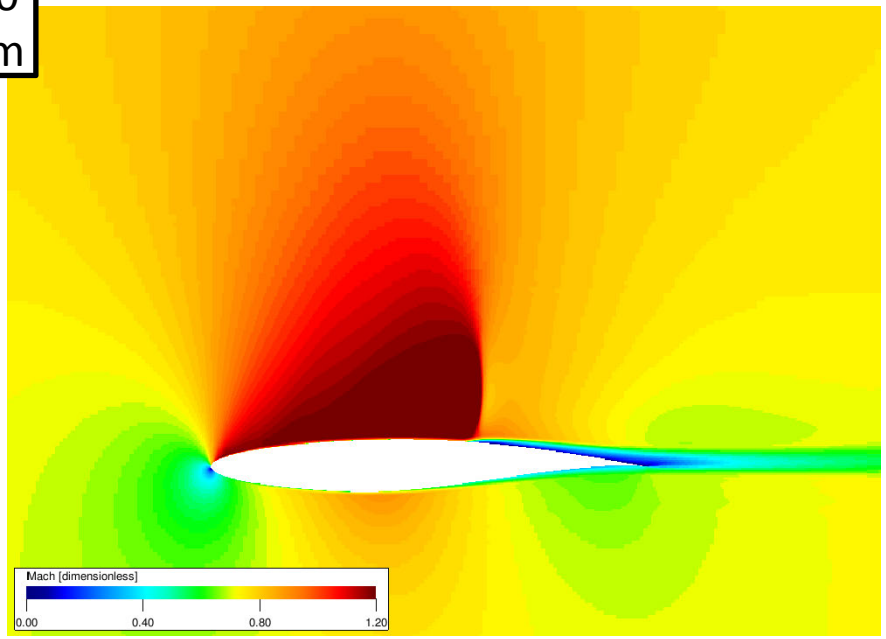



| | coarse | Medium | Fine | X-fine | XX-fine |
|---|---|---|---|---|---|
| Resolution (cells / chord) | 592 | 888 | 1333 | 2000 | 3000 |
| Voxels [$10^3$] | 63 | 138 | 300 | 667 | 1500 |
| CPUh | 30 | 65 | 160 | 480 | 1880 |
| Wallclock on 32 cores [h] | 1 | 2 | 5 | 15 | 36 |

# Transonic Flow over the RAE 2822 airfoil

Case 10
medium

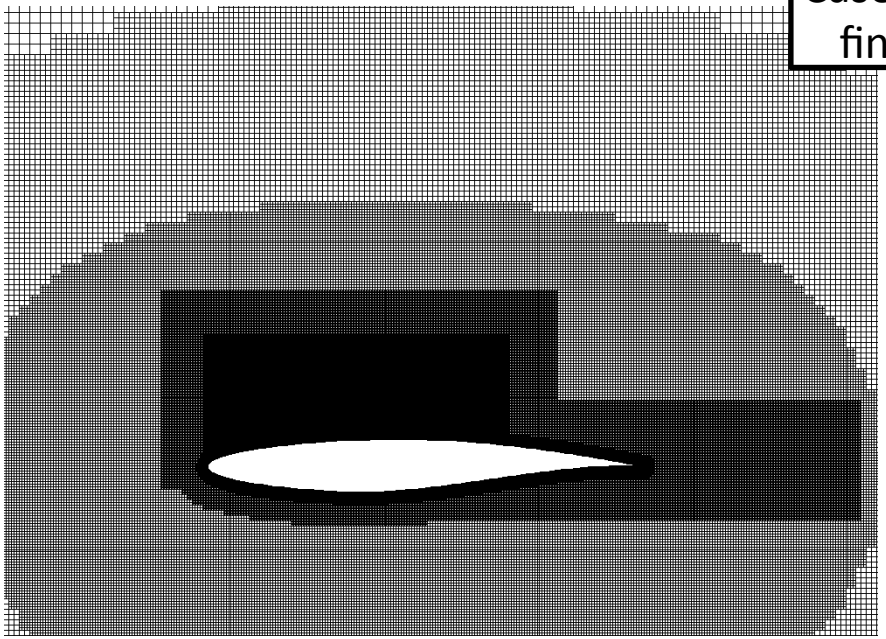


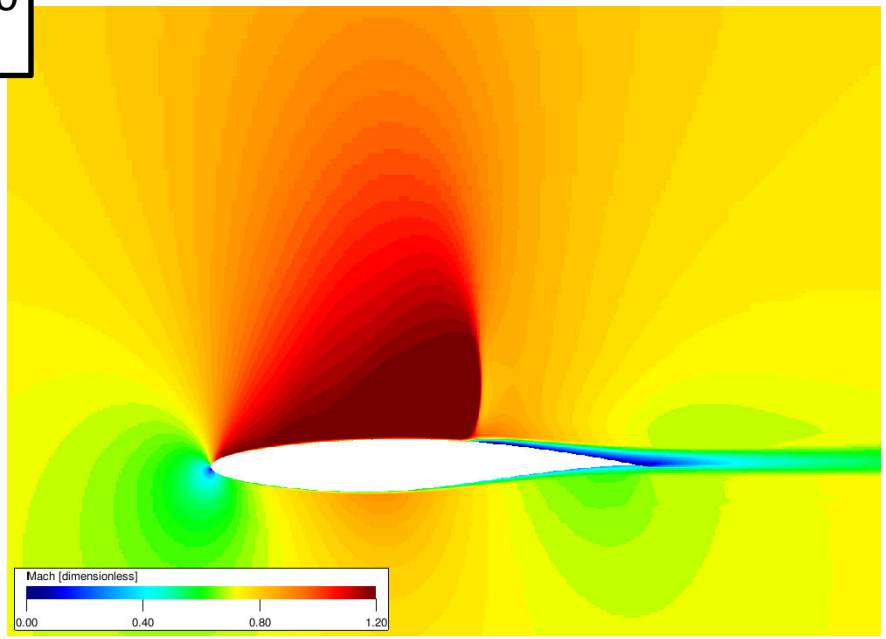



| | coarse | Medium | Fine | X-fine | XX-fine |
|---|---|---|---|---|---|
| Resolution (cells / chord) | 592 | 888 | 1333 | 2000 | 3000 |
| Voxels [$10^3$] | 63 | 138 | 300 | 667 | 1500 |
| CPUh | 30 | 65 | 160 | 480 | 1880 |
| Wallclock on 32 cores [h] | 1 | 2 | 5 | 15 | 36 |

# Transonic Flow over the RAE 2822 airfoil

Case 10 fine

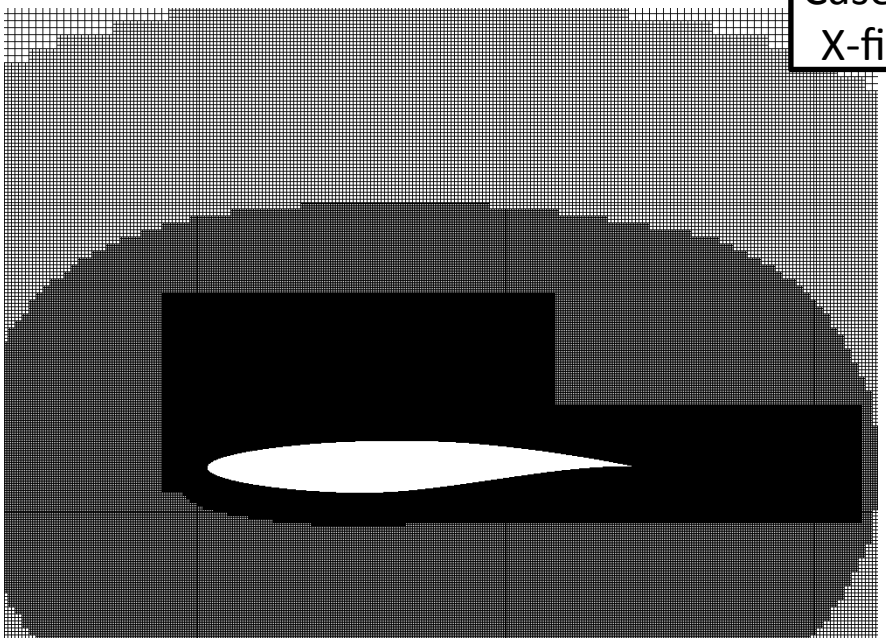


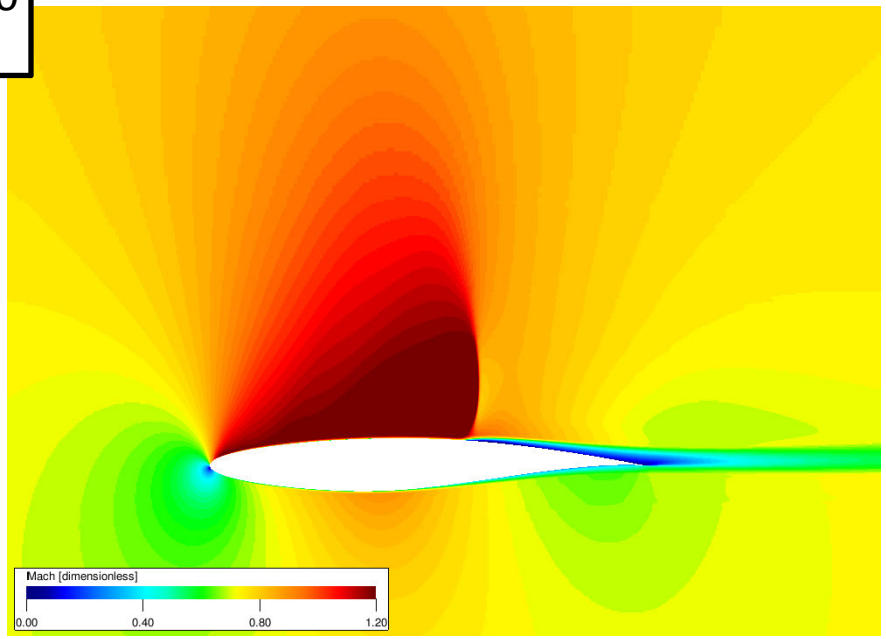



| | coarse | Medium | Fine | X-fine | XX-fine |
|---|---|---|---|---|---|
| Resolution (cells / chord) | 592 | 888 | 1333 | 2000 | 3000 |
| Voxels [$10^3$] | 63 | 138 | 300 | 667 | 1500 |
| CPUh | 30 | 65 | 160 | 480 | 1880 |
| Wallclock on 32 cores [h] | 1 | 2 | 5 | 15 | 36 |

# Transonic Flow over the RAE 2822 airfoil

Case 10
X-fine

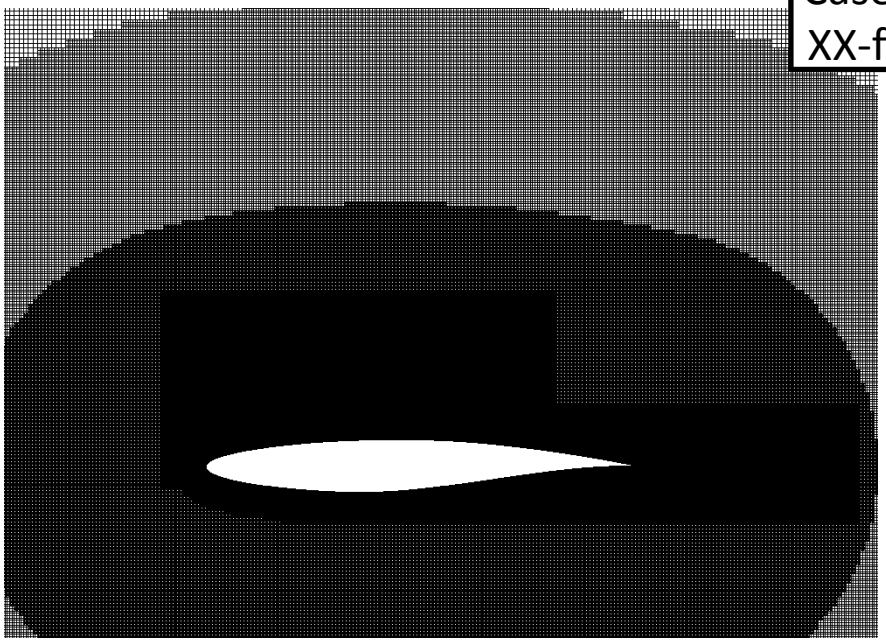


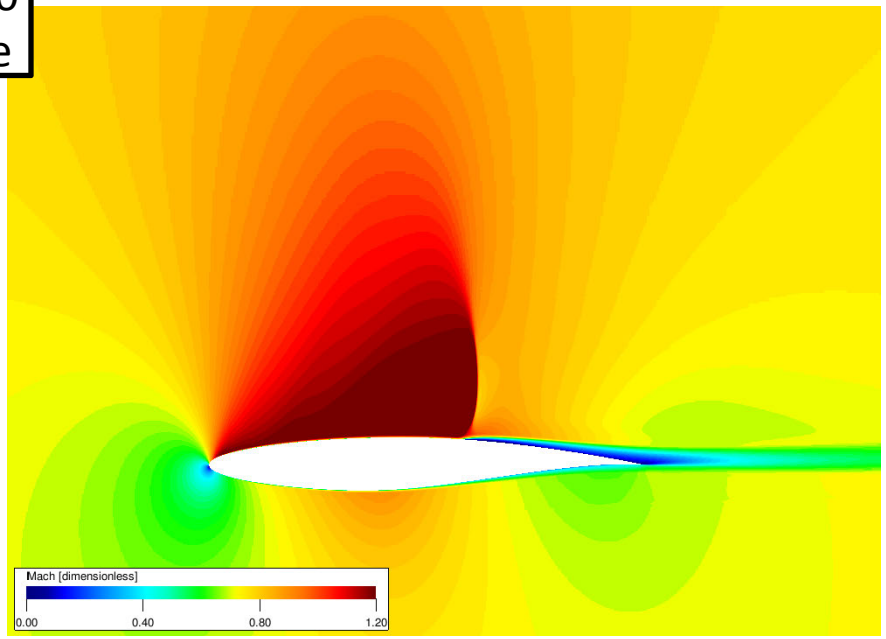



| | coarse | Medium | Fine | X-fine | XX-fine |
|---|---|---|---|---|---|
| Resolution (cells / chord) | 592 | 888 | 1333 | 2000 | 3000 |
| Voxels [$10^3$] | 63 | 138 | 300 | 667 | 1500 |
| CPUh | 30 | 65 | 160 | 480 | 1880 |
| Wallclock on 32 cores [h] | 1 | 2 | 5 | 15 | 36 |

# Transonic Flow over the RAE 2822 airfoil

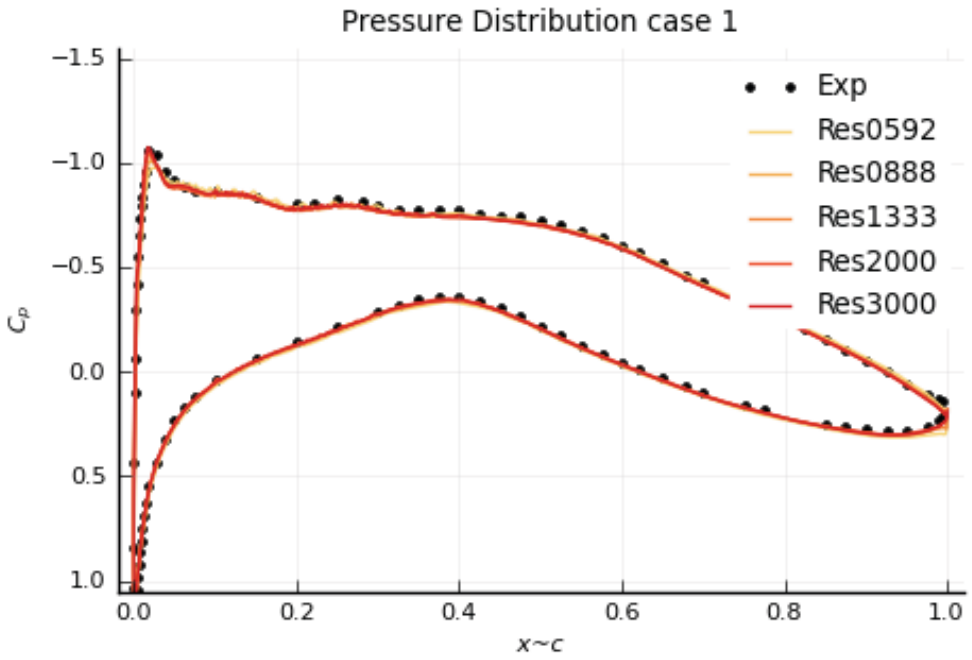
Case 10
XX-fine






| | coarse | Medium | Fine | X-fine | XX-fine |
|---|---|---|---|---|---|
| Resolution (cells / chord) | 592 | 888 | 1333 | 2000 | 3000 |
| Voxels [$10^3$] | 63 | 138 | 300 | 667 | 1500 |
| CPUh | 30 | 65 | 160 | 480 | 1880 |
| Wallclock on 32 cores [h] | 1 | 2 | 5 | 15 | 36 |

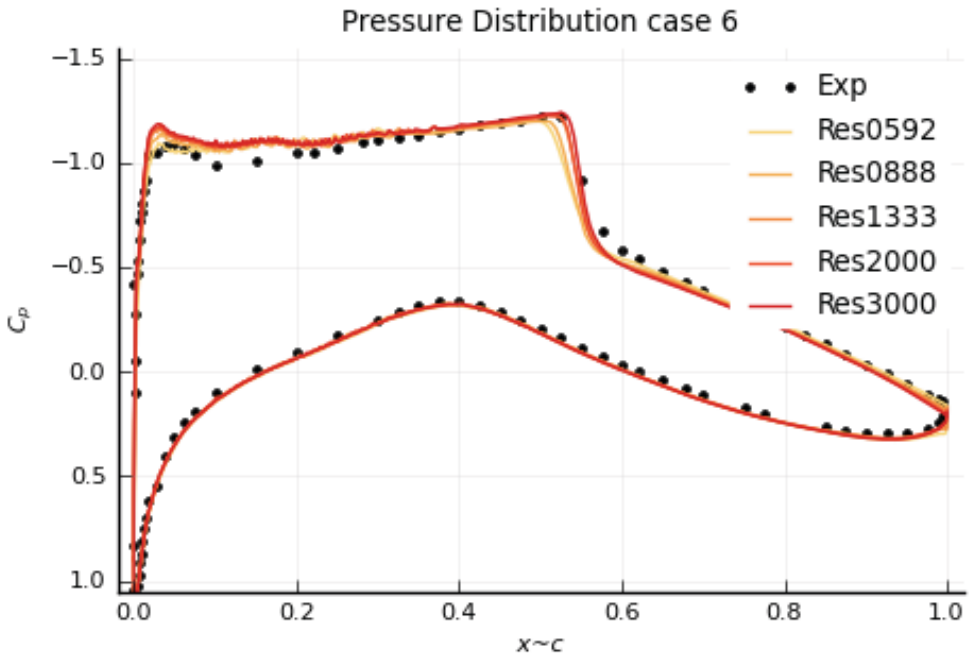
# Transonic Flow over the RAE 2822 airfoil




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| AoA [°] | 1.8148 | 2.4508 | 2.6873 | 2.7147 |
| Re [$10^6$] | 5.7 | 6.5 | 6.5 | 6.2 |


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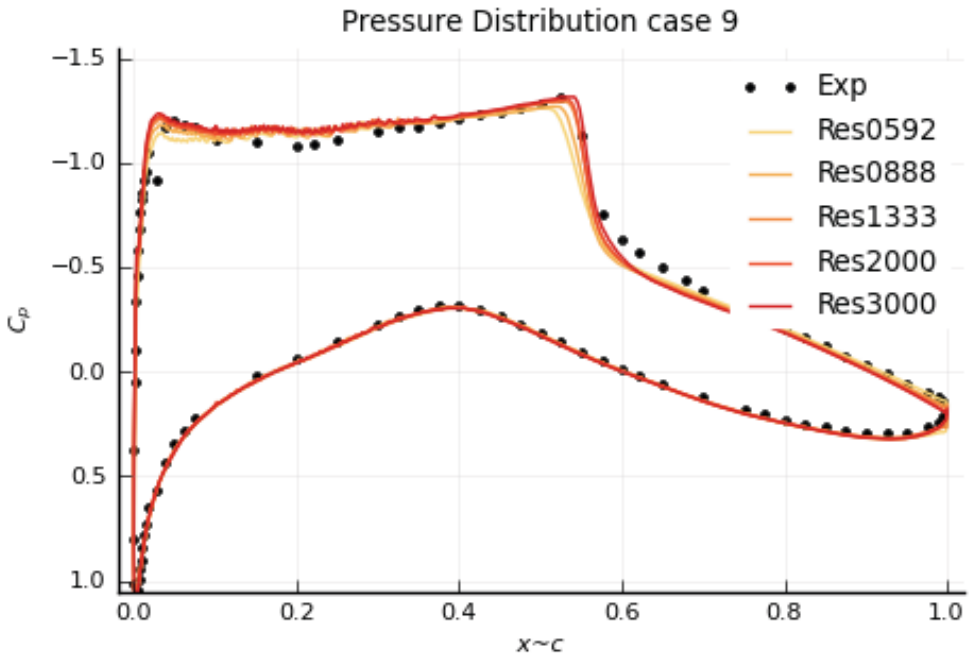
# Transonic Flow over the RAE 2822 airfoil




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|---|---|---|---|---|
| Ma [-] | 0.676 | 0.729 | 0.73 | 0.75 |
| AoA [°] | 1.8148 | 2.4508 | 2.6873 | 2.7147 |
| Re [$10^6$] | 5.7 | 6.5 | 6.5 | 6.2 |


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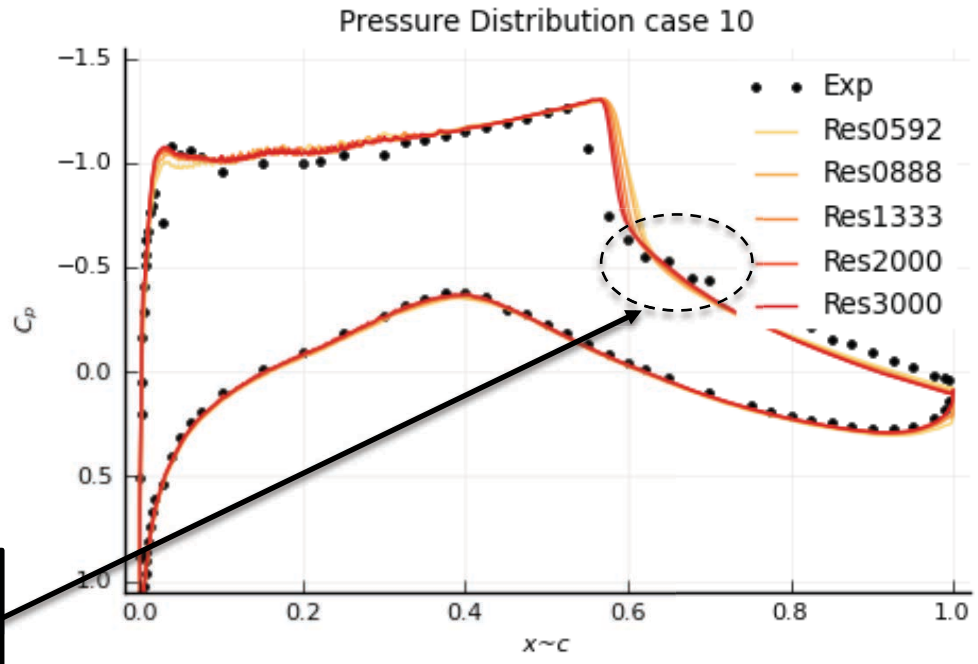
# Transonic Flow over the RAE 2822 airfoil




| | Case 1 | Case 6 | Case 9 | Case 10 |
|---|---|---|---|---|
| Ma [-] | 0.676 | 0.729 | 0.73 | 0.75 |
| AoA [°] | 1.8148 | 2.4508 | 2.6873 | 2.7147 |
| Re [$10^6$] | 5.7 | 6.5 | 6.5 | 6.2 |


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# Transonic Flow over the RAE 2822 airfoil

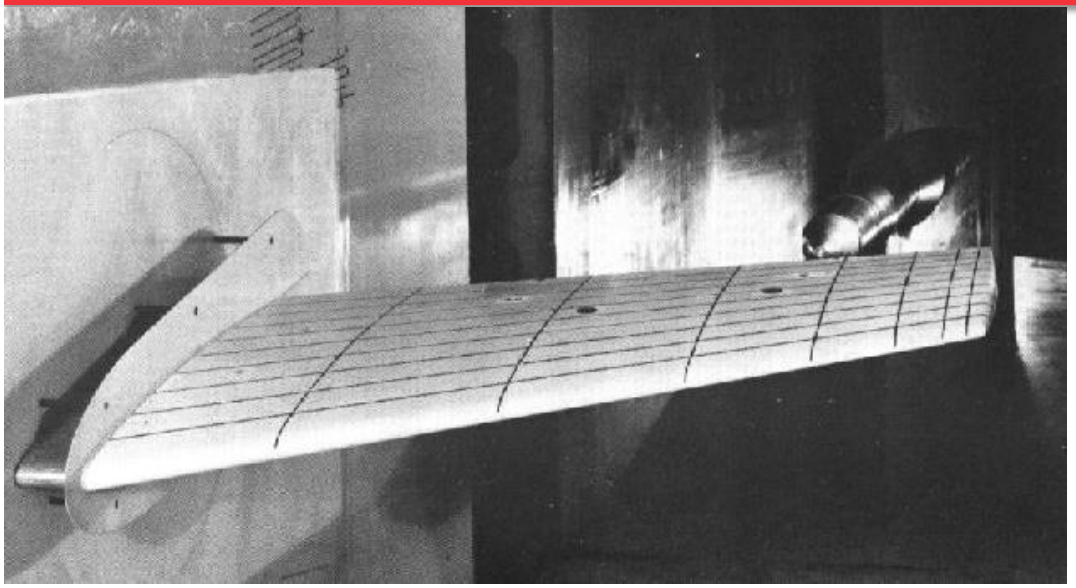



shock-induced separation expected to be better captured in 3D

| | Case 1 | Case 6 | Case 9 | Case 10 |
|---|---|---|---|---|
| Ma [-] | 0.676 | 0.729 | 0.73 | 0.75 |
| AoA [°] | 1.8148 | 2.4508 | 2.6873 | 2.7147 |
| Re [$10^6$] | 5.7 | 6.5 | 6.5 | 6.2 |

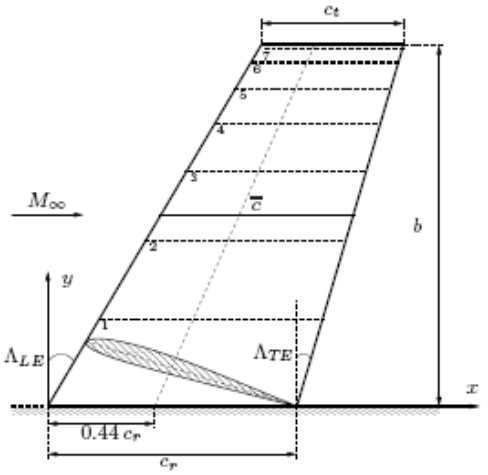

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# 3D Onera-M6



| | |
|---|---|
| Span, **b** | 1.1963 meters |
| Mean Aerodynamic Chord, **c** | 0.64607 meters |
| Aspect Ratio | 3.8 |
| Taper Ratio | 0.562 |
| Leading-edge Sweep | 30.0 degrees |
| Trailing-edge Sweep | 15.8 degrees |

| Mach # | Reynolds # | AoA |
|---|---|---|
| 0.84 | 11.72E6 | 3.06 |

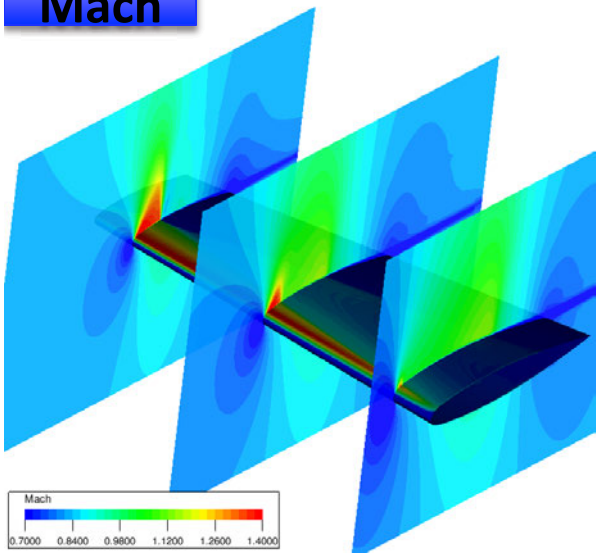



| Geometry | |
|---|---|
| AR | 3.8 |
| $b$ | 1.196 $m$ |
| $\Lambda_{LE}$ | 30° |
| $\Lambda_{TE}$ | 15.8° |
| $\lambda$ | 0.562 |
| $\overline{c}$ | 0.646 $m$ |
| $S$ | 1.506 $m^2$ |

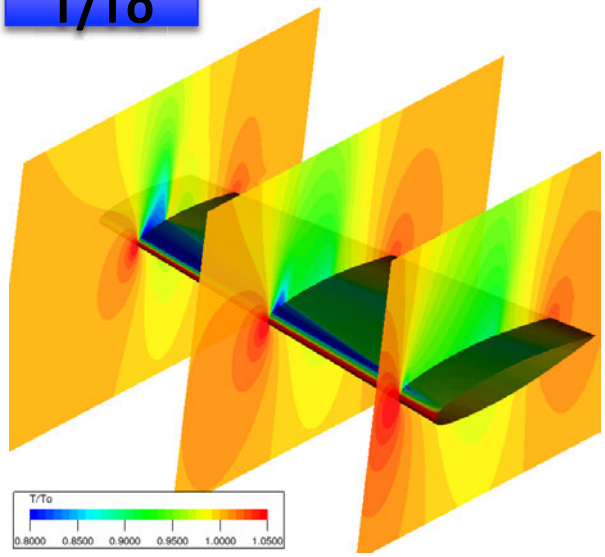

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# Flow-field Images

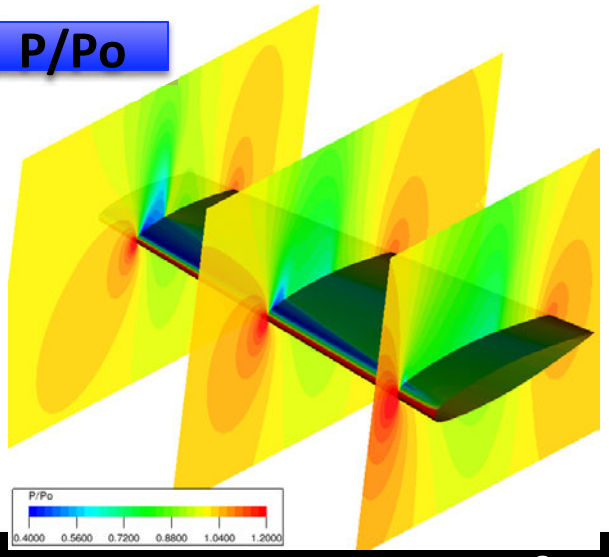
**Mach**



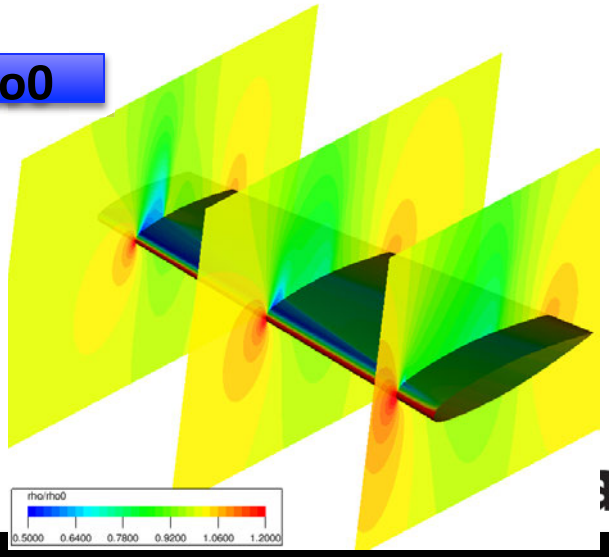

**T/To**




**P/Po**



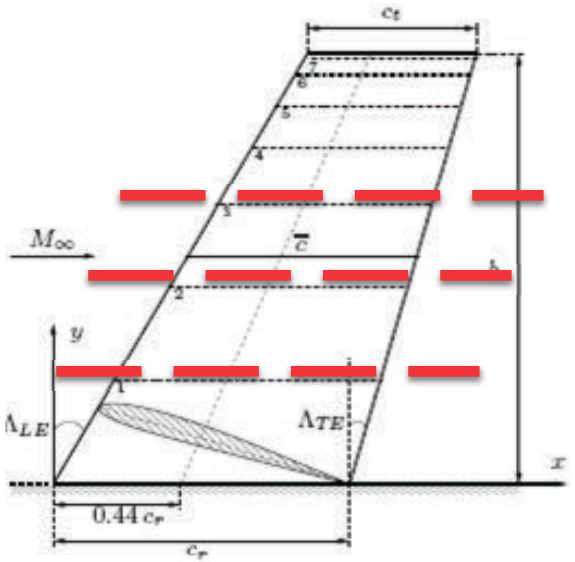

**rho/rho0**

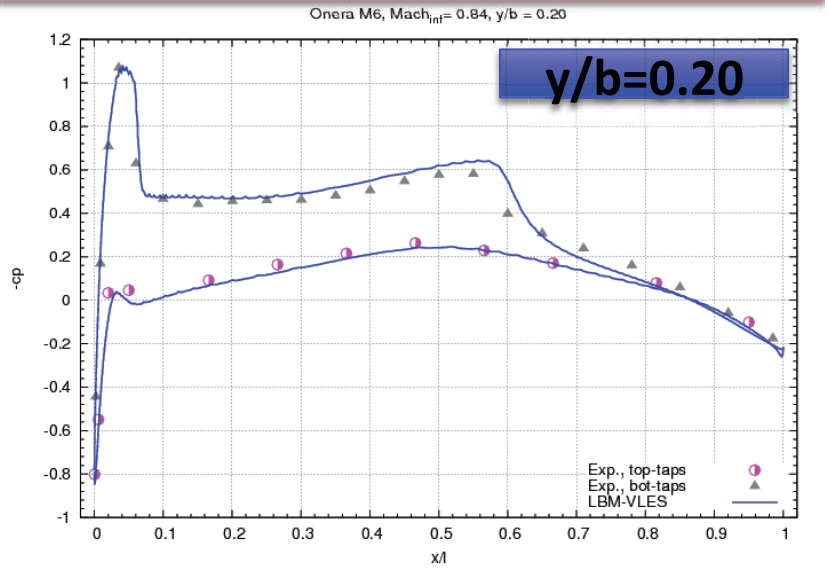


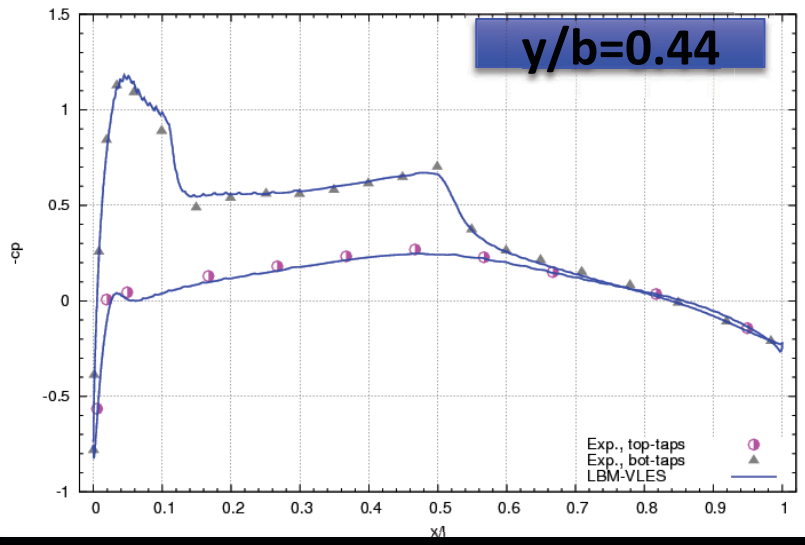


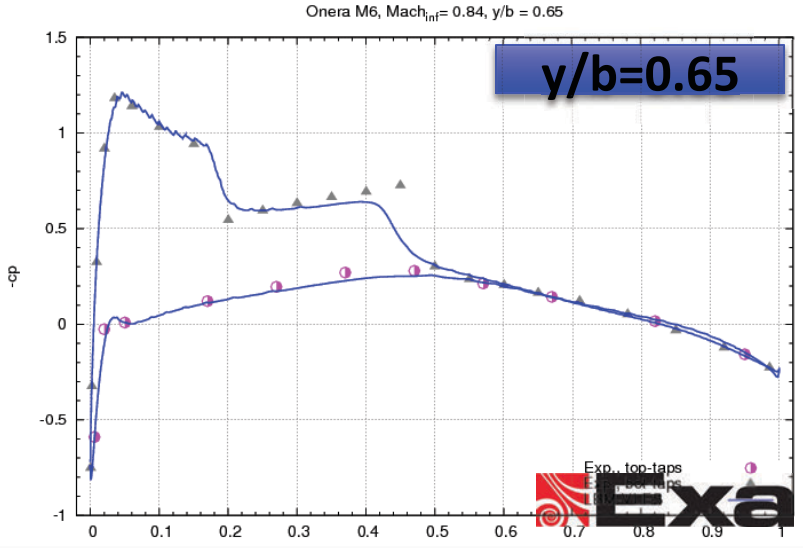
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# 3D Onera-M6
# Sectional Cp on Surface



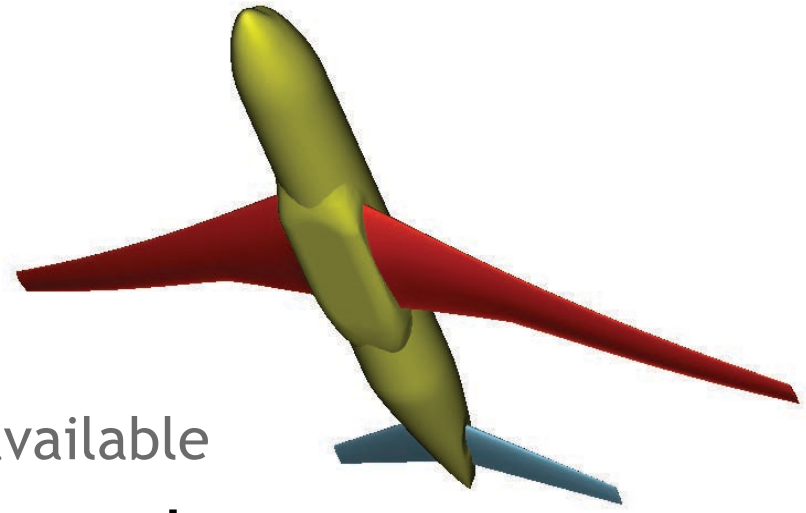





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# NASA-CRM Model

- DPW4 Geometry
  - *Reference CFD Data*
  - *Wing-body & tail*
    - Supercritical wing
    - Built to the design-shape
    - Twist correction information available

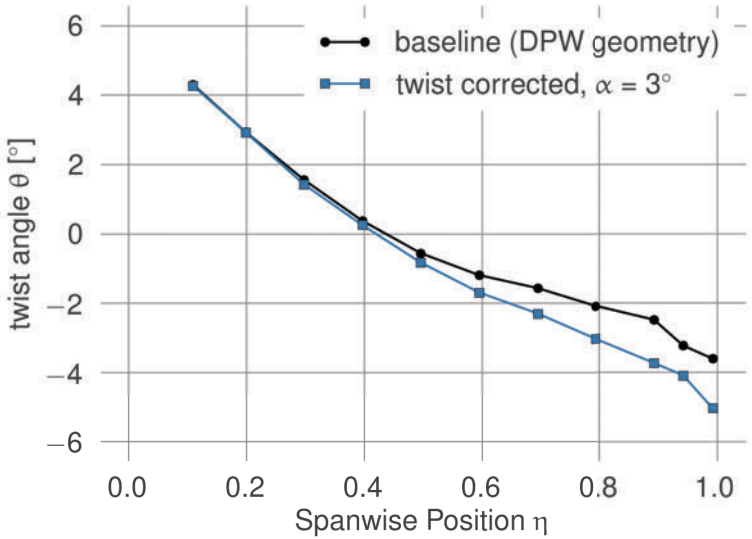


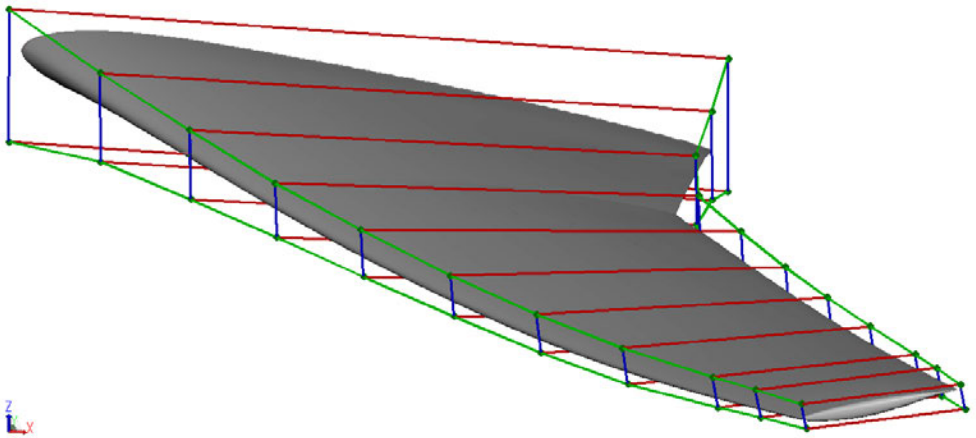
- Measured at several Windtunnels
  - ***ETW, NTF**, NASA Ames 11ft, JAXA JTWT*




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# Wing Twist Correction



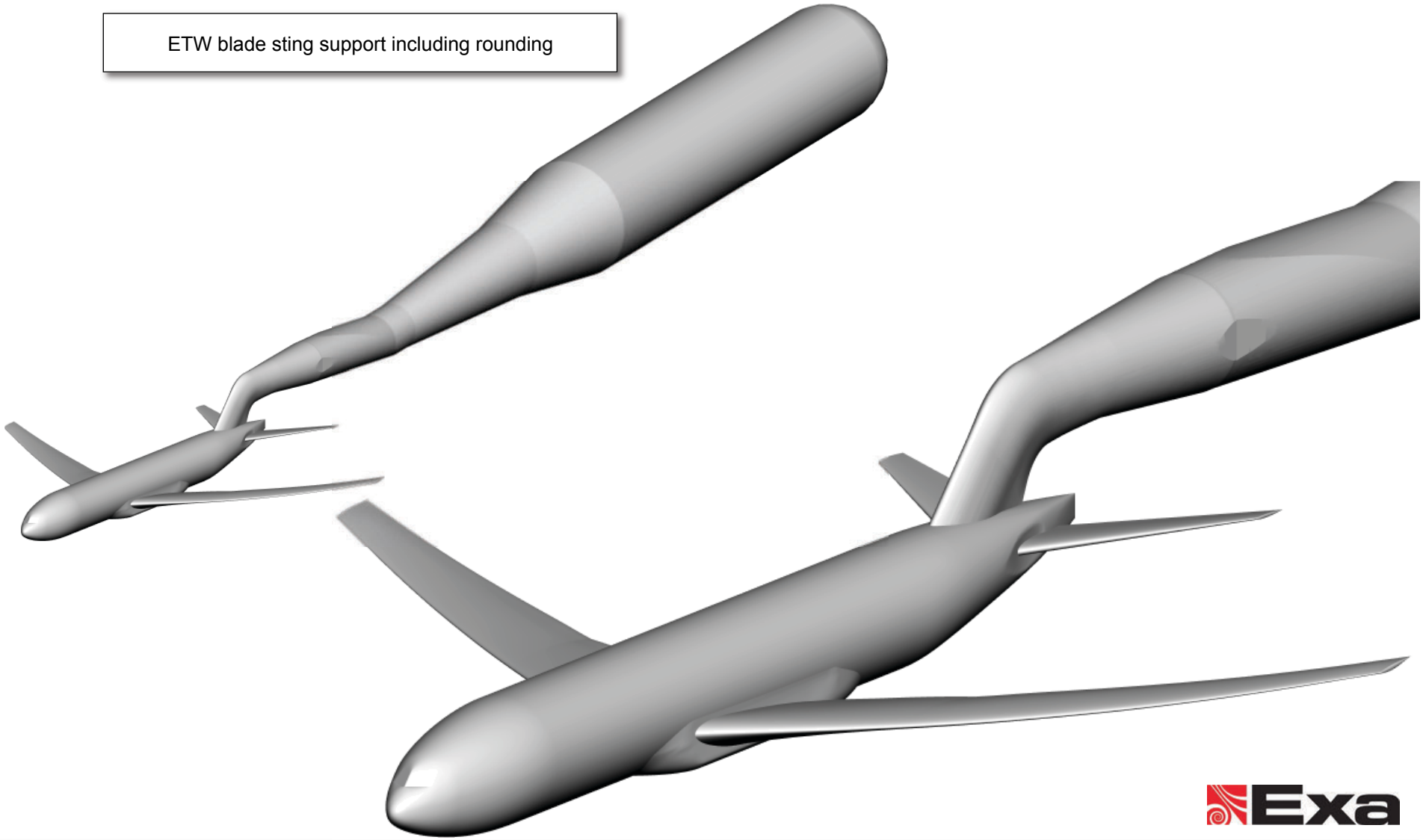



**PowerDELTA® morphing**


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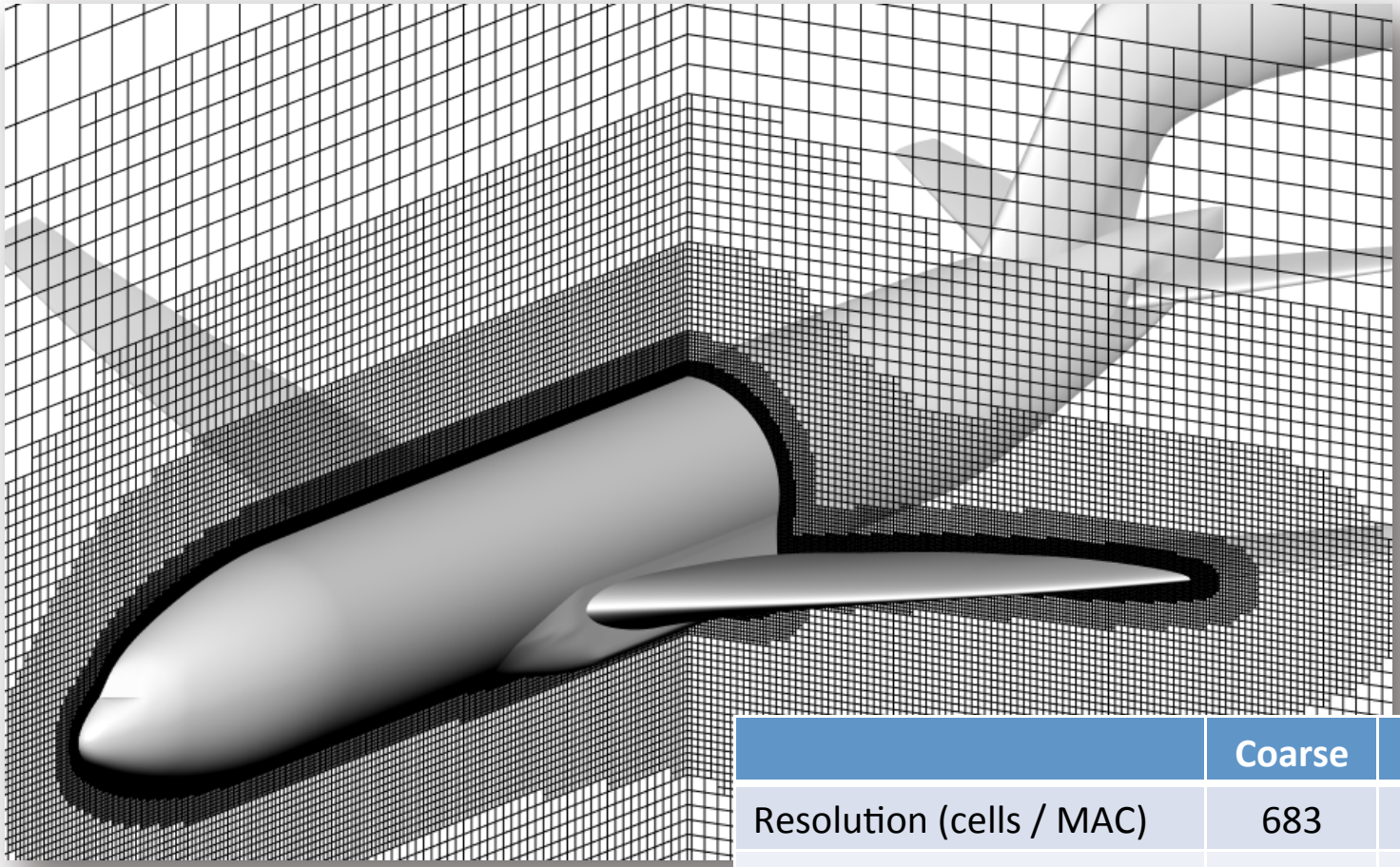
# Simulated Geometry

ETW blade sting support including rounding




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# Computational Mesh*

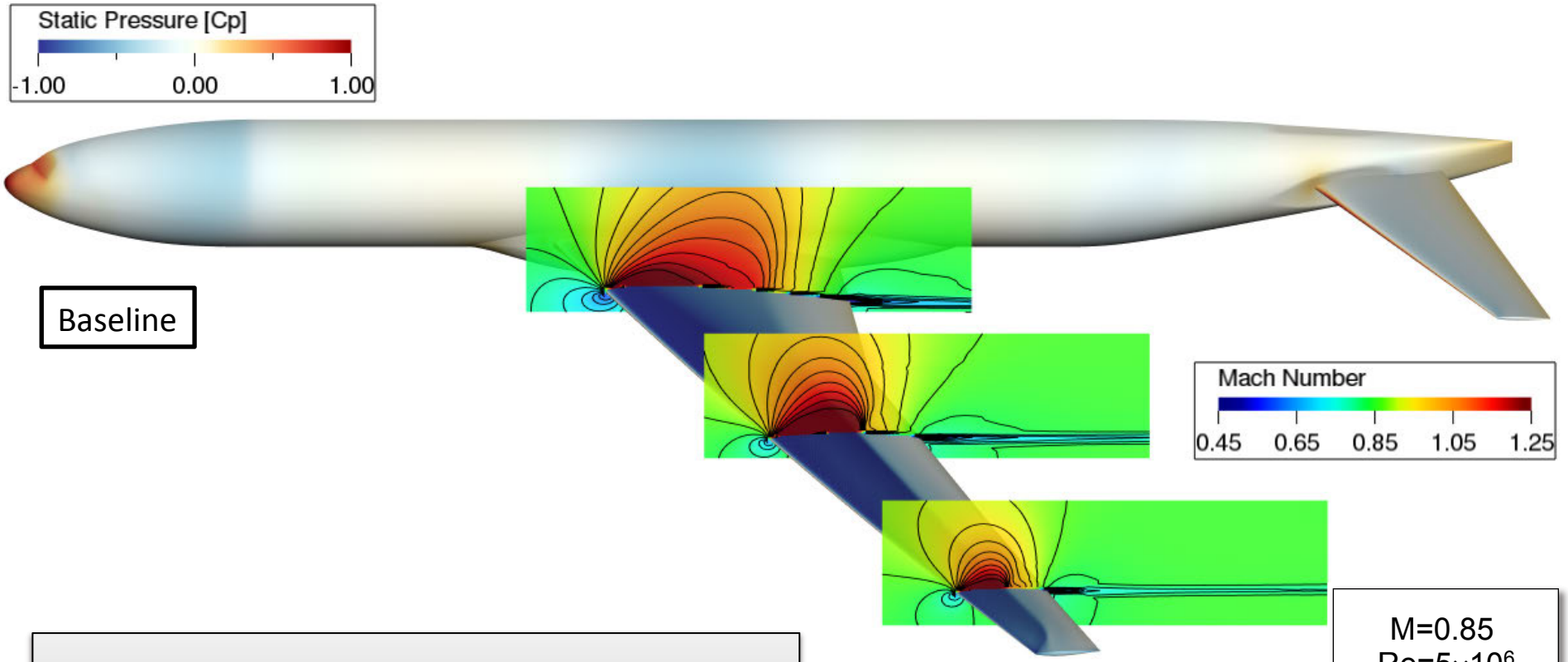


| | Coarse | Medium | Fine |
|---|---|---|---|
| Resolution (cells / MAC) | 683 | 1024 | 1536 |
| Voxels [$10^6$] | 30 | 88 | 274 |
| CPUh [$10^3$] | 5.4 | 17 | 38 |
| Wallclock on 360 cores [d] | 0.6 | 2 | 4.4 |

* Simulated with Symmetry
* additional resolution to resolve sting negligible


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# Results



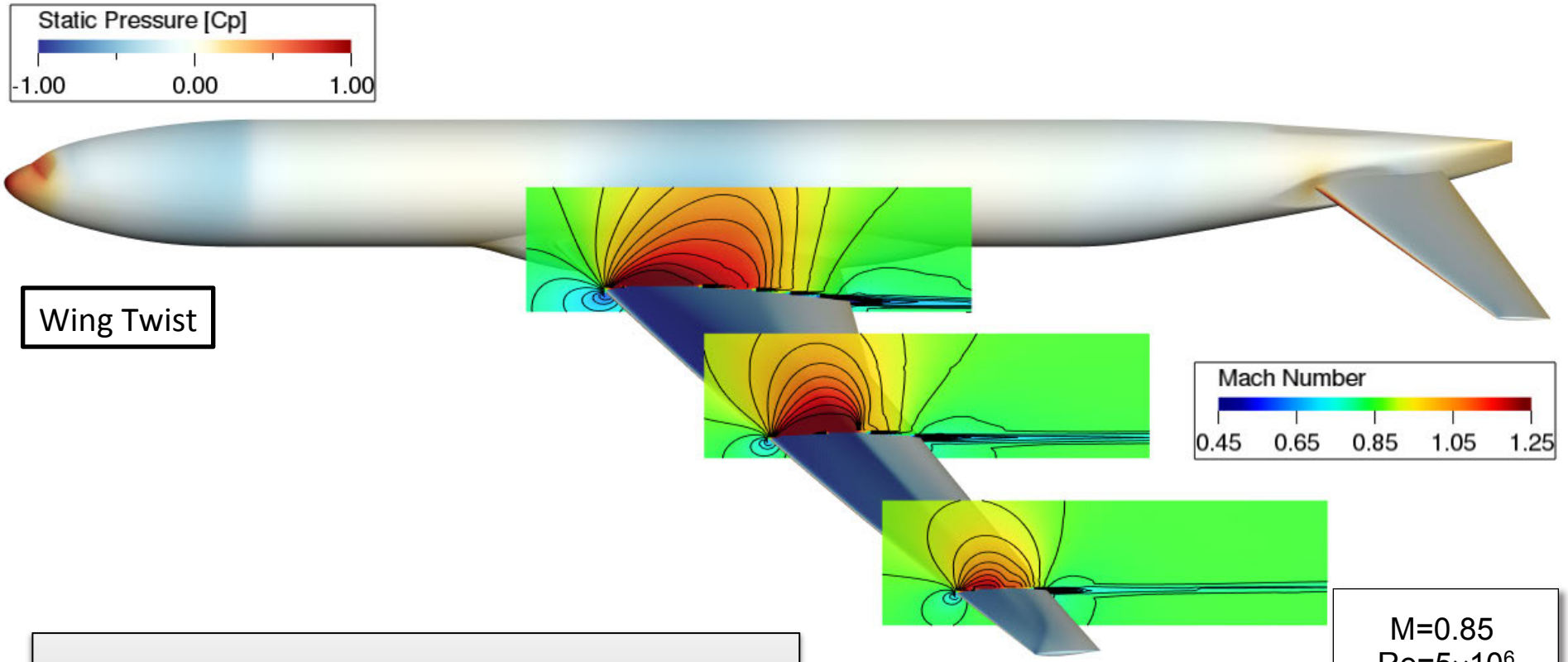

Koenig, B.,and Fares, E. "Validation of a Transonic Lattice-Boltzmann Method on the NASA Common Research Model", AIAA 2023-2016.

M=0.85
$Re=5\times10^6$
$\alpha=2.9°$


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# Results

- DPW4 Geometry (NASA CRM model)

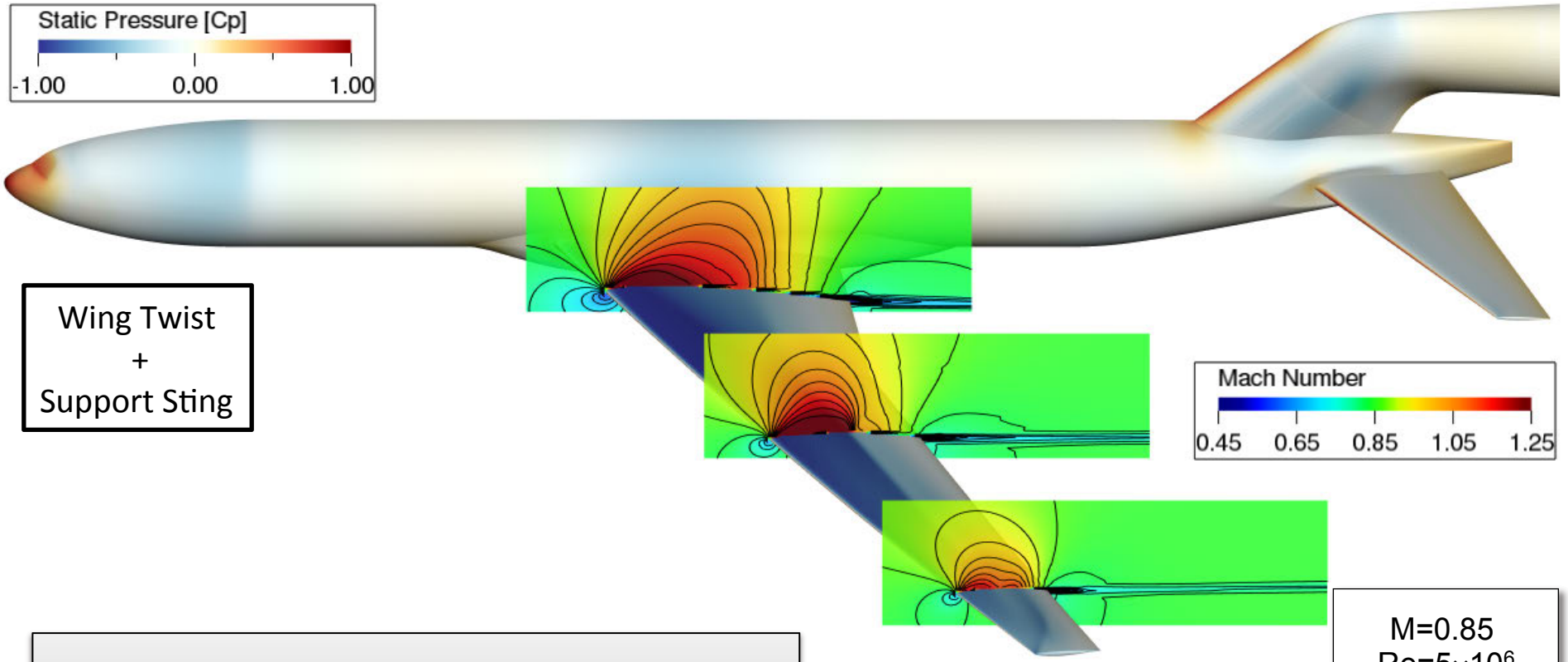



Koenig, B.,and Fares, E. "Validation of a Transonic Lattice-Boltzmann Method on the NASA Common Research Model", AIAA 2023-2016.


© Exa Corporation

# Results

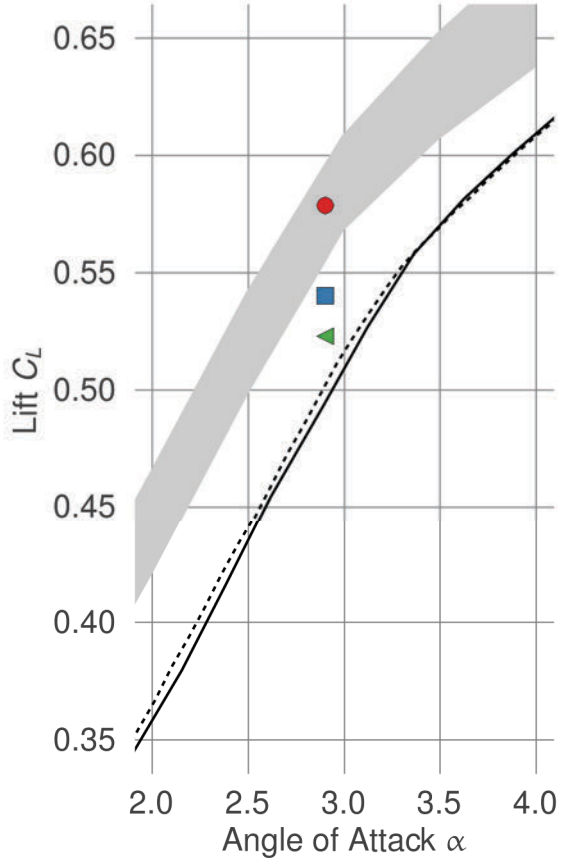
- DPW4 Geometry (NASA CRM model)

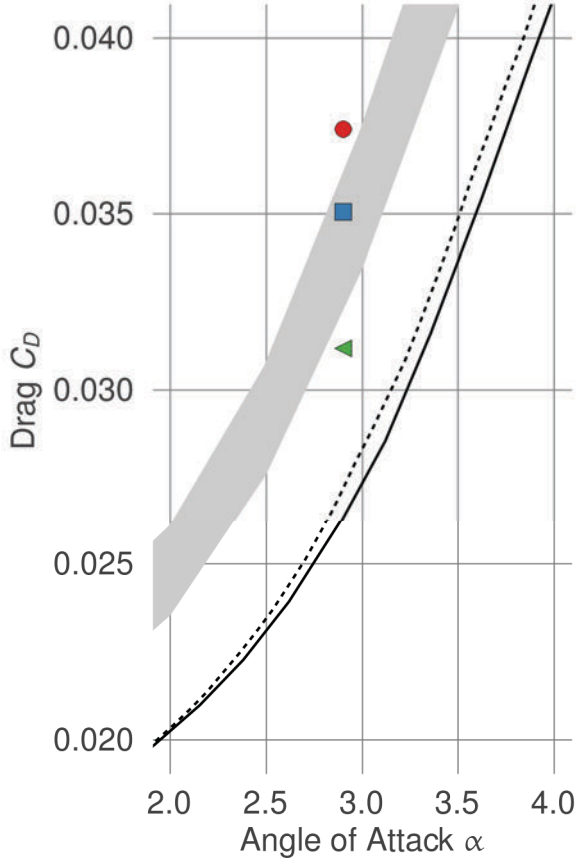


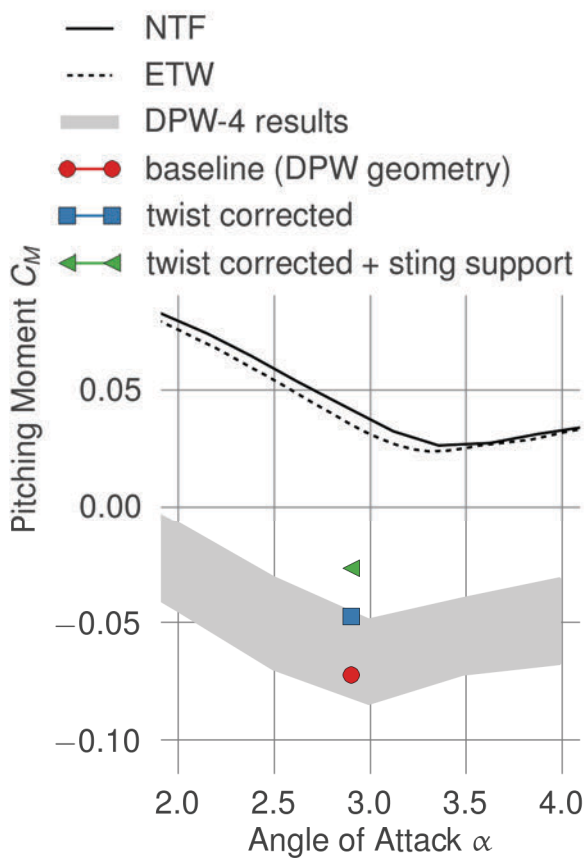

Koenig, B.,and Fares, E. "Validation of a Transonic Lattice-Boltzmann Method on the NASA Common Research Model", AIAA 2023-2016.


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# Results – Wing Twist and Sting Effects



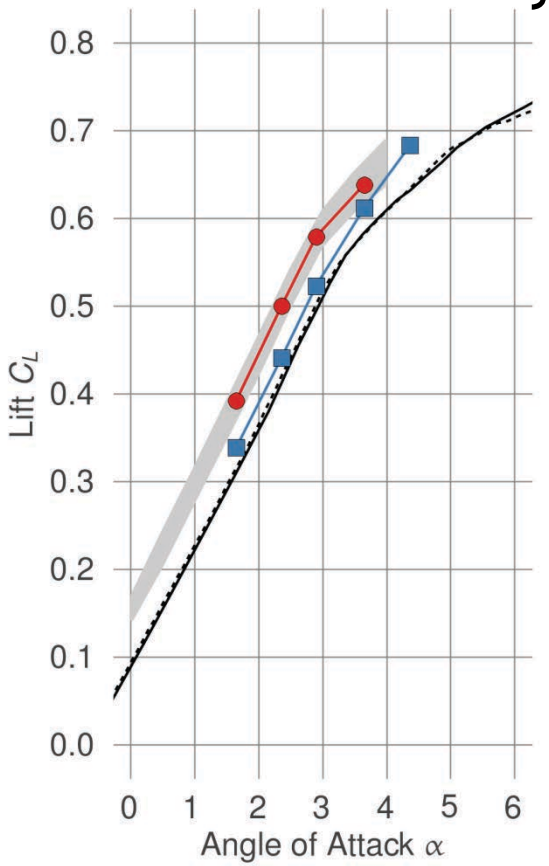



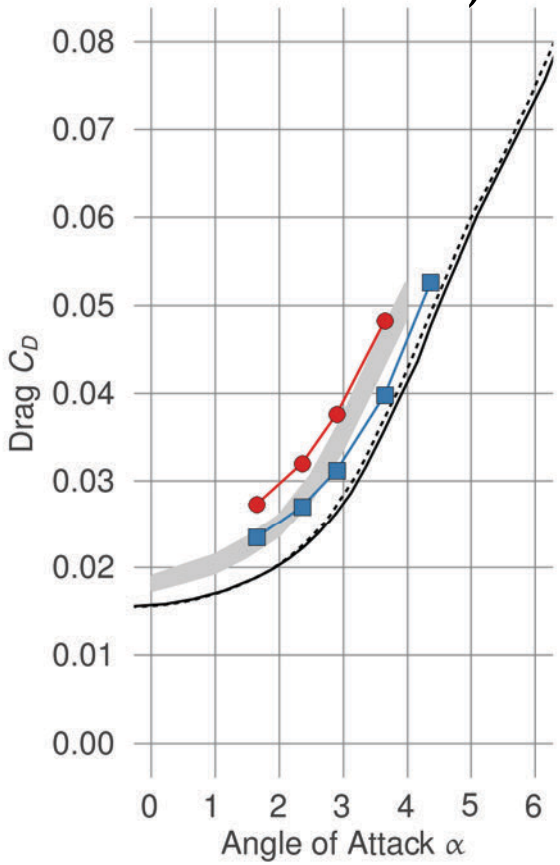

M=0.85
Re=5×10$^6$

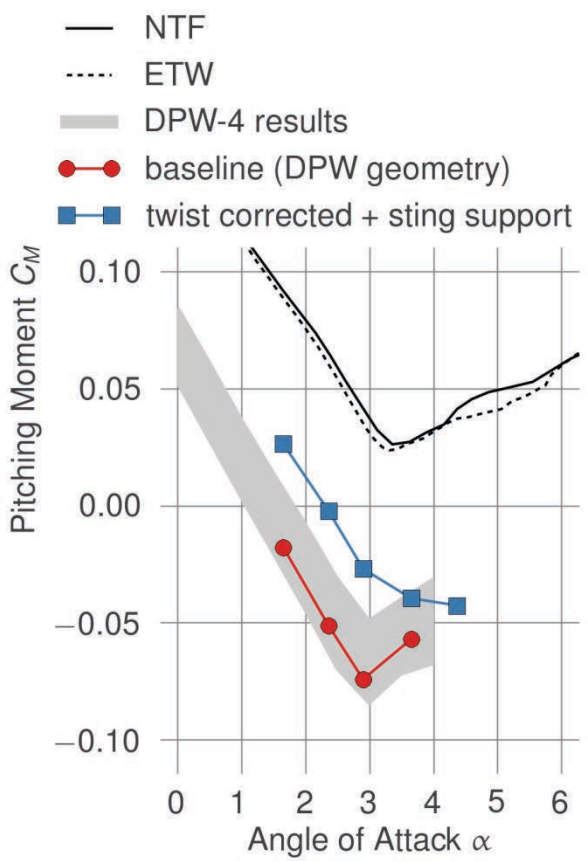

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# Results – Wing Twist and Sting Effects

- DPW4 Geometry (NASA CRM model)



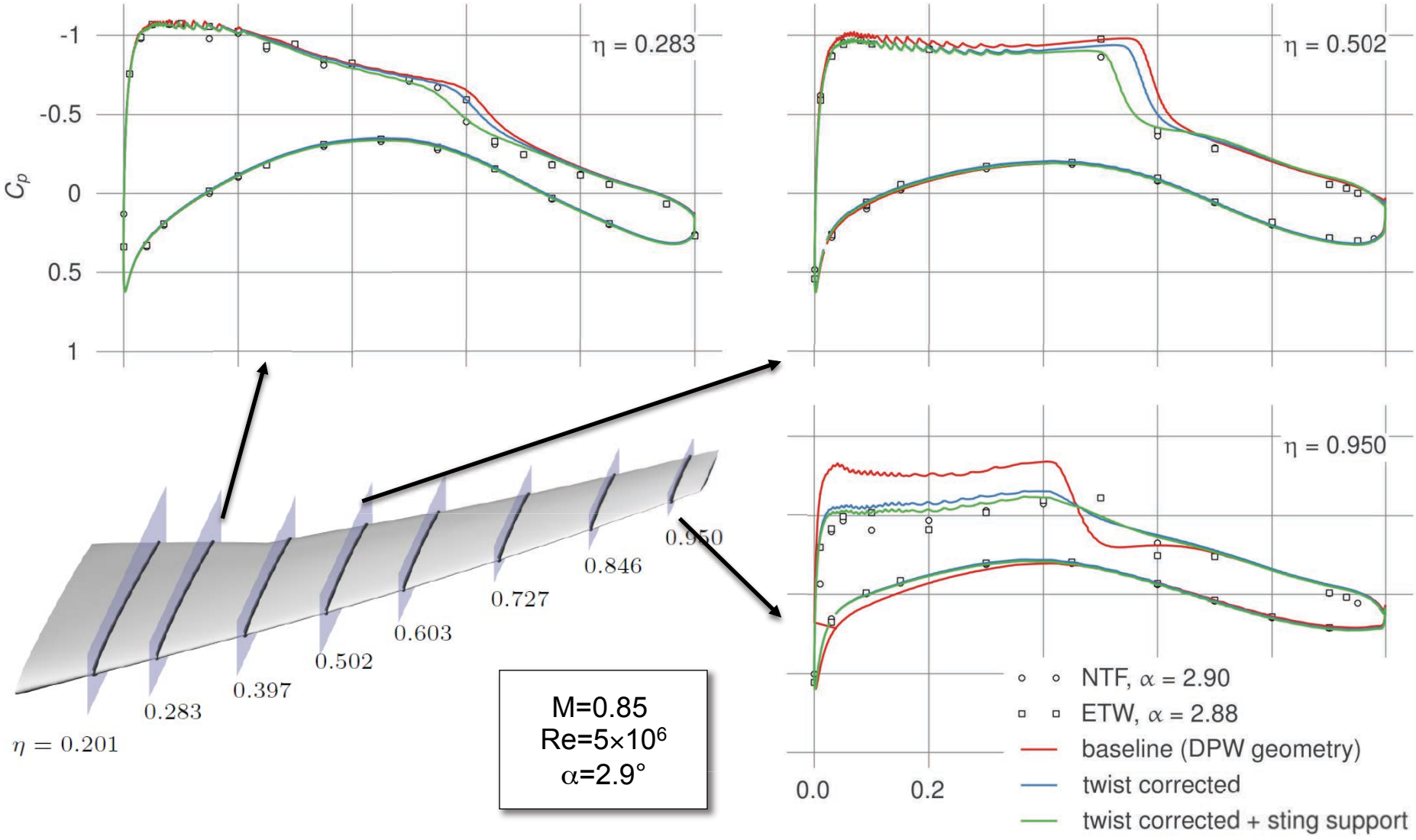




M=0.85
Re=5×10$^6$


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# Results – Wing Twist and Sting Effects

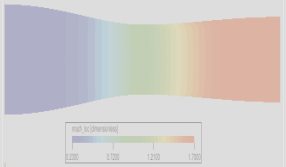




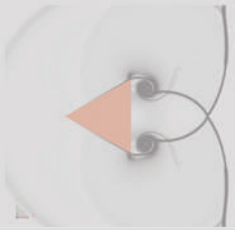
© Exa Corporation

# Transonic Code Validation & Application

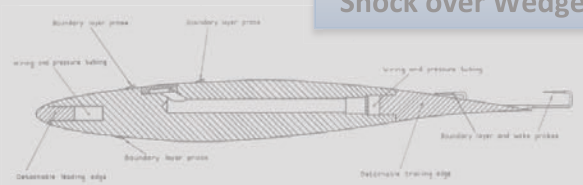
## Fundamental Validations



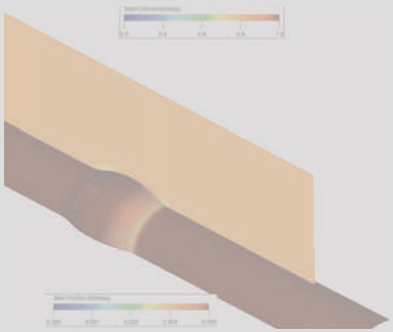
CDV nozzle



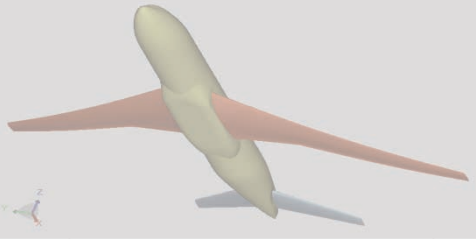
Shock over Wedge



RAE 2822 Airfoil

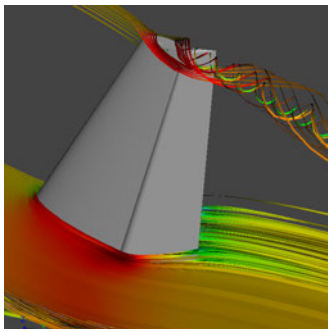


Transonic Bump



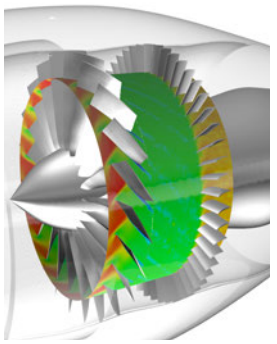
CRM

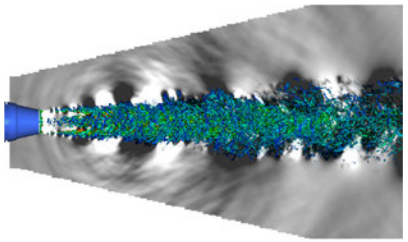
## Industrial Applications



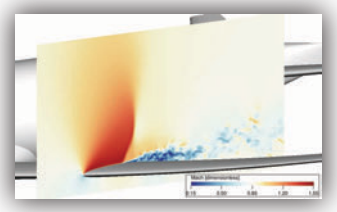
Flow Control

Fan Noise



Jet Noise

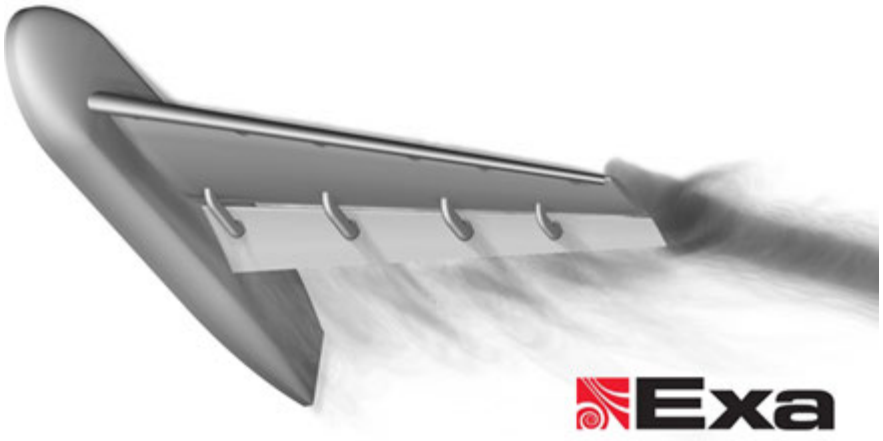


Buffet



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# Trapezoidal Wing FSF Configurations

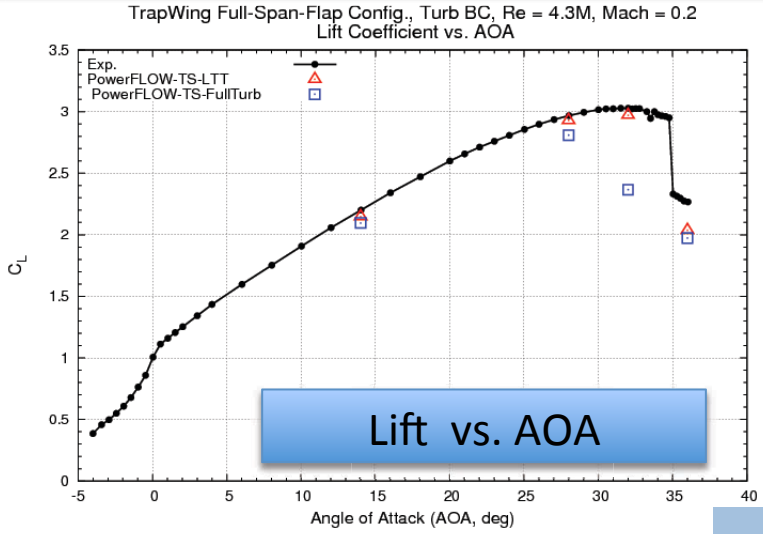


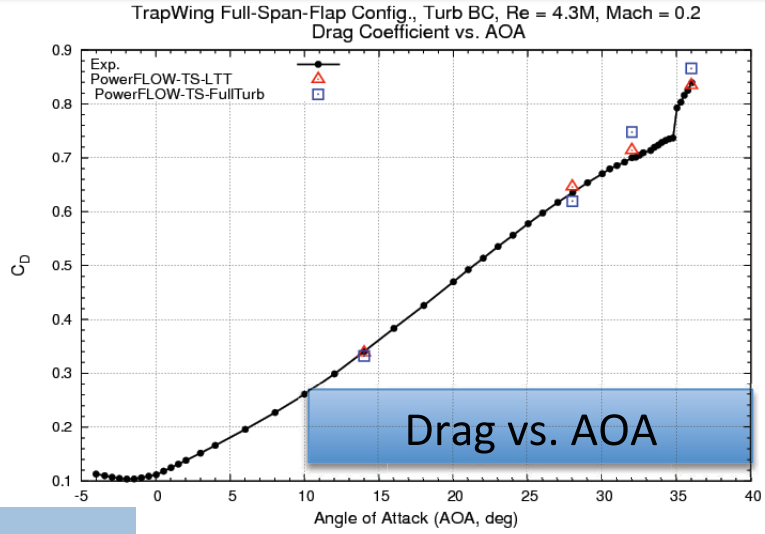

- **Full Span Flap (FSF) Configuration**
- **Re = 4.3 M**
- **Mach = 0.2**
- **Laminar to turbulence transition (LTT) included**



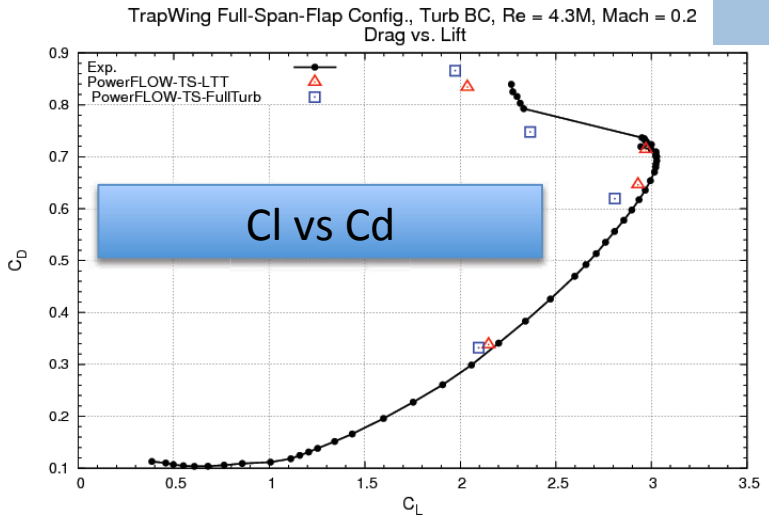

© Exa Corporation

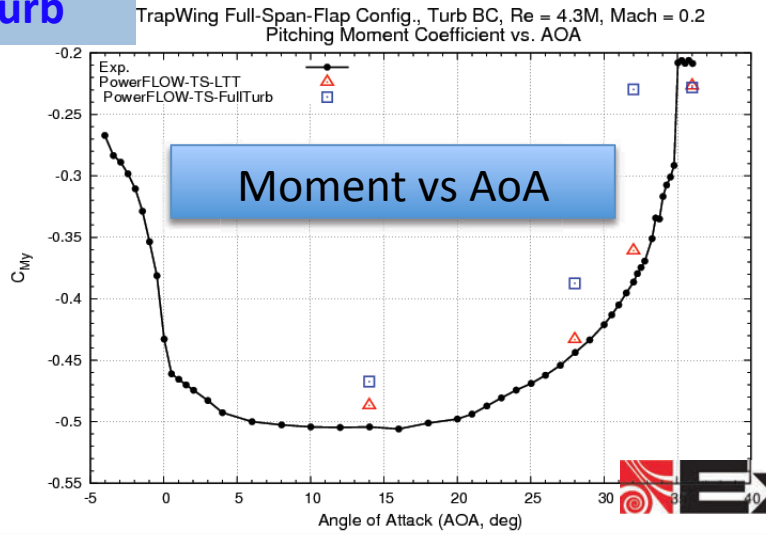
# TrapWing : Drag & Lift




**LTT**
**Full-Turb**



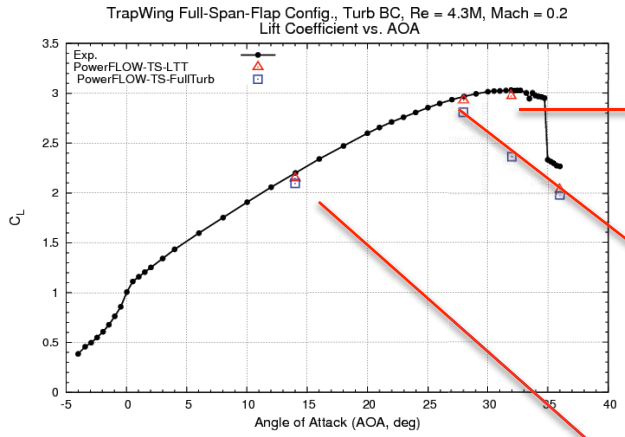



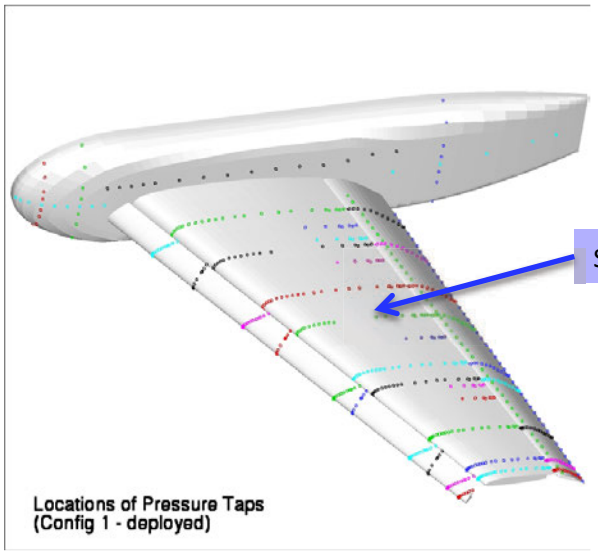


© Exa Corporation

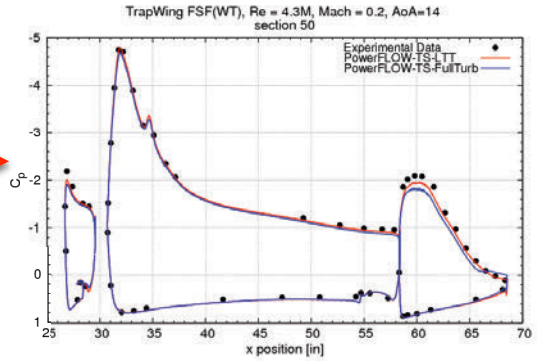
# Sectional Surface Pressure

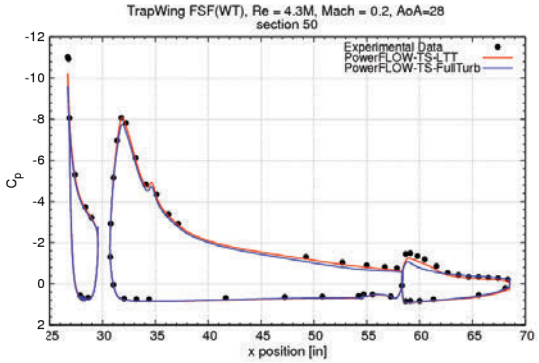
**LTT**
**Full-Turb**

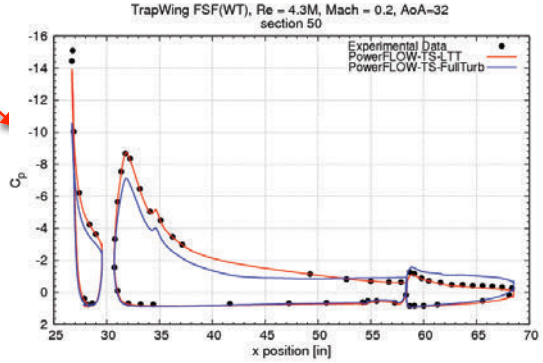



Section 50



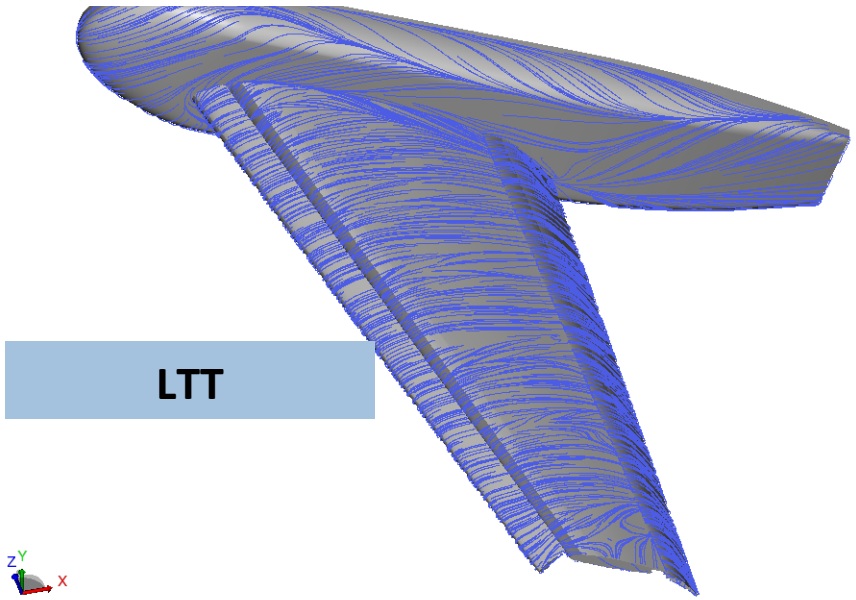





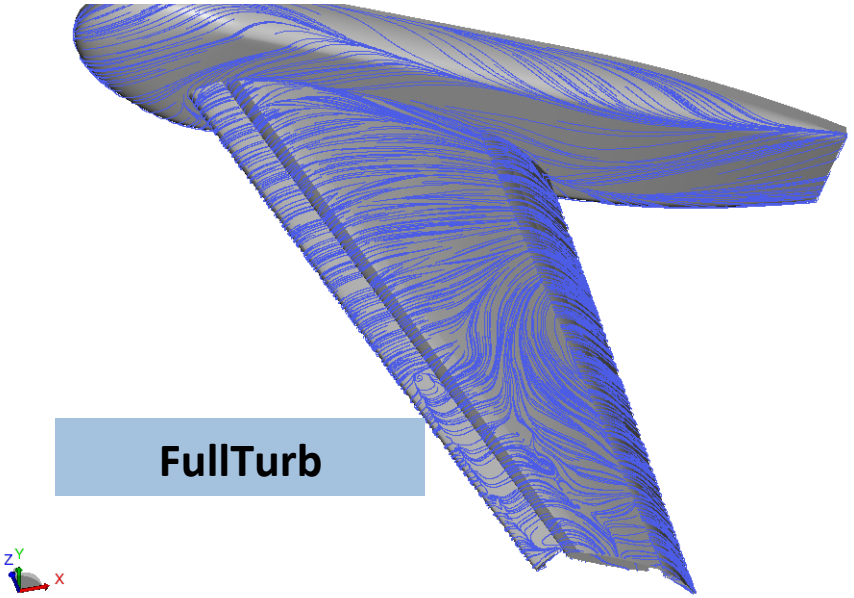
© Exa Corporation

# Surface Streamlines – AoA 32



LTT





FullTurb

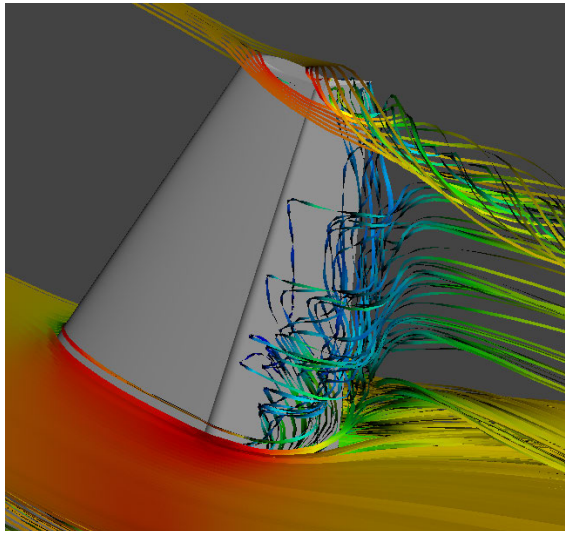




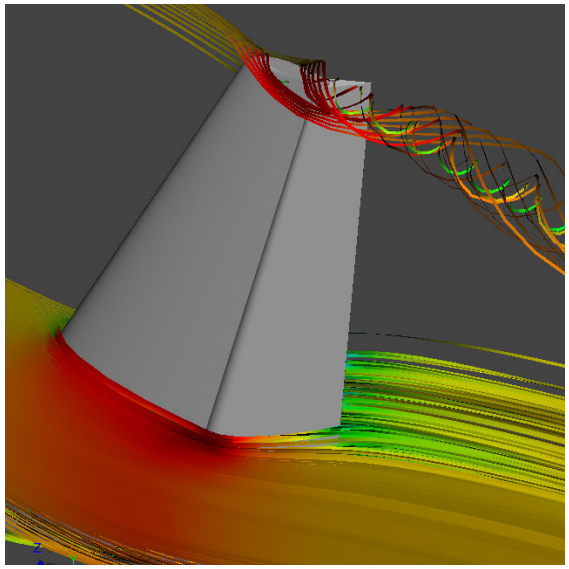
© Exa Corporation

# NASA - Active Flow Control

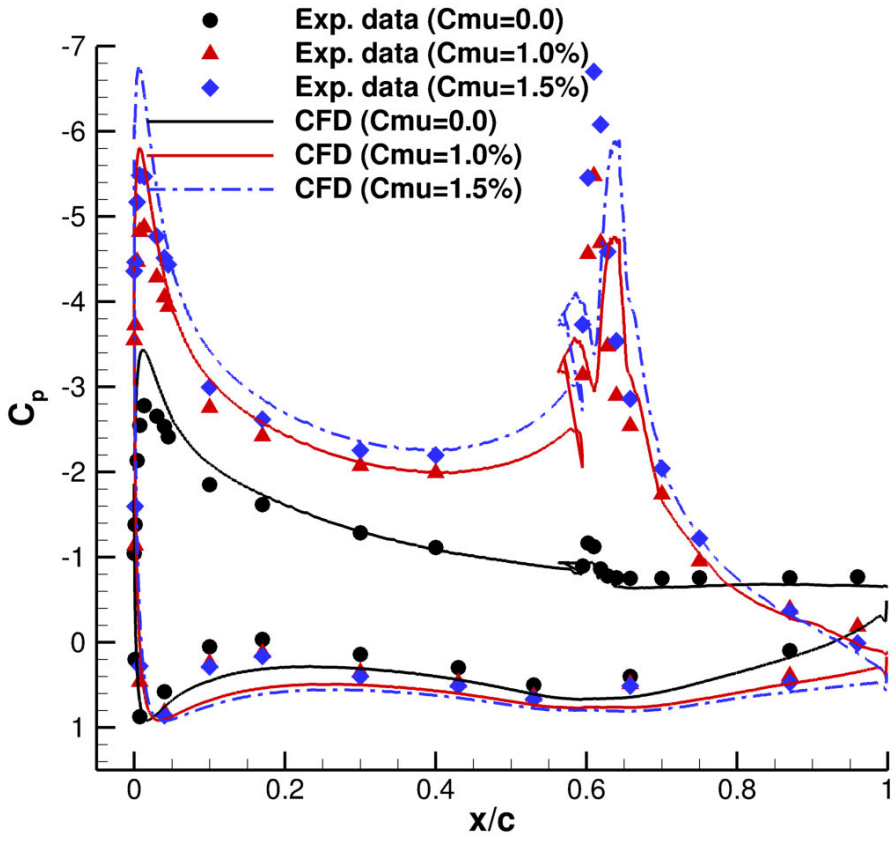
Unactuated, Cmu=0.0



Actuated, Cmu=1.5%



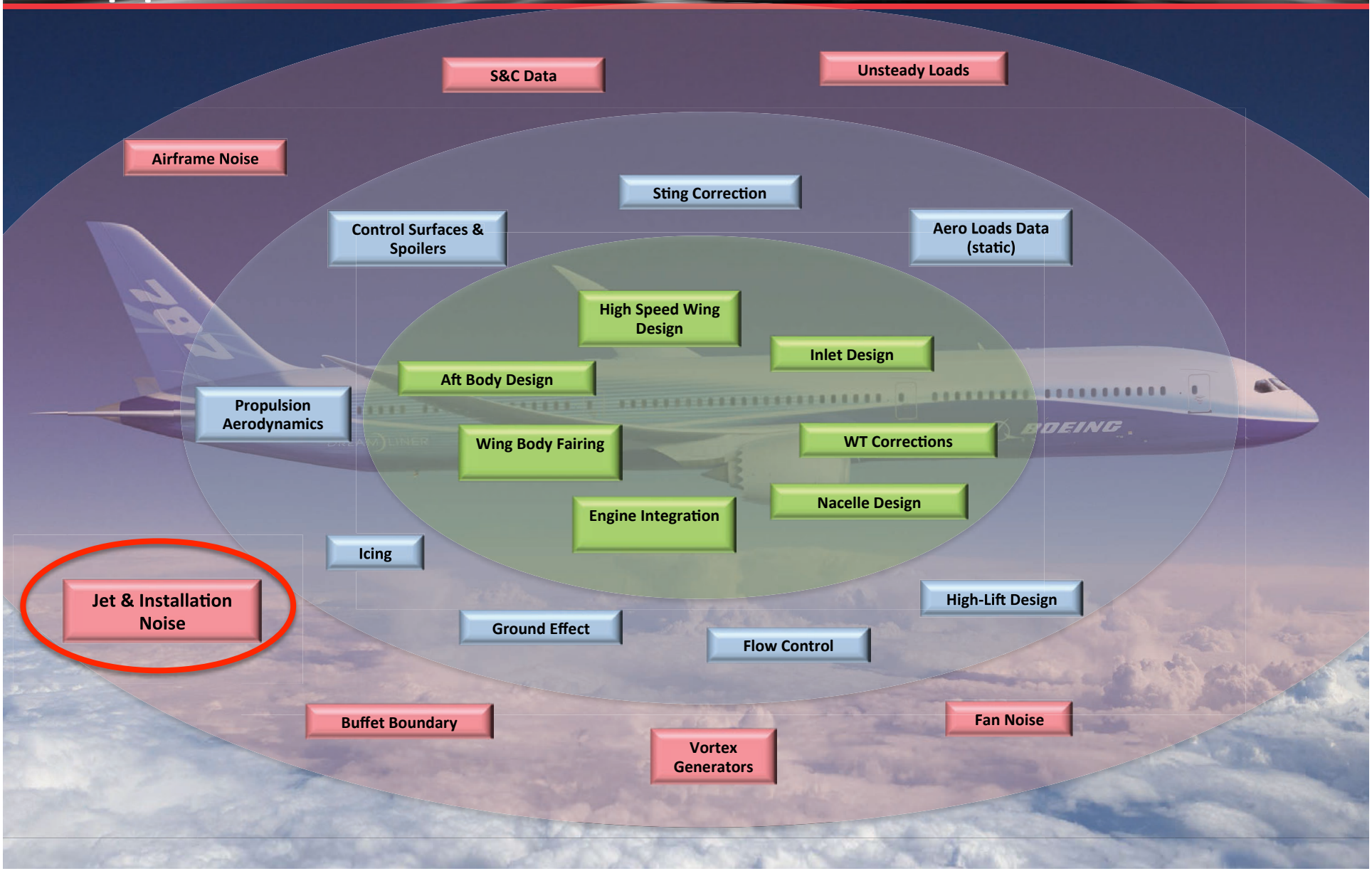
$C_p$ at 89% span





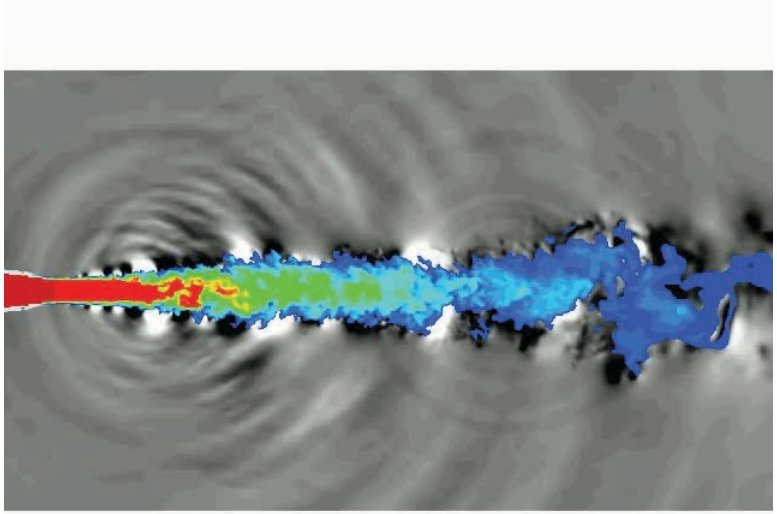
© Exa Corporation

# Applications

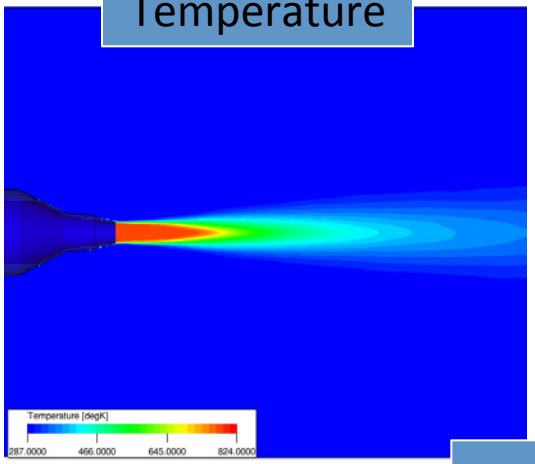


# Jet Noise: SMC000 (SP46): Ma=0.9, $T_j/T_o$=2.7

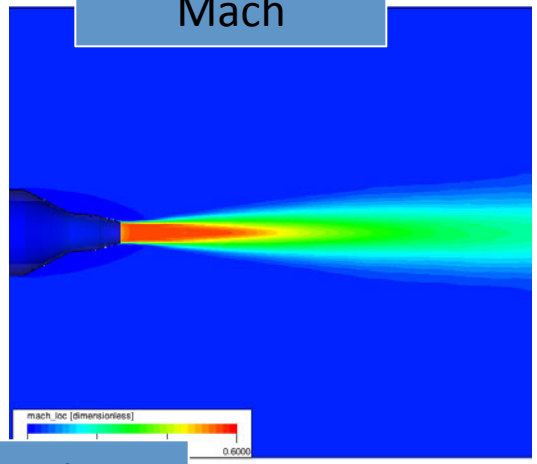
| $M_j = U_j/a_j$ | $M_a = U_j/a_{inf}$ | $T_j/T_{inf}$ |
|---|---|---|
| 0.548 | 0.90 | 2.70 |



Temperature

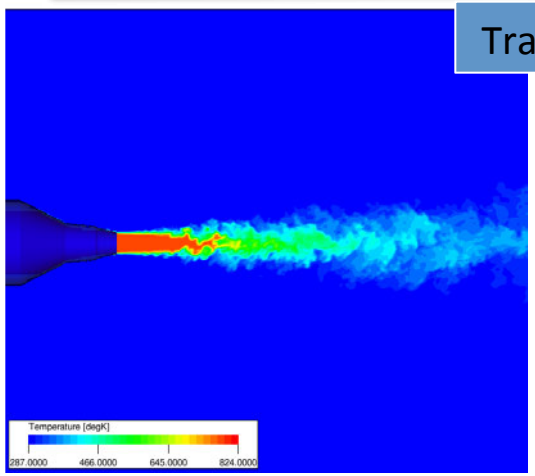


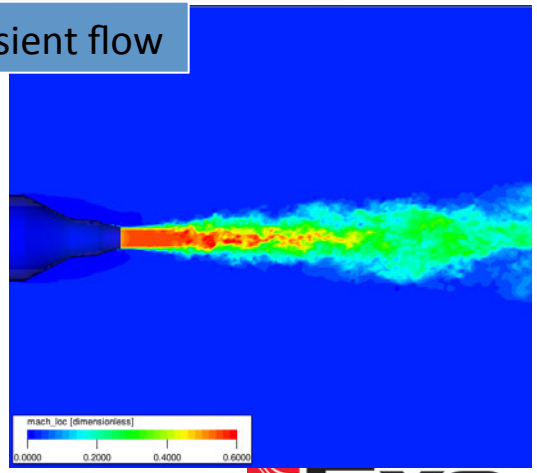

Mach




Mean flow

Transient flow



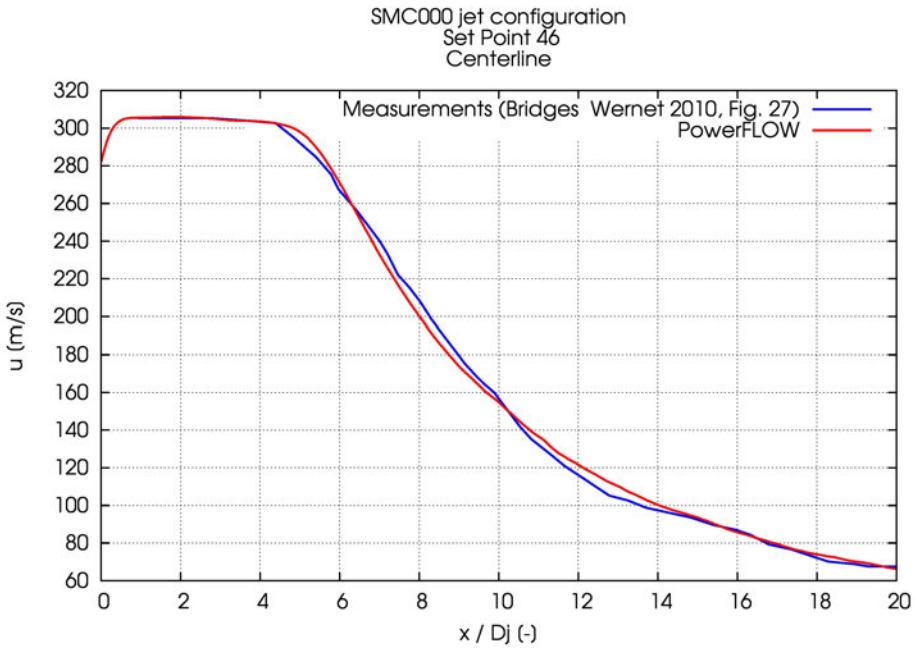



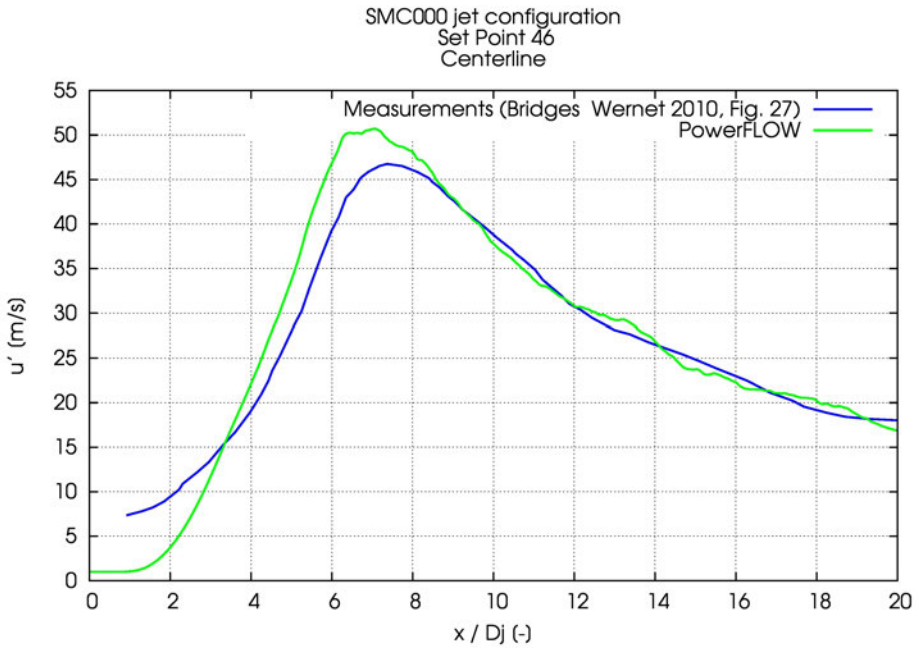

Exa



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# 3D SMC Jet, SP46: Centerline mean and RMS velocity



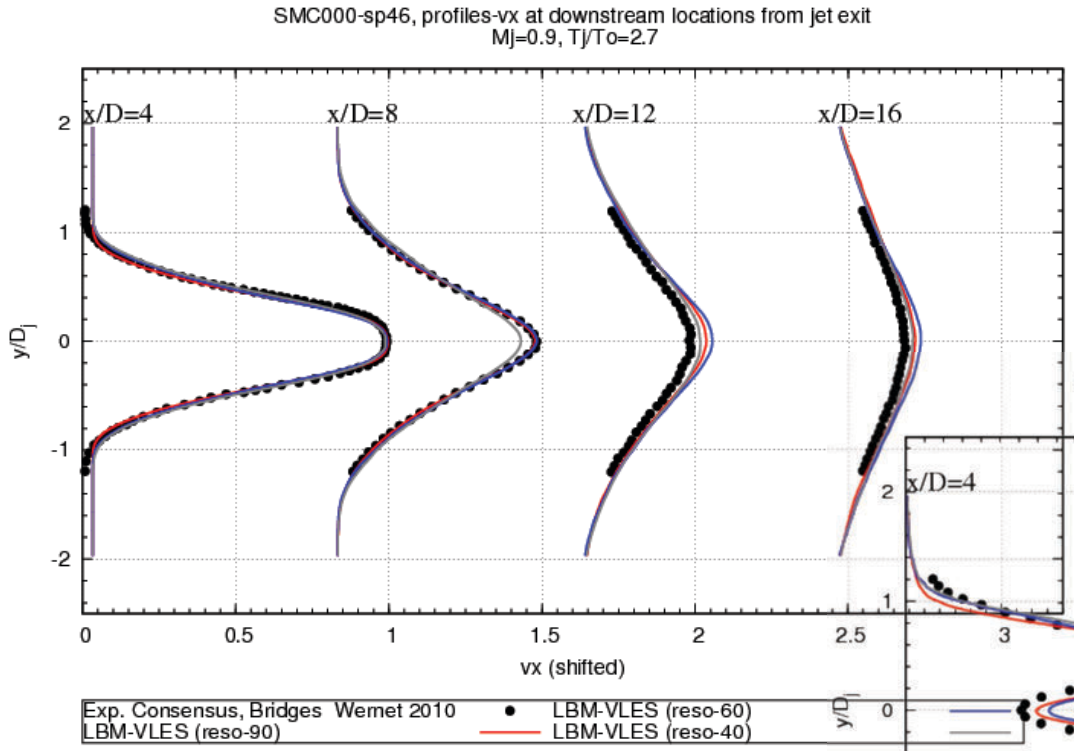



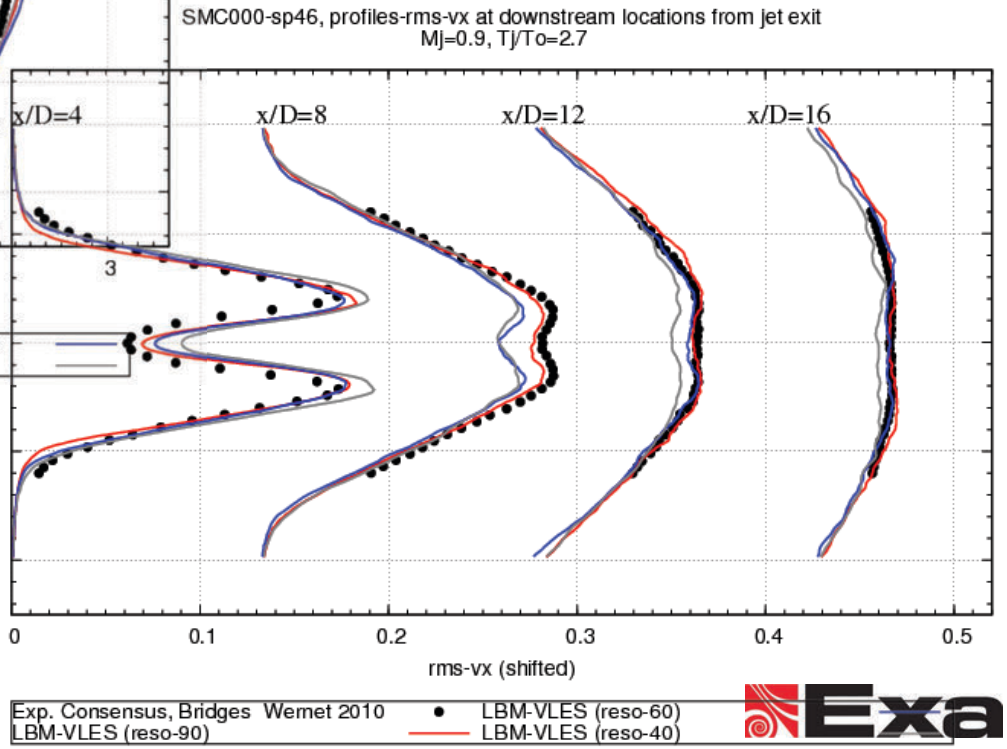

**Mean velocity**

**RMS velocity**


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# 3D SMC Jet, SP46: Radical profiles of mean and RMS velocity

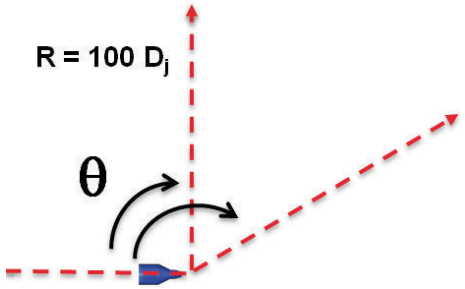


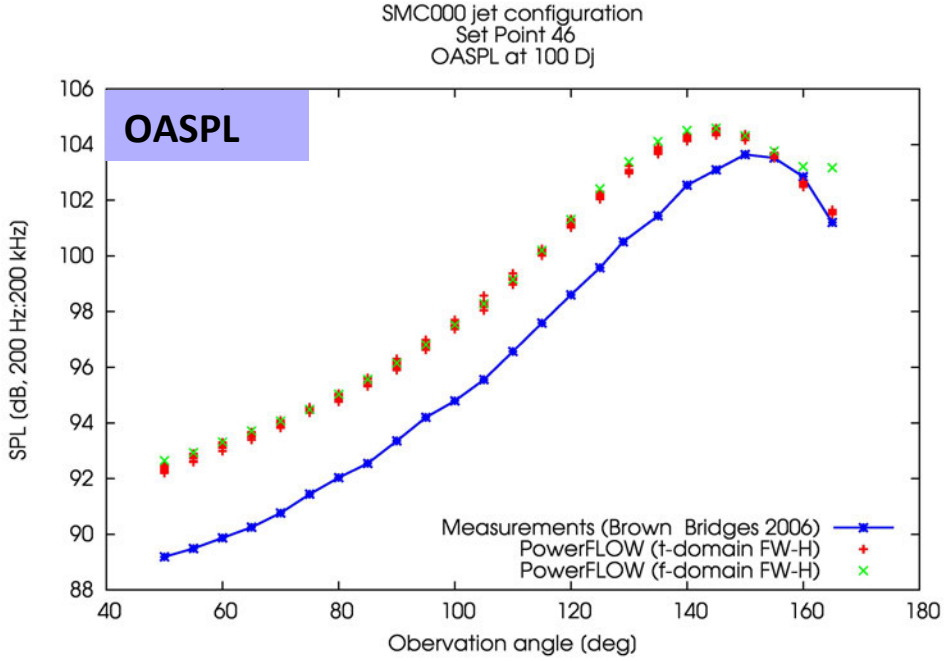



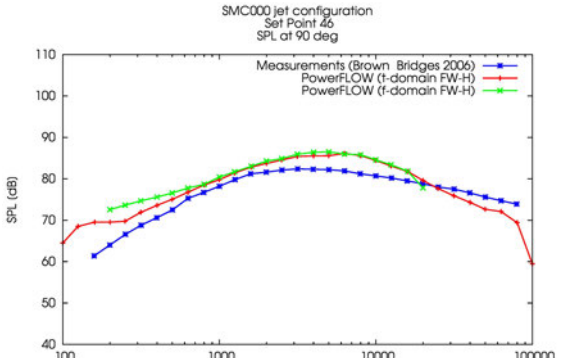

**Exp.**
**Reso-90**
**Reso-60**
**Reso-40**


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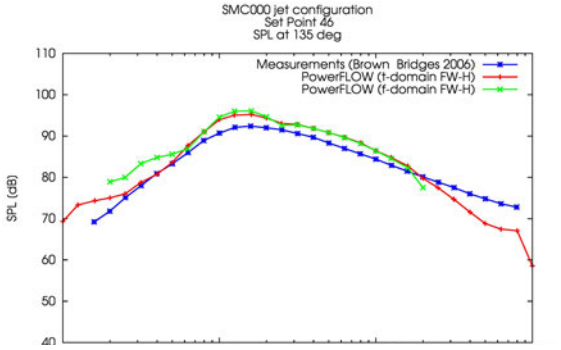
# 3D SMC Jet, SP46, FW-H OASPL and Far-field probes



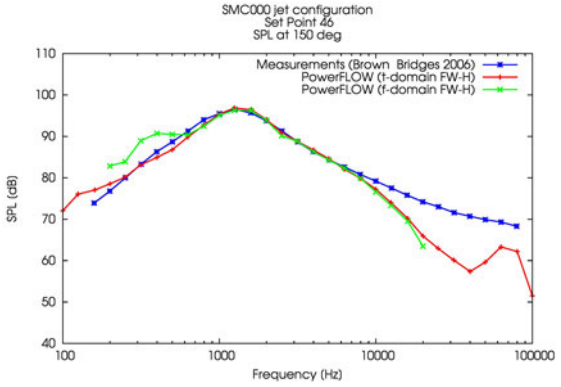




90°



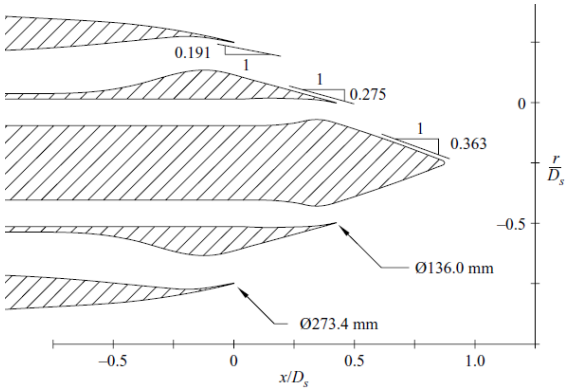

135°

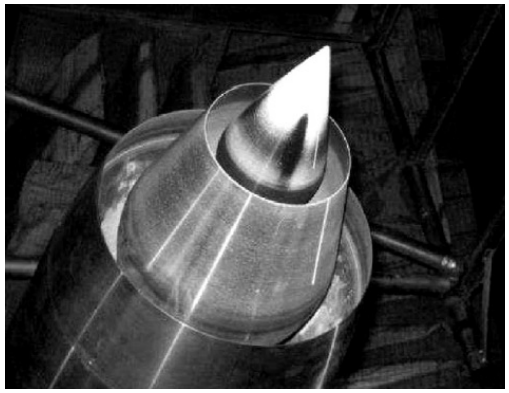



150°

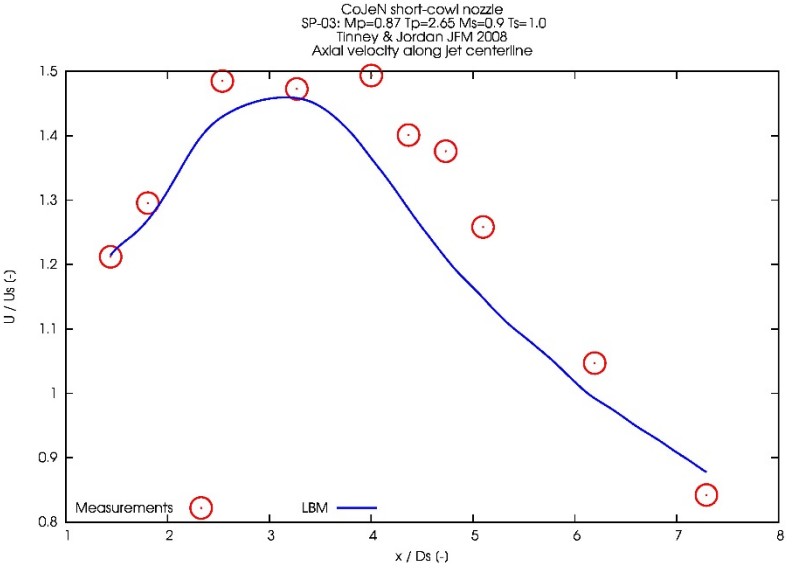

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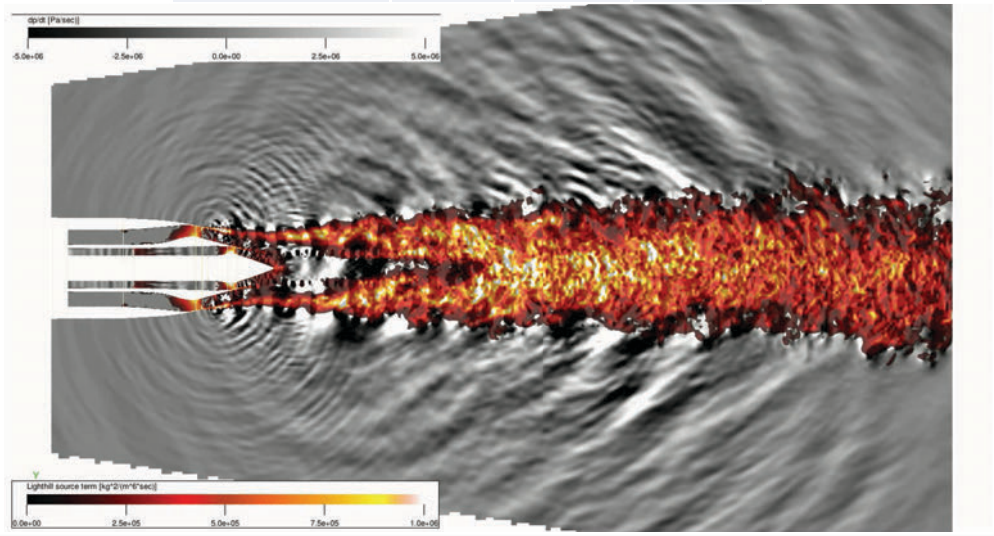
# Co-axial Nozzle case

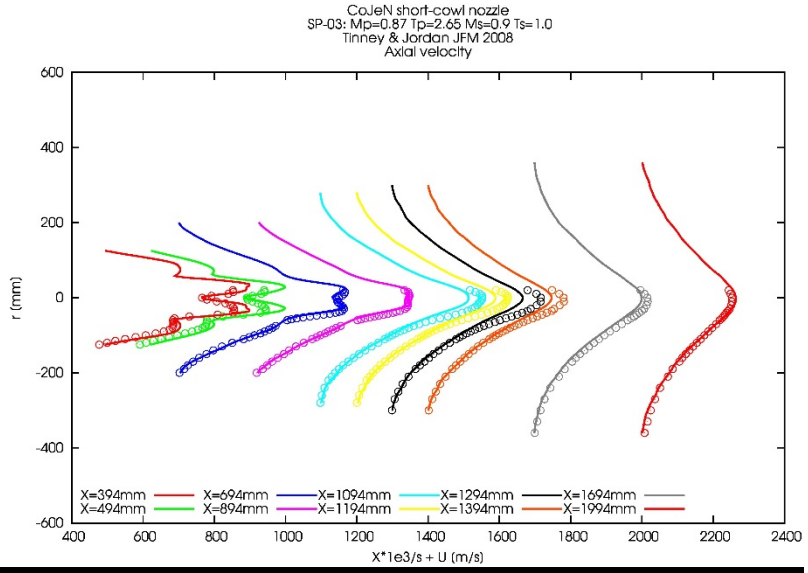


| jet | M | Ma | Tr |
|---|---|---|---|
| primary | 0.87 | 1.41 | 2.65 |
| secondary | 0.90 | 0.90 | 1.0 |



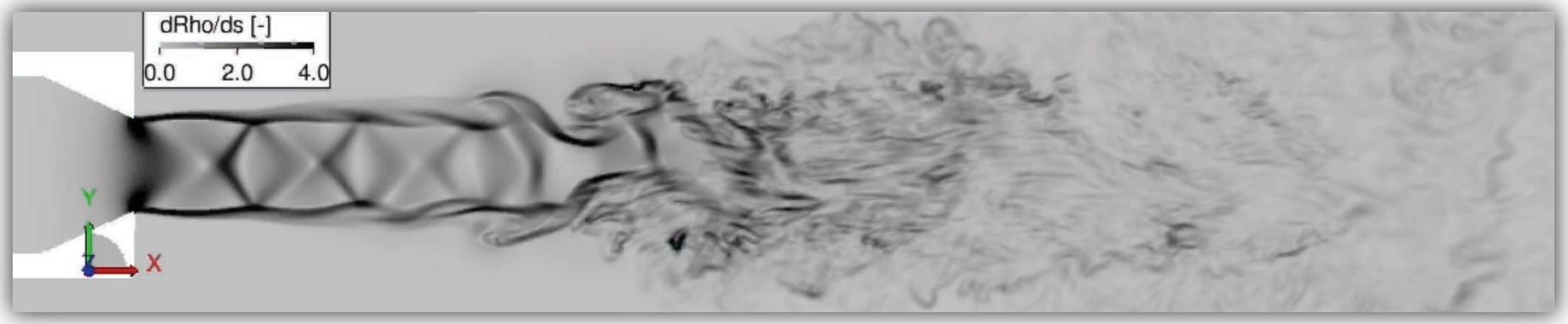







Tinney & Jordan, JFM 611, 2008 – co-axial subsonic jets
© Exa Corporation

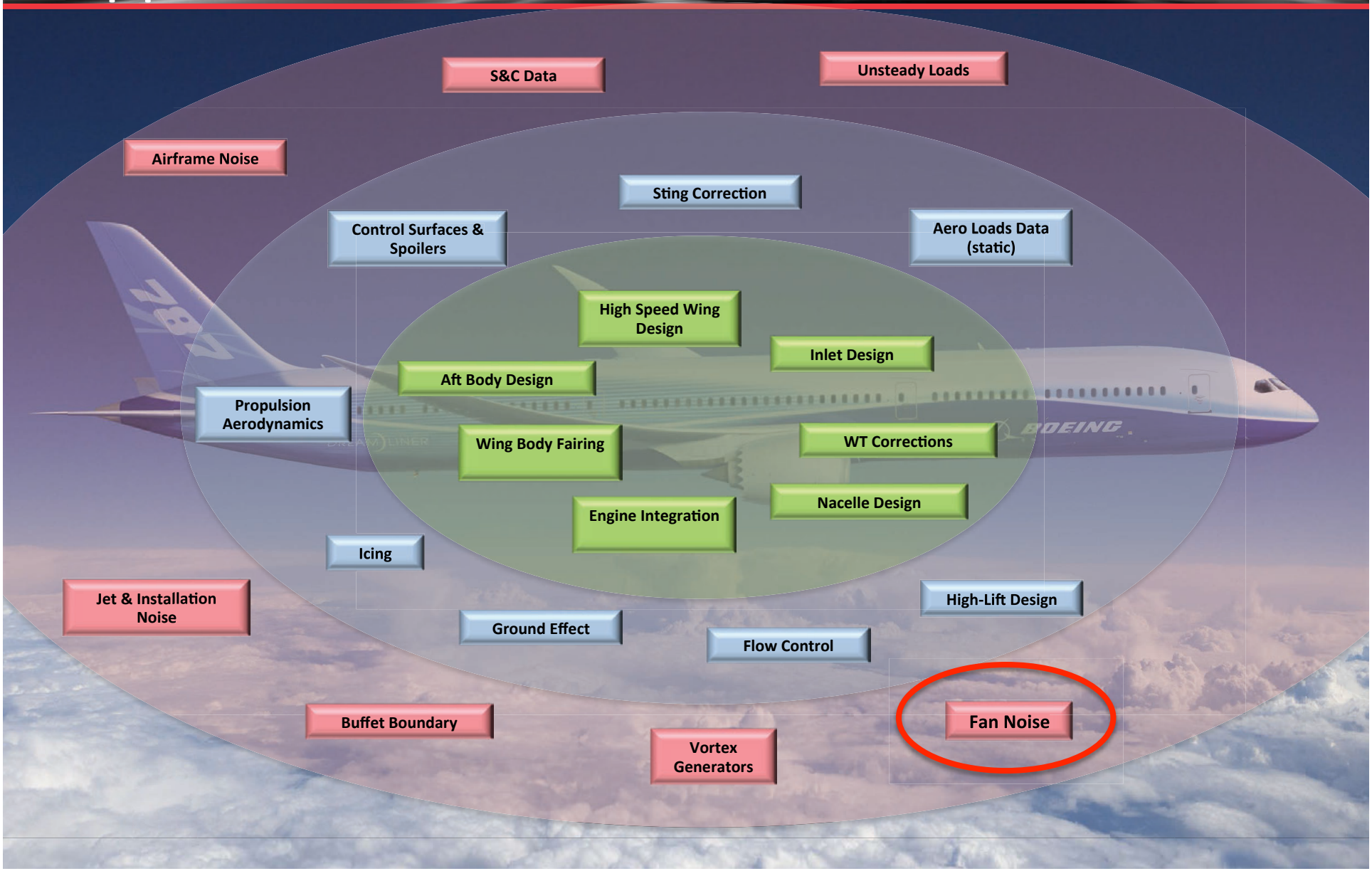
# Supersonic Jets (Work in Progress)



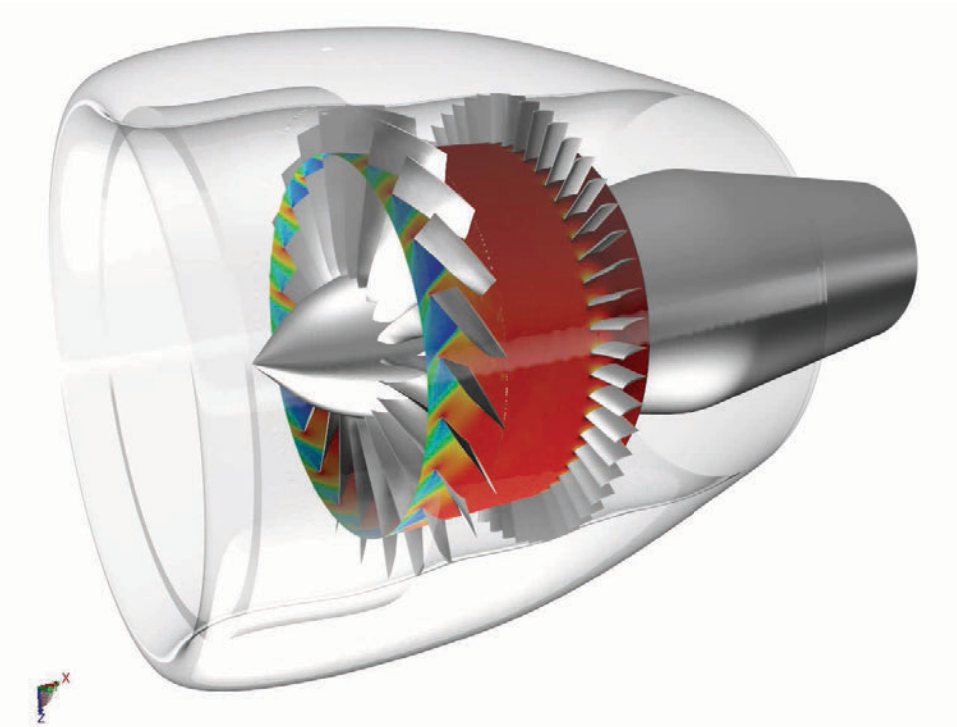


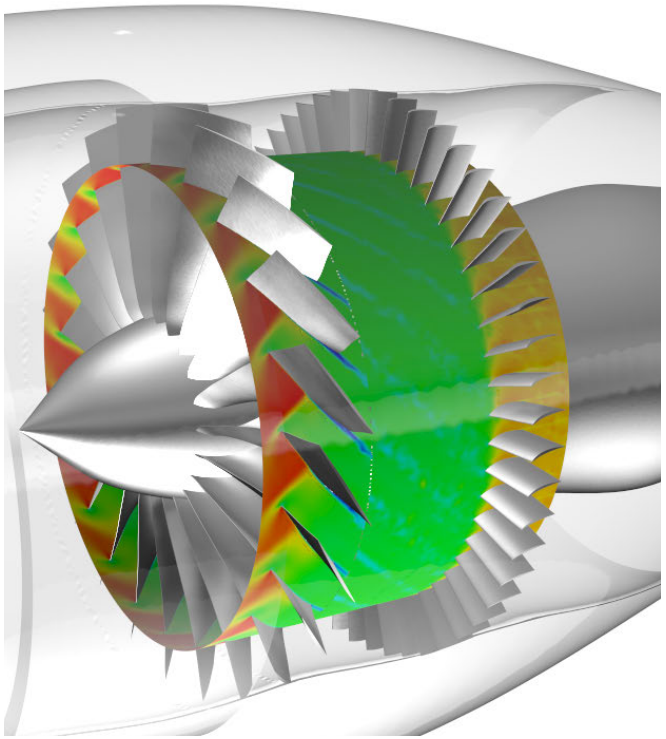
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# Applications



# RC2 Case @12567 rpm



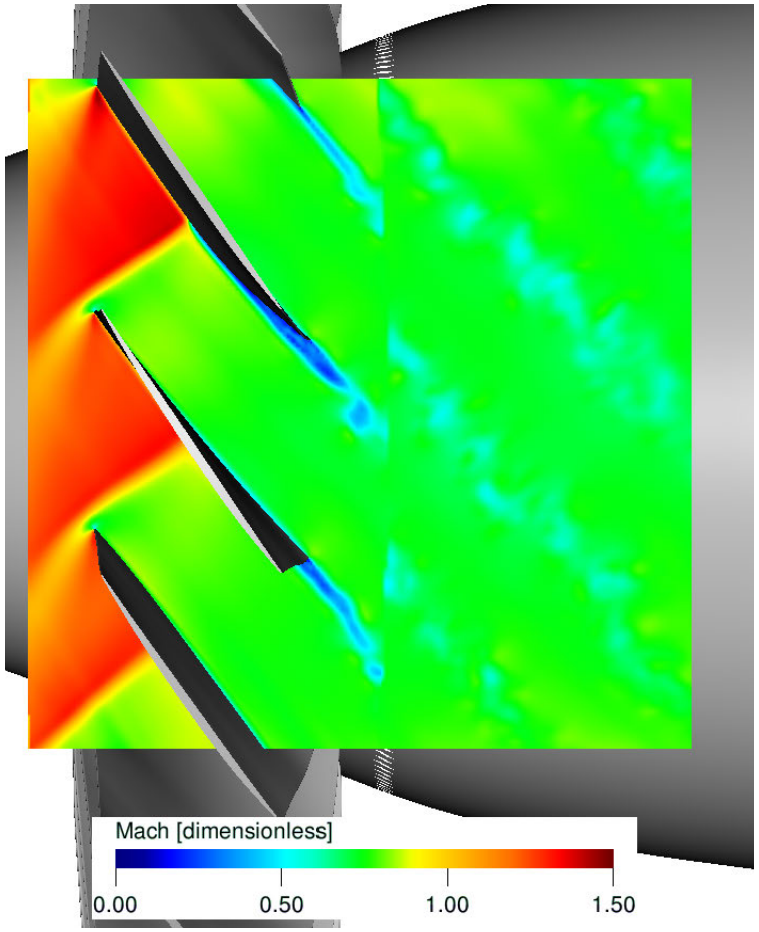



**Density on rotor suction side**

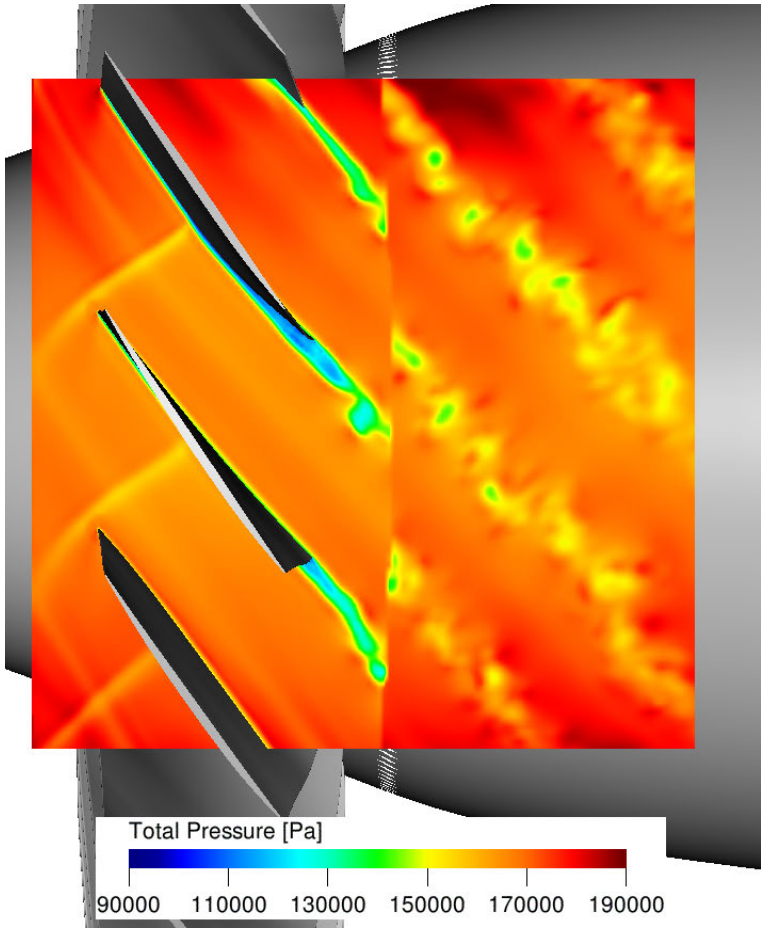

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# Flow analysis: slice @ r/R=0.8

## Relative Mach number




## Total Pressure

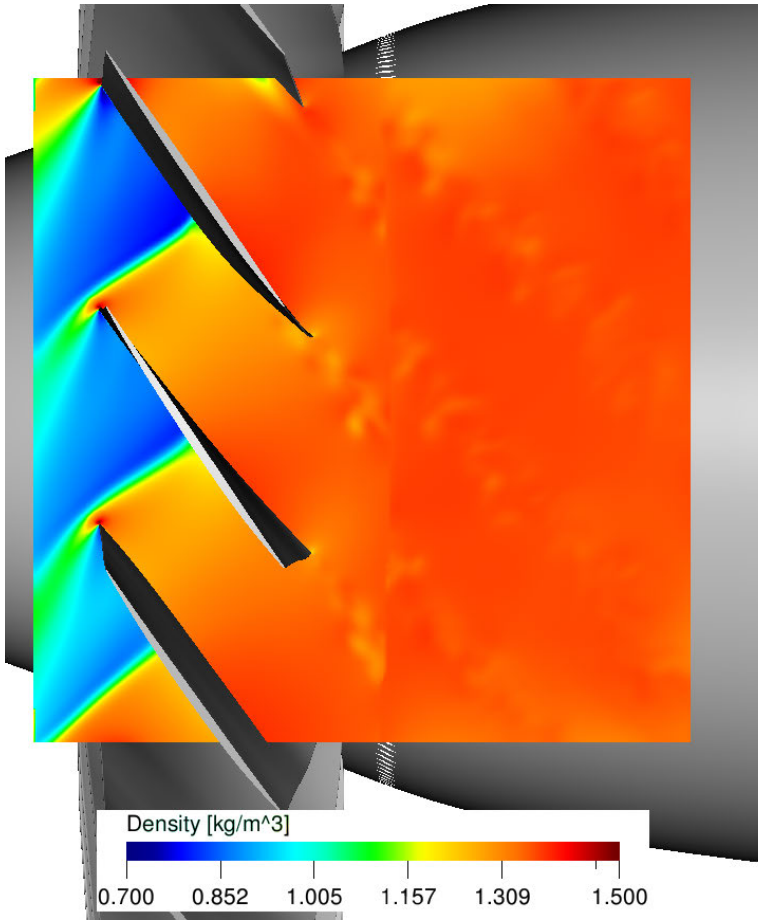




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# Flow analysis: slice @ r/R=0.8

## Density



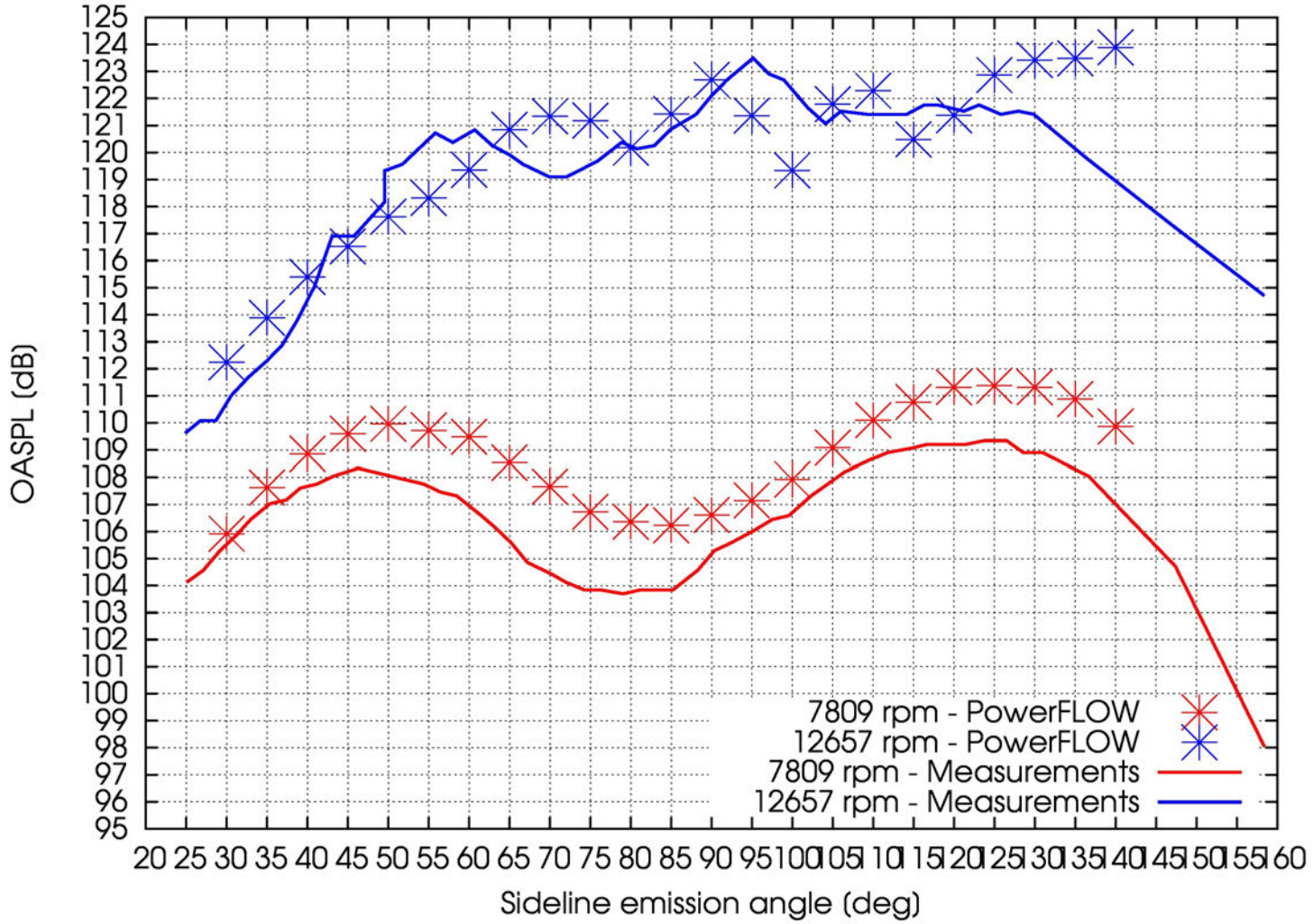

## Density Gradient





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# Far-field noise results

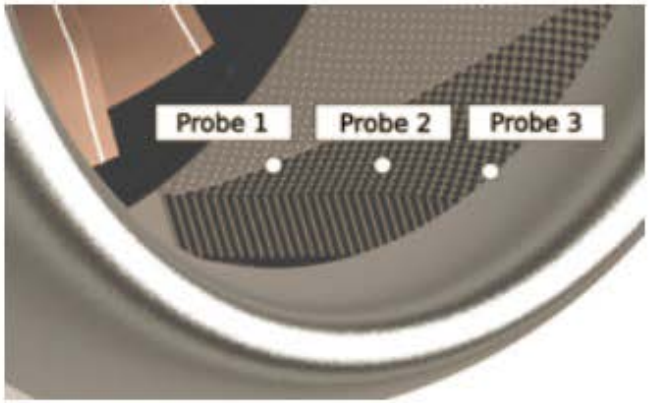


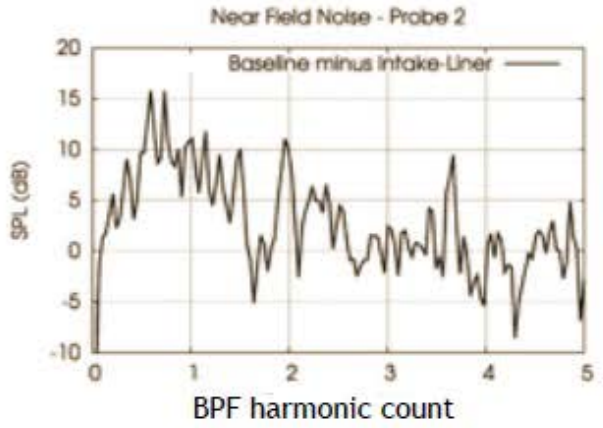


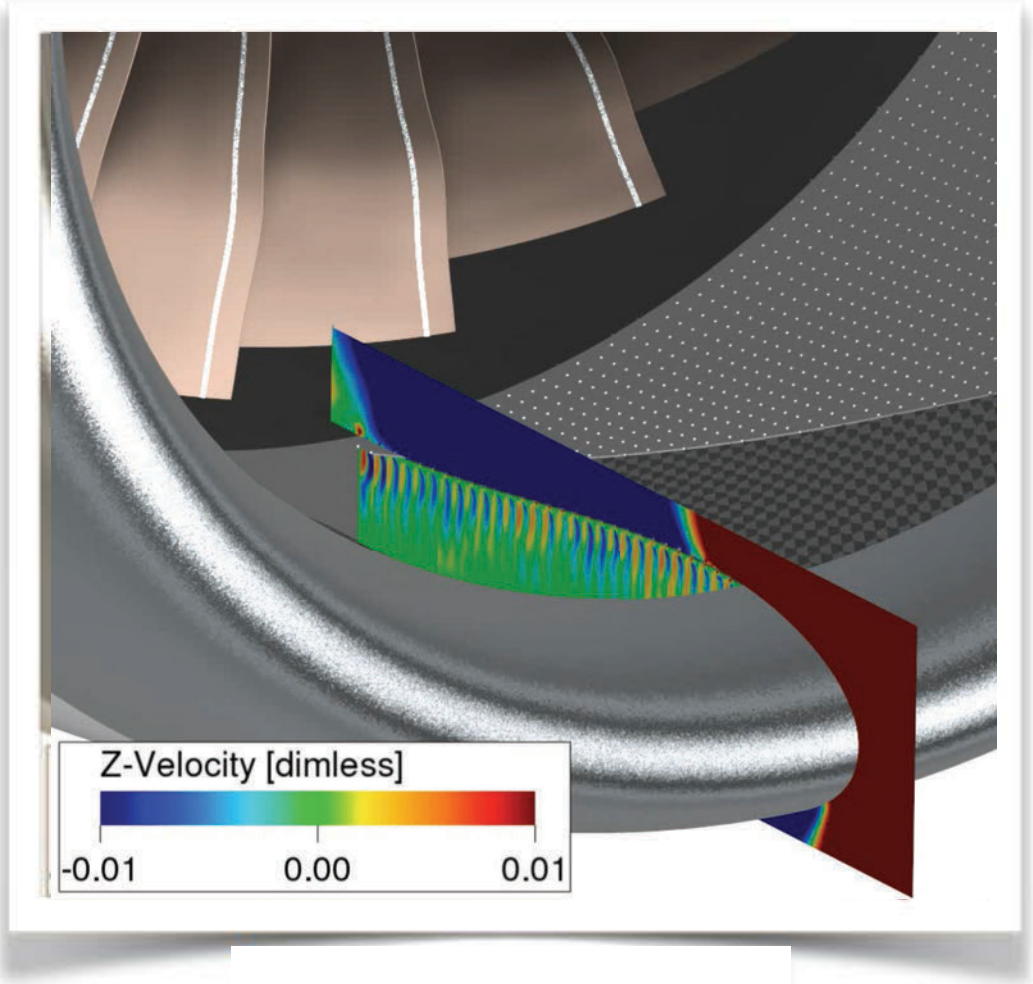
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# Liner Simulation - Preview

- 1 DoF honeycomb liner
- Realistic orifice diameter, face sheet thickness and porosity (> 8000 orifices and honeycomb cells)
- Optimal design for BPF-2 and ~BPF-4
- Expected broadband properties because of slightly variable depth



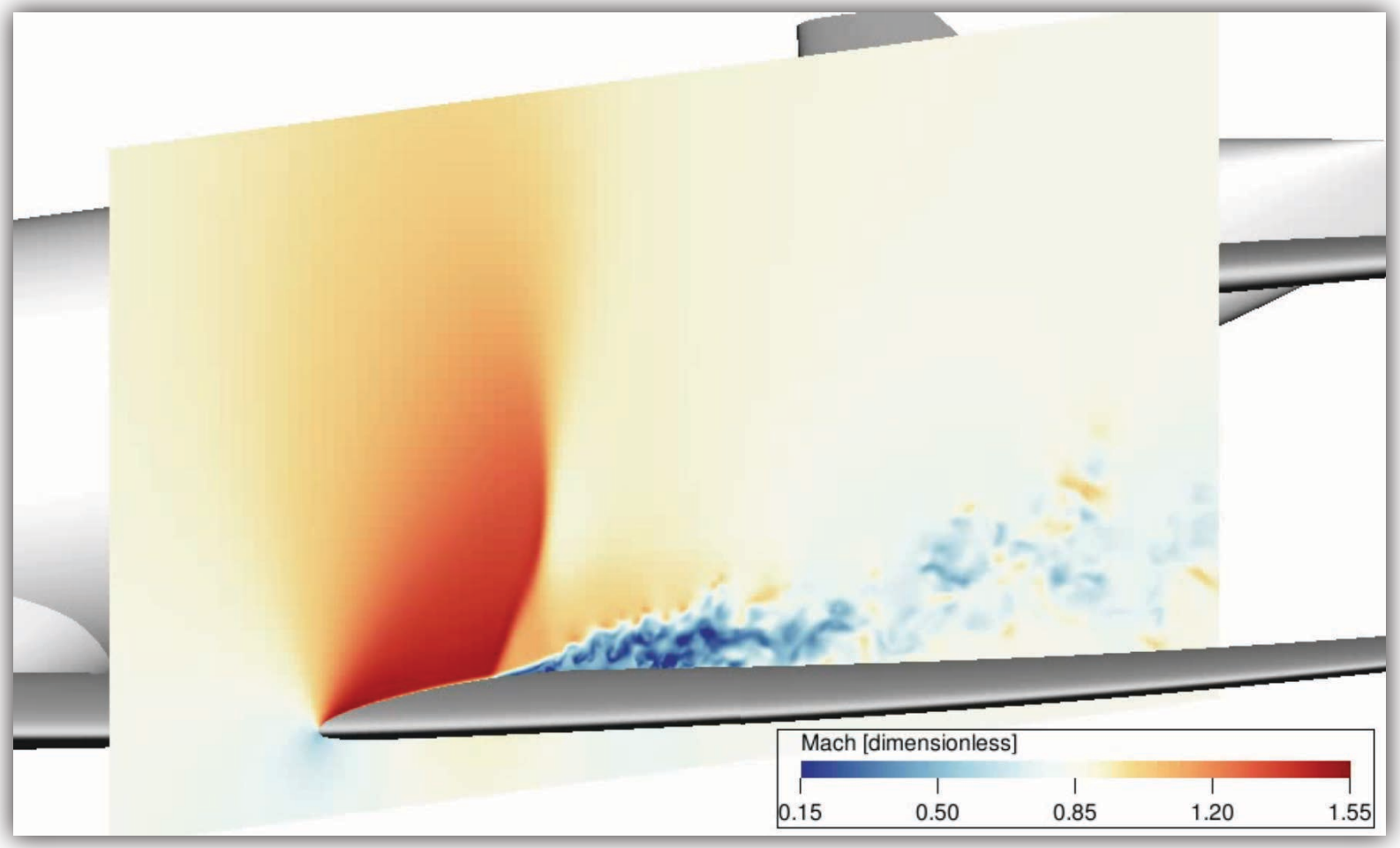





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# Outlook: High-Speed Buffet

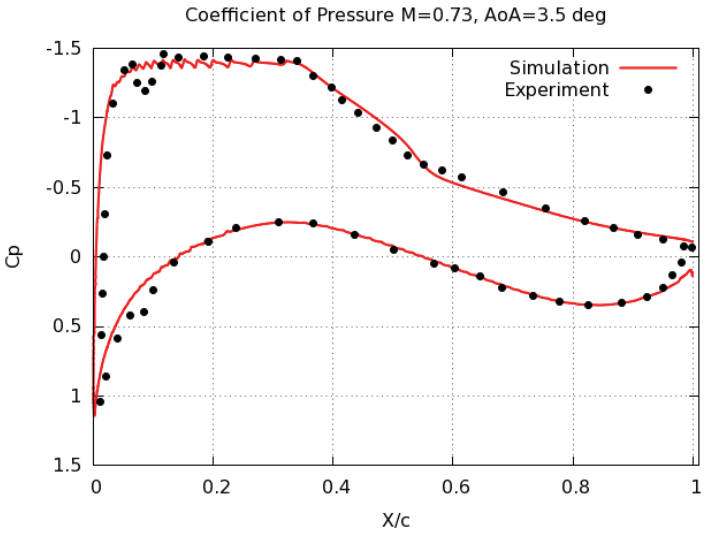


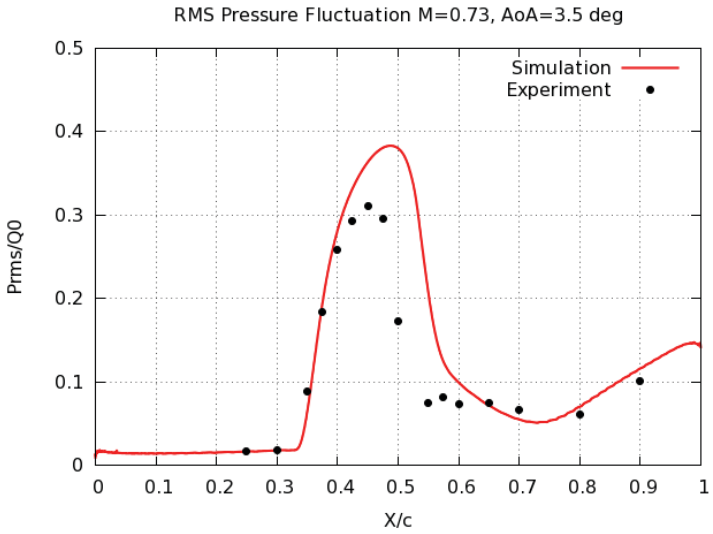


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# Transonic/Buffeting (Preliminary)

- Buffeting study on OAT15A Supercritical Airfoil
  - *Shock wave- boundary layer interaction involving large scale instabilities.*
  - *Preliminary 2D simulation at M= 0.73, angle of attack= 3.5$^0$, Re≈ 3e6*



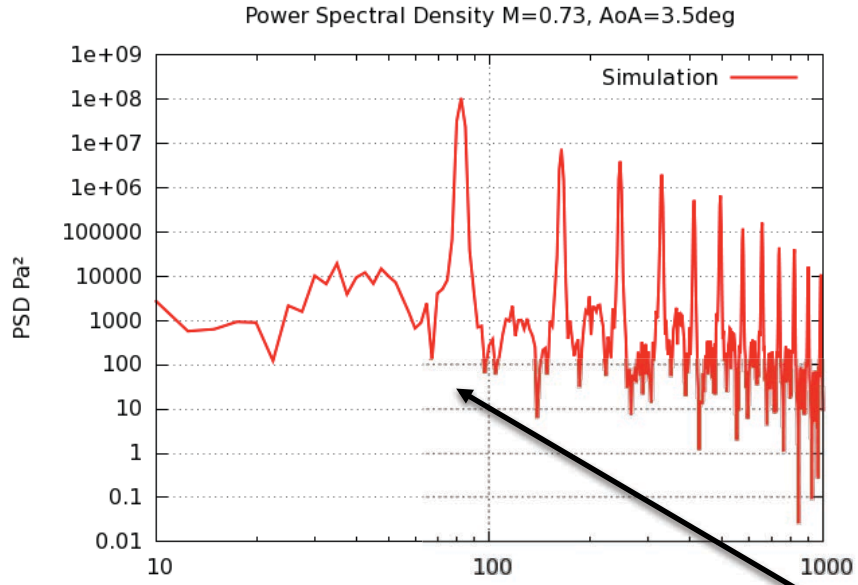

  - *Close agreement of average coefficient of pressure over the surface and amplitude of oscillation with experiments*.*

***Reference**: Jacquin L., Molton P., Deck S., Maury B., Soulevant D., 'An Experimental Study of Shock Oscillation over a Transonic Supercritical Profile', AIAA Journal Vol 47, No 9, 2009.

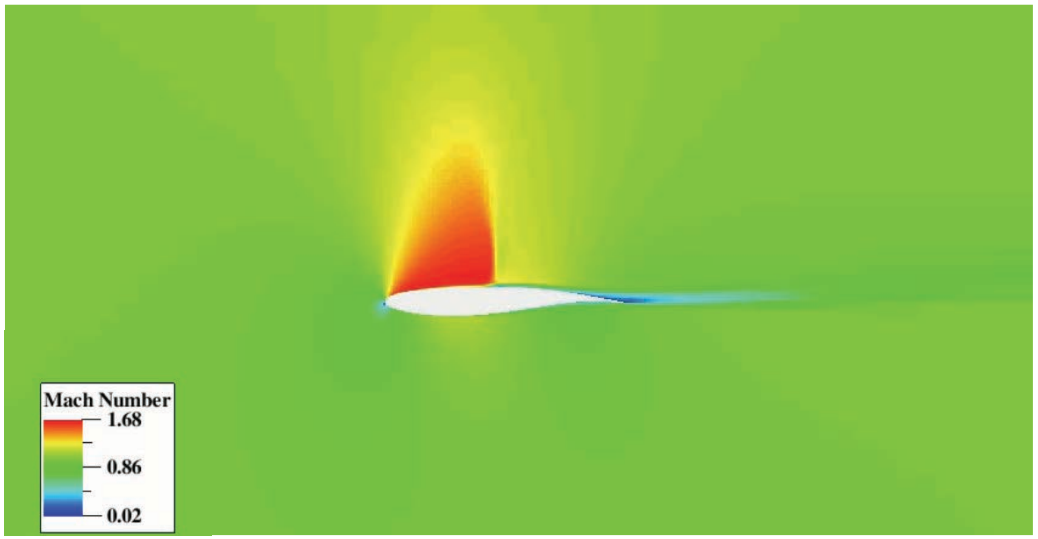

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# Transonic/Buffeting (Preliminary)

- Buffeting study on OAT15A Supercritical Airfoil (2D)




Pressure power spectrum of surface signal
45% chord length




Mach number field

*Frequency of oscillation (experiments):* ***78 Hz***
*Obtained frequency:* ***82 Hz***


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# Summary

- Extension of LBM to transonic & supersonic flows
  - *Achieved through hybrid higher-order LBM scheme*
  - *Enables simulations up to ~Mach 2.0*
  - *Preserves all key advantages of low speed LBM versions*
- Main Initial Application Targets
  - *Unsteady high-speed aerodynamics (buffet, …)*
  - *Flow control*
  - *Propulsion noise: fan, jet & installation noise*
- Status of LBM with regard to CFD Vision 2030 Report
  - *Efficient handling of unsteady turbulent flows with significant regions of separation*
  - *Mesh generation*
  - *Robustness and automation of CFD simulations*
  - *Efficient use of HPC infrastructure*
  - *Managing very large amounts of data*
  - *Multi-disciplinary analysis & optimization*





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# Thank You!


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